



Suppose we have a population of adult men with a mean height of 71 inches and standard deviation of 2.5 inches. We also have a population of adult women with a mean height of 65 inches and standard deviation of 2.3 inches. In this case the researcher is interested in comparing the mean height between men and women. His research question is: **Does the mean height of men differ from the mean height of women?**. Here, the hypotheses are

 $H_0: \mu_1 = \mu_2$ $H_1: \mu_1 \neq \mu_2$

where,

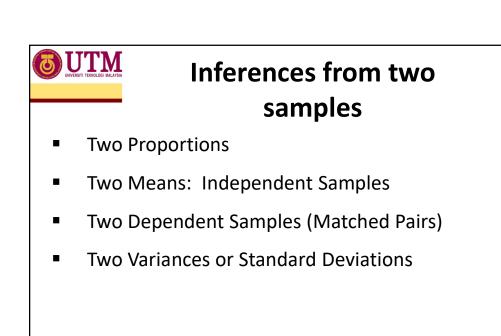
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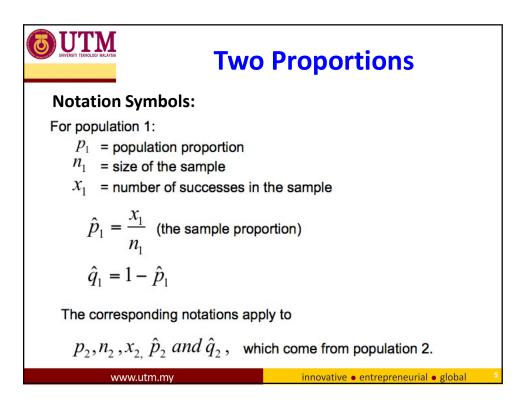
 m_1 = mean height of men m_2 = mean height of women

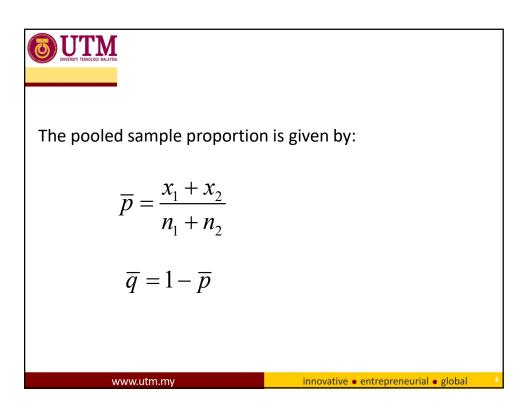
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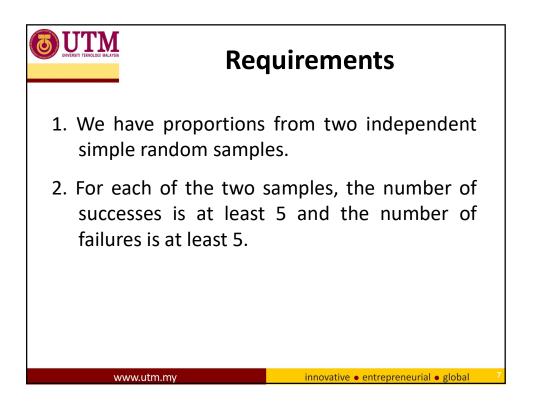
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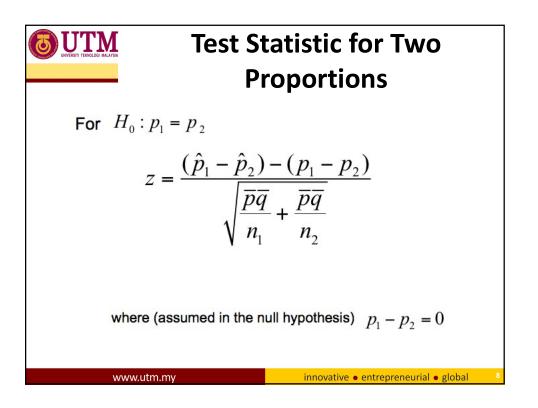


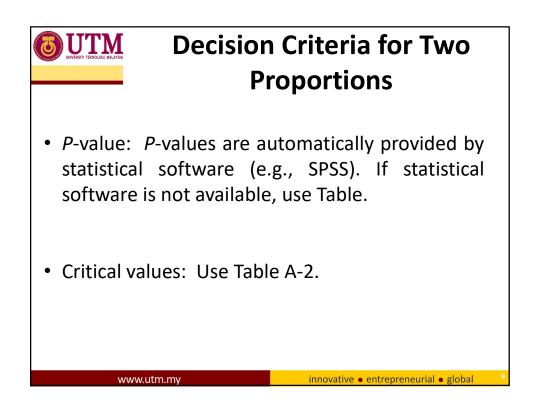


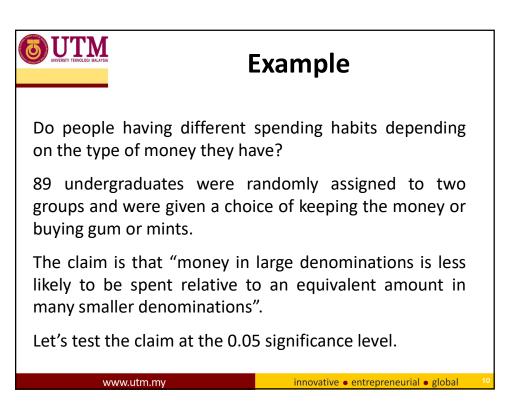




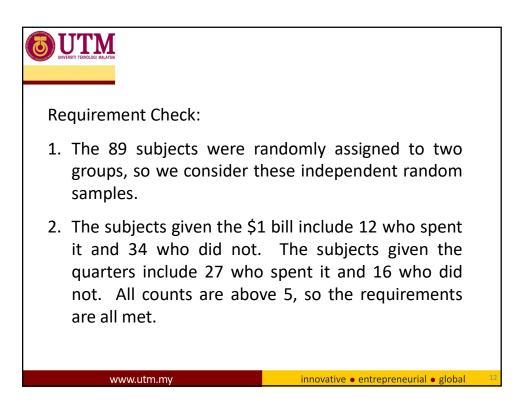


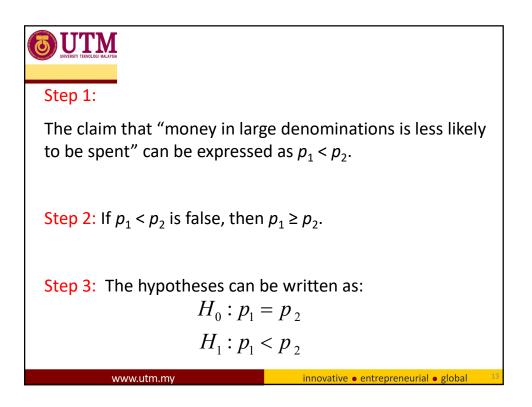


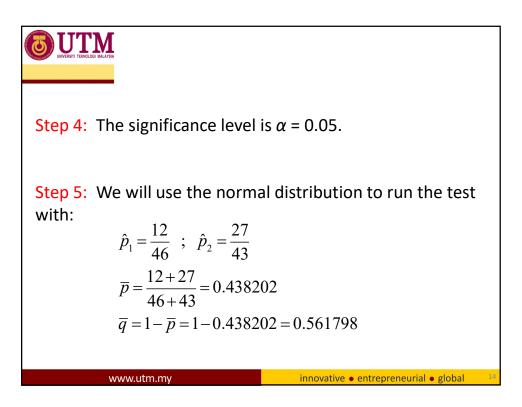


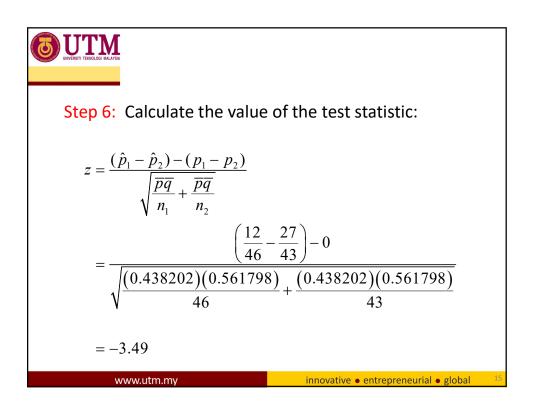


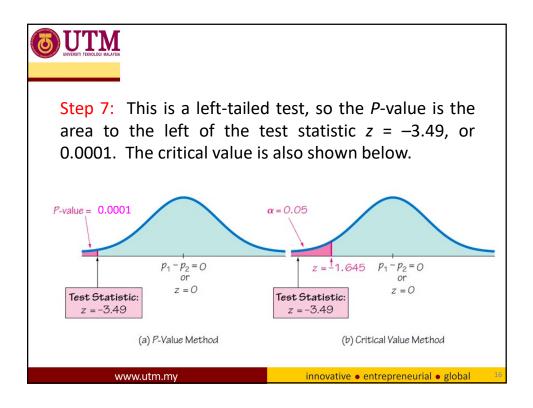
UNIVERSITI YEMIGLOGI INALAYEM	Example - S	olution
• Below are the s	ample data and sum	mary statistics:
	Group 1	Group 2
	Subjects Given \$1	Subjects Given 4 quarters (1 quarter = 25 cent)
Spent the money	x ₁ =12	x ₂ =27
Subjects in group	n ₁ =46	n ₂ =43
	$\hat{p}_1 = \frac{12}{46}$; $\hat{p}_2 = \frac{27}{43}$	
	$\overline{p} = \frac{12 + 27}{46 + 43} = 0.43820$	02
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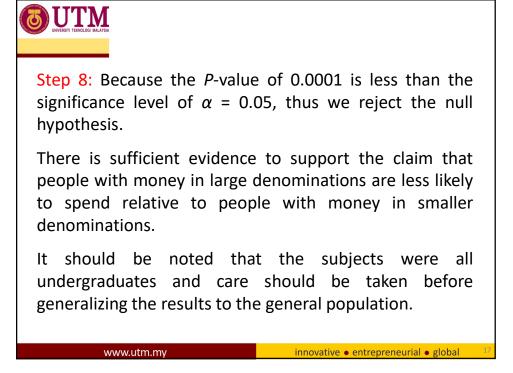




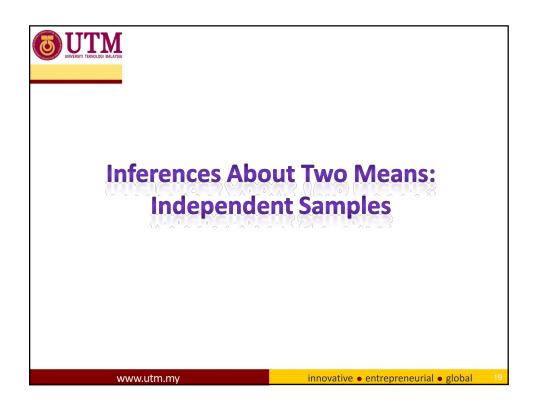


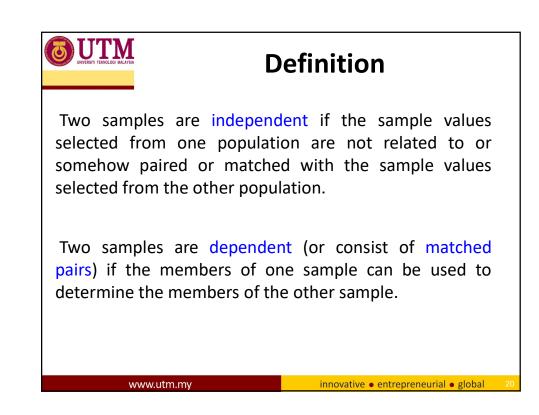


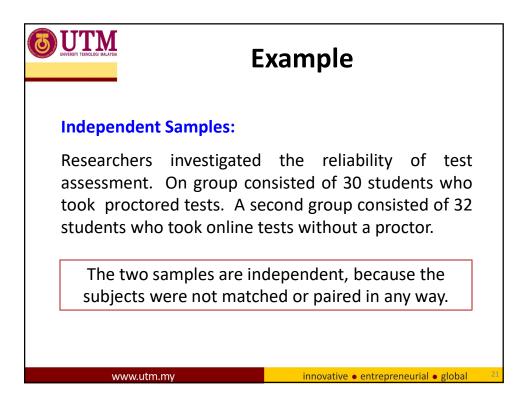




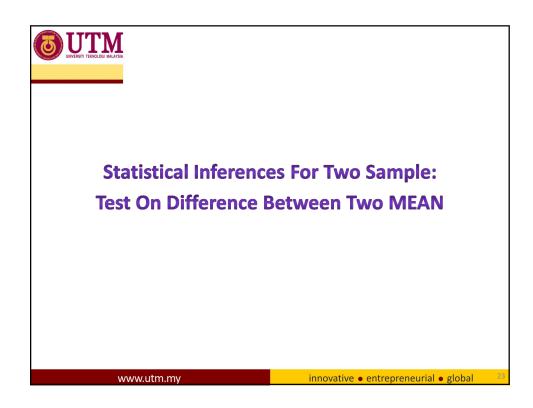
	ercise #1
800 adult Americans. The que who were surveyed was:	result of a telephone poll of estion posed of the Americans "Should the federal tax on for health care reform?" The
Non-smoker	Smoker
N ₁ = 605	N ₂ = 195
Y ₁ = 351 said yes	Y ₂ = 41 said yes
	the α = 0.05 level, to conclude smokers and non-smokers) is t to their opinions?
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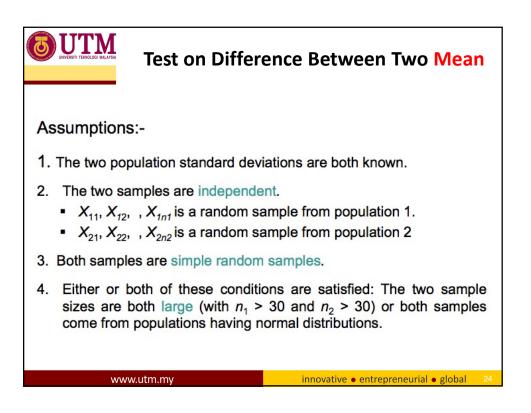


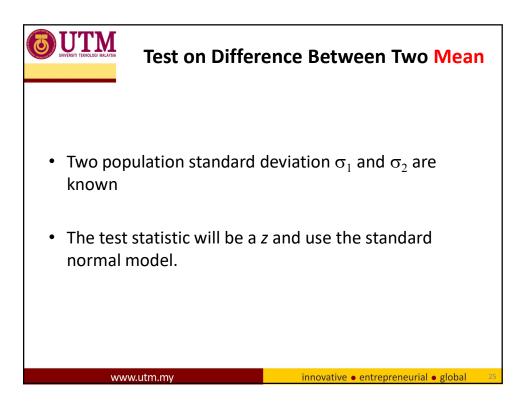


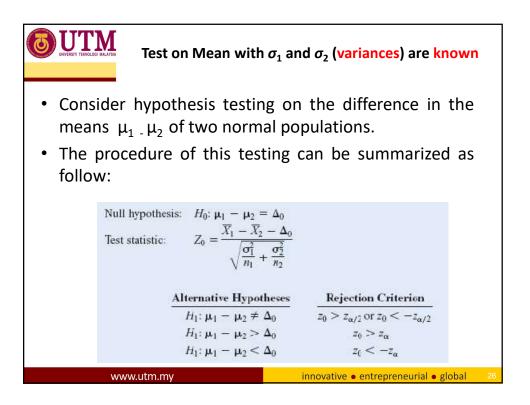


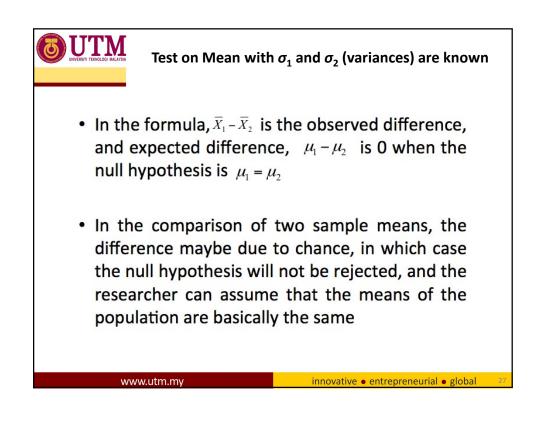
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Depende	nt Samp	les:			
	cm) of hu	sbands a	nd the h	eights (ci	ting of the m) of their 178
Husband Height of Wife	160	165	163	162	166

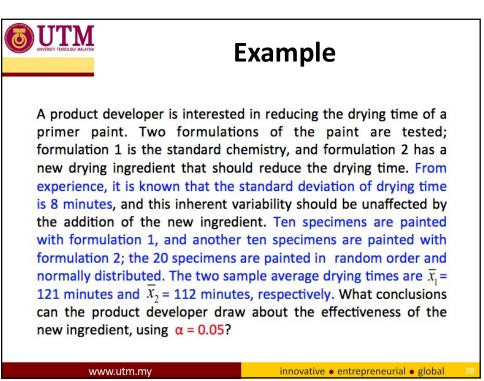




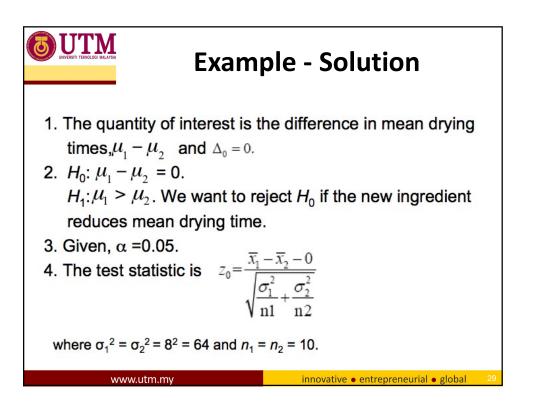


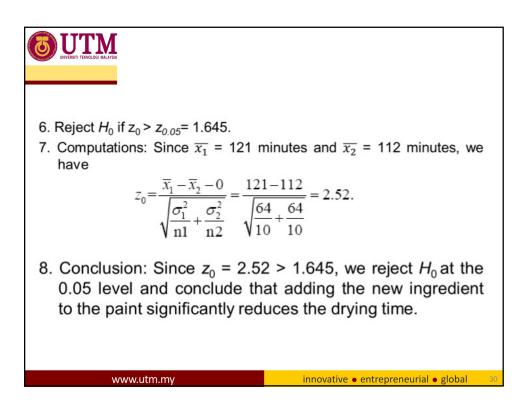






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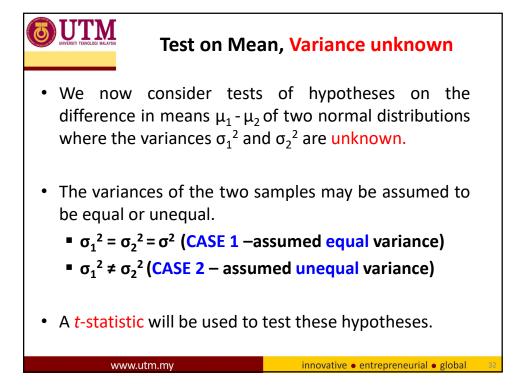


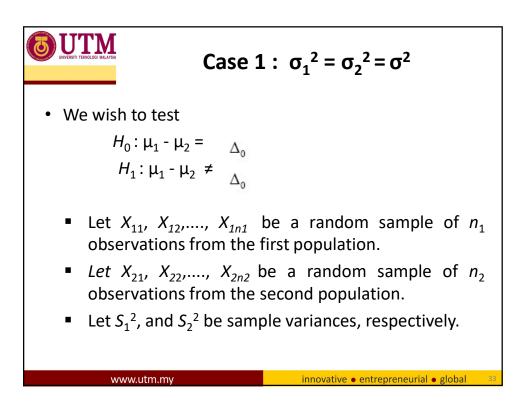


Exercise #2

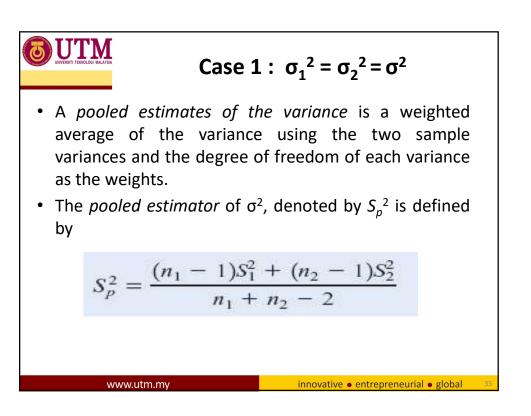
According to the American Medical Association, the average annual of radiologists in the USA are \$230,000 and those of surgeons are \$225,000. Suppose that these means are based on random samples of 300 radiologists and 400 surgeons and that the population standard deviations of the annual earnings of radiologists and surgeons are \$28,000 and \$32,000 respectively. Determine whether there is a difference between the mean annual earnings of radiologists and surgeons with 97% confidence interval.

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• The proce	edure of testing:	
Null hypothe	esis: H_0 : $\mu_1 - \mu_2 = \Delta_0$	
Test statistic	$T_0 = \frac{\overline{X}_1 - \overline{X}_2 - \Delta}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$	<u></u>
	$\frac{\text{Alternative Hypothesis}}{H_1: \mu_1 - \mu_2 \neq \Delta_0}$	$\frac{\text{Rejection Criterion}}{t_0 > t_{\alpha/2,n_1+n_2-2} \text{ or}}$ $t_0 < -t_{\alpha/2,n_1+n_2-2}$
	$egin{array}{ll} H_1\colon oldsymbol{\mu}_1 - oldsymbol{\mu}_2 > \Delta_0 \ H_1\colon oldsymbol{\mu}_1 - oldsymbol{\mu}_2 < \Delta_0 \end{array}$	$t_{0} > t_{\alpha/2,n_{1}+n_{2}-2}$ $t_{0} > t_{\alpha,n_{1}+n_{2}-2}$ $t_{0} < -t_{\alpha,n_{1}+n_{2}-2}$
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Example

Two catalysts are being analyzed to determine how they affect the mean yield of a chemical process. Specifically, catalyst 1 is currently in use, but catalyst 2 is acceptable. Since catalyst 2 is cheaper, it should be adopted, providing it does not change the process yield. A test is run in the pilot plant and results in the data shown in Table 1 (next page). Is there any difference between the mean yields? Conduct the t-test with $\alpha = 0.05$, and assume equal variances.

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	Table 1	
Observation Number	Catalyst 1	Catalyst 2
1	91.50	89.19
2	94.18	90.95
3	92.18	90.46
4	95.39	93.21
5	91.79	97.19
6	89.07	97.04
7	94.72	91.07
8	89.21	92.75
	$x_1 = 92.255$	$x_2 = 92.733$
	$s_1 = 2.39$	$s_2 = 2.98$

Example - Solution

1. The parameters of interest are μ_1 and μ_2 , the mean process yield using catalysts 1 and 2, respectively, and we want to know if

$$H_0: \ \mu_1 - \mu_2 = 0.$$

$$H_1: \ \mu_1 \neq \mu_2.$$

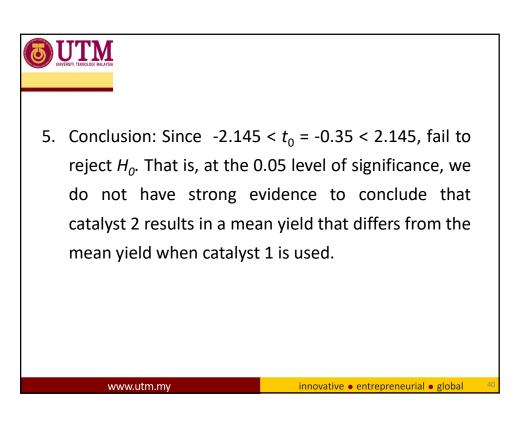
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2. Given, α =0.05. The test statistic is

$$t_0 = \frac{\overline{x_1} - \overline{x_2} - 0}{s_p \sqrt{\frac{1}{n1} + \frac{1}{n2}}}$$

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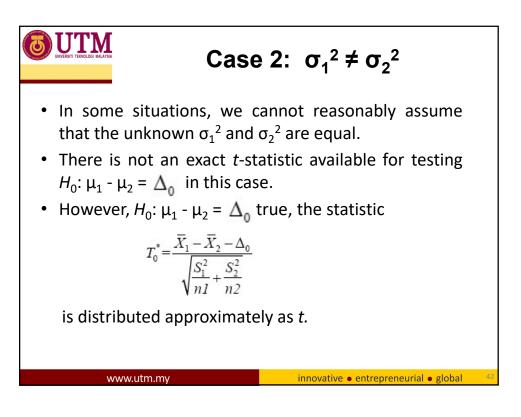
$\begin{aligned} & \underbrace{\textbf{S}. \text{ Reject } H_0 \text{ if } t_0 > t_{0.025, 14} = 2.145, \text{ or} \\ & \text{ if } t_0 < -t_{0.025, 14} = -2.145. \end{aligned} \\ & \textbf{4. Computations: } \overline{\chi}_1 = 92.255, s_1 = 2.39, n_1 = 8, \\ & \overline{\chi}_2 = 92.733, s_2 = 2.98, n_2 = 8: \\ & s_p^2 = \frac{(n1-1)s_1^2 + (n2-1)s_2^2}{n1+n2-2} = \frac{(7)(2.39)^2 + (7)(2.398)^2}{8+8-2} = 7.30, \\ & s_p = \sqrt{7.30} = 2.70, \\ & \text{and} \\ & t_0 = \frac{\overline{\chi}_1 - \overline{\chi}_2 - 0}{2.70\sqrt{\frac{1}{n1} + \frac{1}{n2}}} = \frac{92.255 - 92.733}{2.70\sqrt{\frac{1}{8} + \frac{1}{8}}} = -0.35. \end{aligned}$

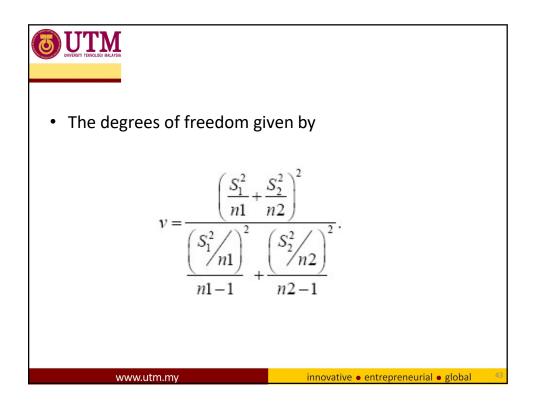


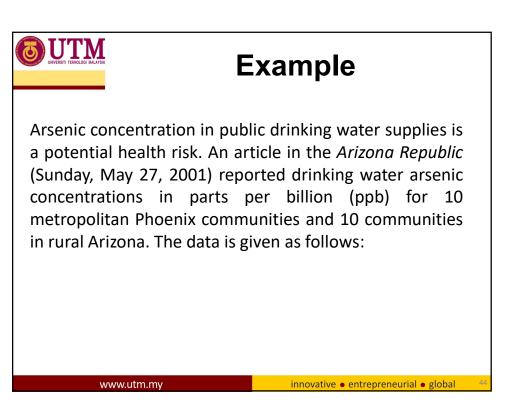
Exercise #3

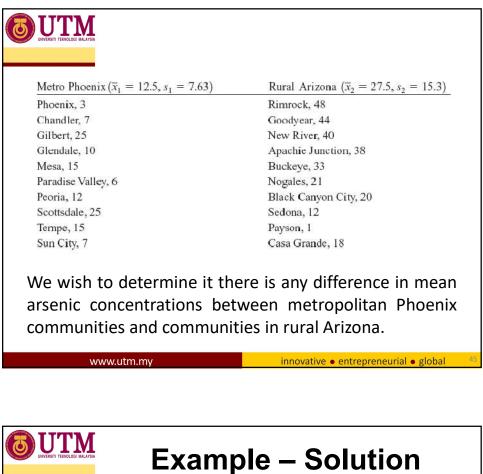
A sample of 15 children from City A showed that the mean time they spend watching television is 28.5 hours per week with a standard deviation of 4 hours. Another sample of 16 children from City B showed that the mean time they spend watching television is 23.25 hours per week with a standard deviation of 5 hours. Using a 2.5% significance level (95% CI), can you conclude that the mean time spent watching television by children in City A is greater than that for children in City B? Assume that the time spent watching television by children have a normal distribution for both populations and that the standard deviations for the two populations are equal.

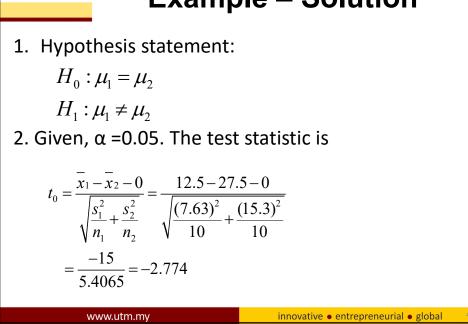
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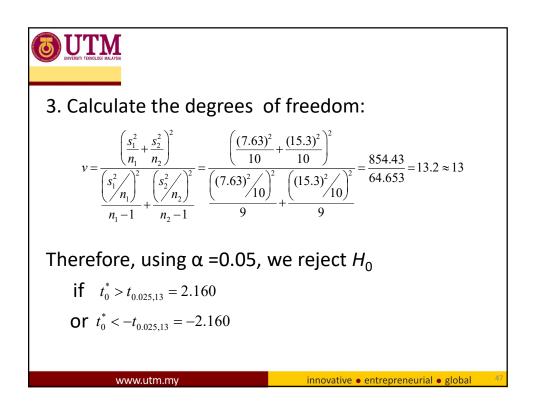












4. Conclusion:

Since, $t_0 = -2.77 < -t_{0.025, 13} = -2.160$, we reject the null hypothesis. There is evidence to conclude that mean arsenic concentration in the drinking water in rural Arizona is different from the mean arsenic concentration in metropolitan Phoenix drinking water.

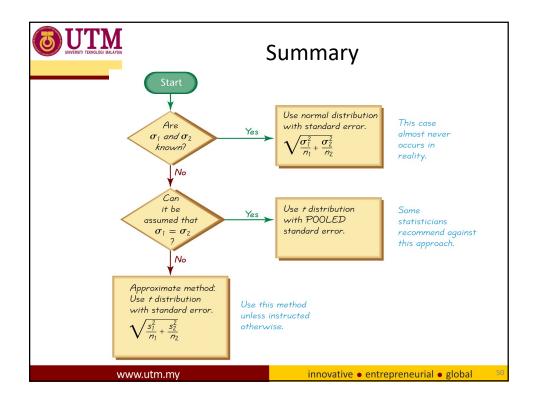
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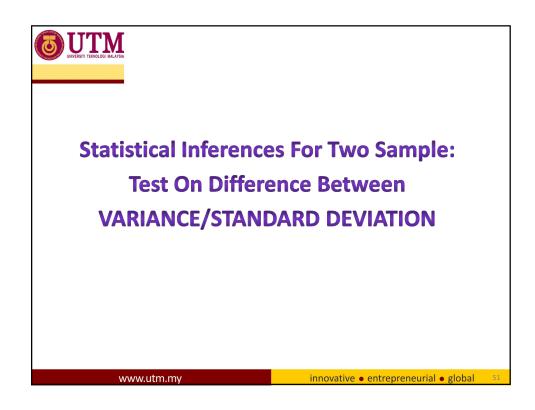
Exercise #4

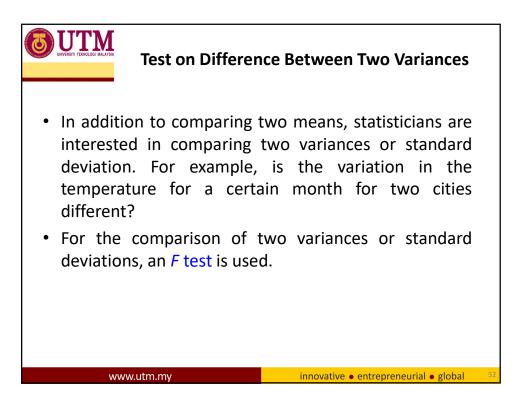
A sample of 14 cans of Brand I diet soda gave the mean number of calories per can as 23 with a standard deviation of 3 calories. Another sample of 16 cans of Brand II diet soda gave the mean number of calories per can as 25 with a standard deviation of 4 calories. Test at the 1% significance level (99% CI) whether the mean numbers of calories per can of diet soda are different for these two brands. Assume that the calories per can of diet soda are normally distributed for each of these two brands and that the standard deviations for the two populations are not equal.

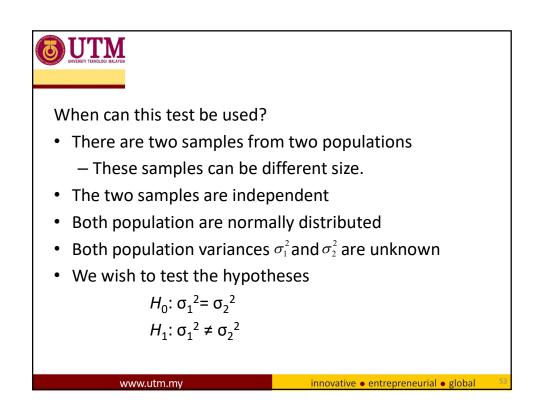
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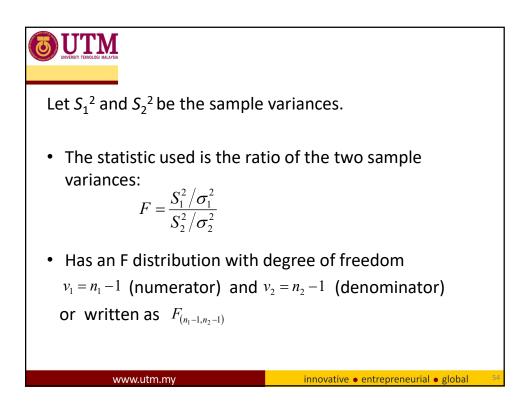
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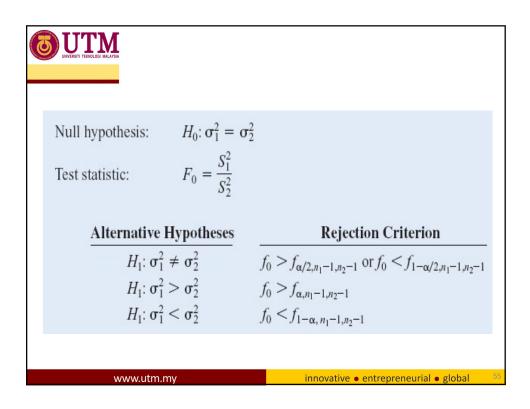


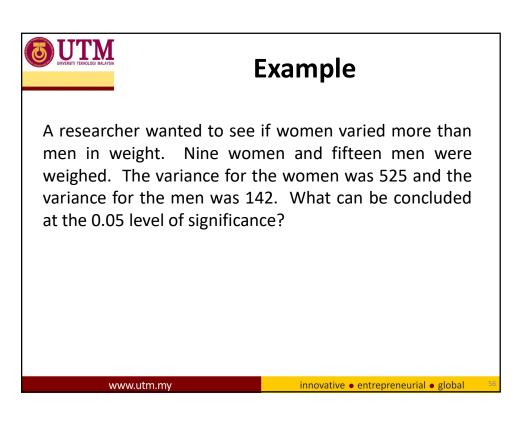


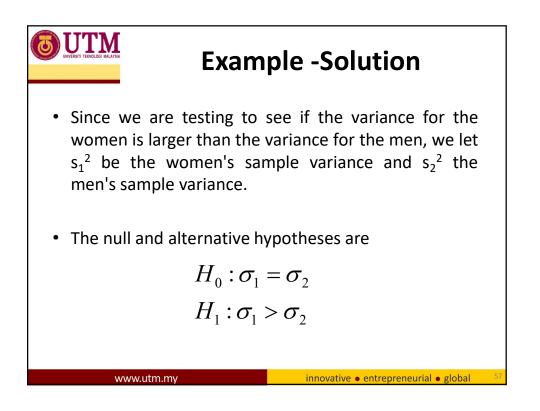


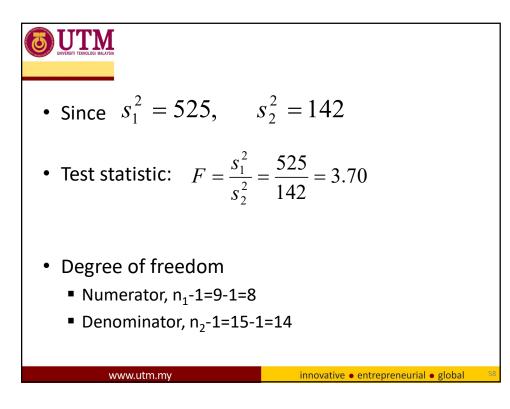












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Defe		F tab			F		F_0	05,8,14	= 2.	/0
Refe	er to i	F-tap	ole, α	=0.0	5		0.	05,6,14	1	
			00.57		Degr	ees of freed	lom in num	erator (df1)		
	p	1	2	3	4	5	6	7	8	<u>_</u>
10	0.100	3.29	2.92	2.73	2.61	2.52	2.46	2.41	2.38	2.
	0.050	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	2.
	0 0 2 5	6 94	546	4 83	4 47	4 7 4	4 07	3 95	3 85	3
	0.010	10.04	7.56	6.55	5.99	5.64	5.39	5_20	5.06	4.
	0.001	21.04	14.90	12.55	11.28	10.48	9.93	9.52	9.20	8.
12	0.100	3.18	2.81	2.61	2.48	2.39	2.33	2.28	2.24	2
	0.050	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2
	0.025	6.55	5.10	4.47	4.12	3.89	3.73	3.61	3.51	3.
	0.010	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.
	0.001	18.64	12.97	10_80	9.63	8.89	8.38	8_00	7.71	7.
14	0.100	3.10	2.73	2.52	2.39	2.31	2.24	2.19	2 15	2.
	0.050	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2
	0.025	6.30	4.86	4.24	3.89	3.66	3.50	3.38	3.29	3.
	0.010	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	3.
	0.001	17.14	11.78	9,73	8.62	7.92	7.44	7.08	6.80	6



• Conclusion:

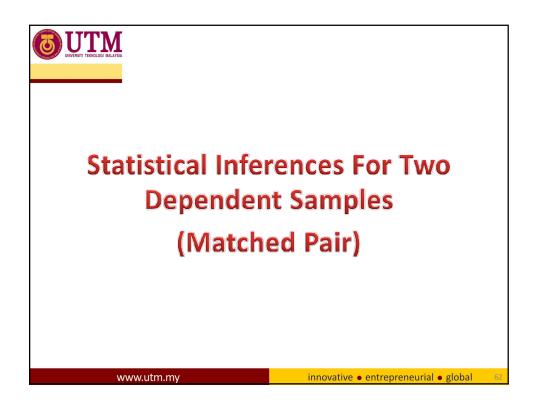
Since $F = 3.70 > F_{0.05,8,14} = 2.70$, we reject the null hypothesis. Hence, we have significant evidence to conclude that the variance for all female weights is larger than the variance for all male weights.

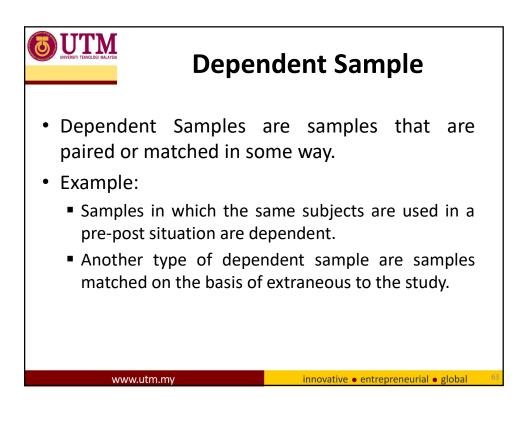
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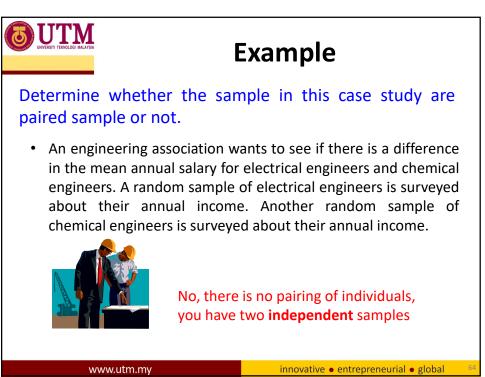
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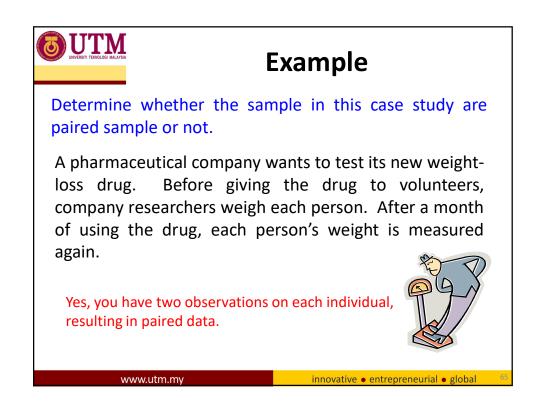
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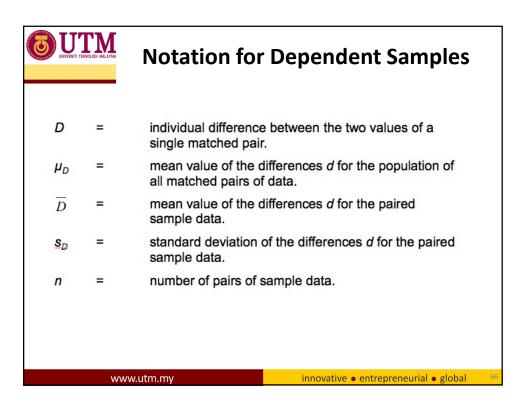
UNVERSITI TEKNOLOGI HALAYSIA		Exercise	#5
of the head different f who do na data are sh	art rates (ir rom the val ot smoke. 1	wishes to see whet n beats per minuteriance of the heart Two samples are set $\alpha = 0.05$, is there of	e) of smokers is rates of people elected, and the
	Smokers	Non-smokers	
	n ₁ =26	n ₂ =18	-
	s ² =36	s ² =10	
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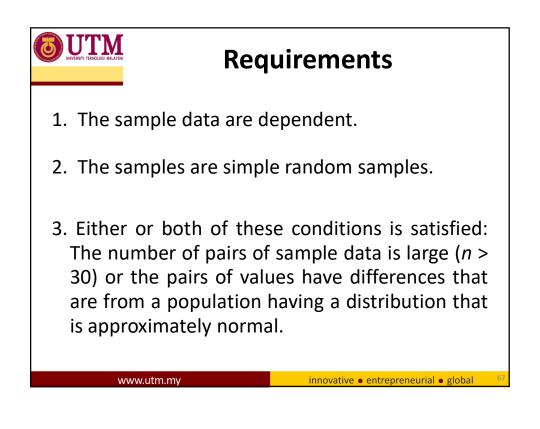


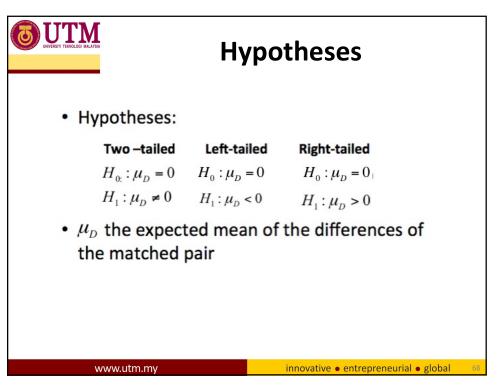


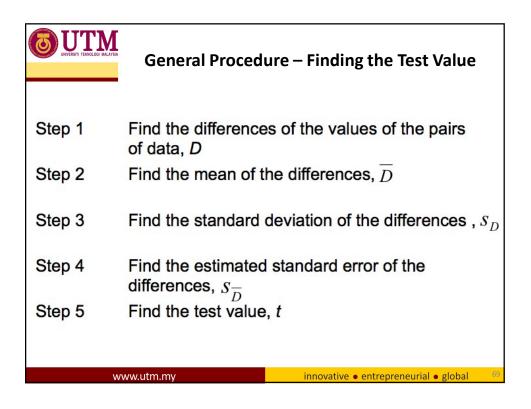


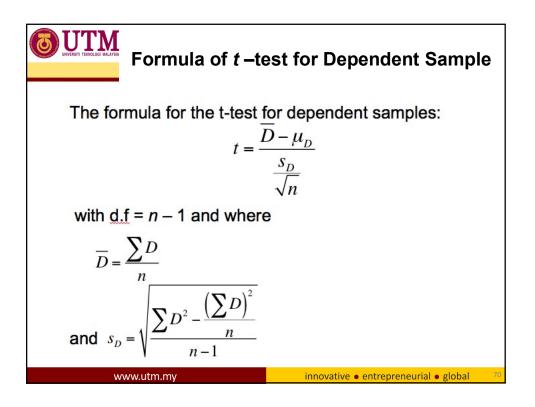










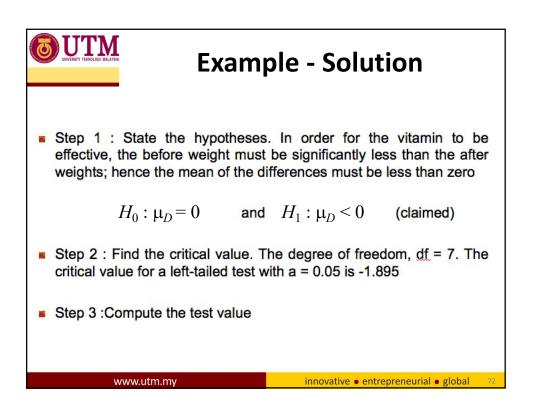


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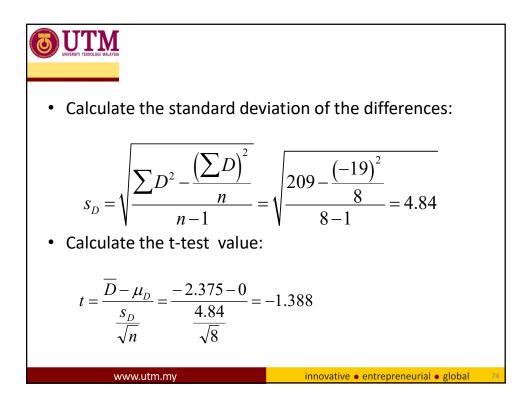
Example

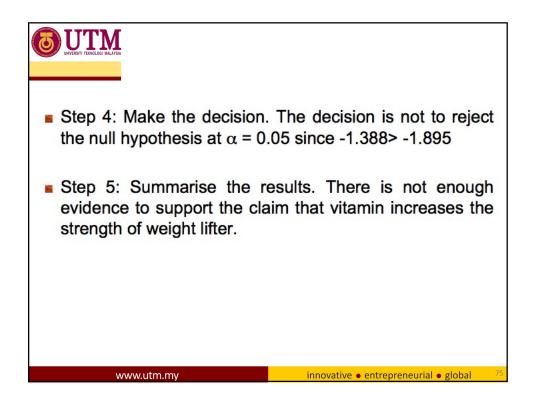
A physical education director claims by taking a special vitamin a weight lifter can increase his strength. Eight athletes are selected and given a test of strength, using the standard bench press. After two weeks of regular training, supplemented with the vitamin, they are tested again. Test the effectiveness of the vitamin regime at a =0.05. Each value in these data represents the maximum numbers of pounds the athlete can bench-press. Assume that the variables is approximately normally distributed

Athlete	1	2	3	4	5	6	7	8	
Before (x ₁)	210	230	182	205	262	253	219	216	
After (x ₂)	219	236	179	204	270	250	222	216	
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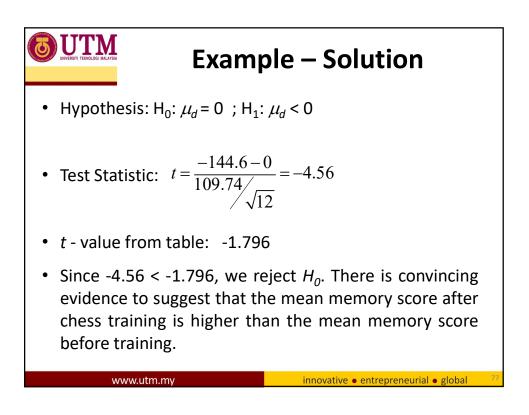


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Before(x_1)	After(x_2)	$D = x_1 - x_2$	$D^2 = (x_1 - x_2)^2$
210	219	-9	<mark>81</mark>
230	236	-6	36
182	179	3	9
205	204	1	1
262	270	-8	64
253	250	-3	9
219	222	3	9
216	216	0	0
-		$\sum D = -19$	$\sum D^2 = 209$
		$\overline{D} = \frac{\sum D}{n} = \frac{-1}{8}$	$\frac{19}{3} = -2.375$
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Can playir previously lessons an before star	played od played	d ches ed che	ss par ess da	ticipat ily for	ed in 9 mor	a pro nths.	gram Each s	in wh studen	nich th t took	a me	ok che mory t	est
Student	1	2	3	4	5	6	7	8	9	10	11	12
Pre-test	510	610	640	675	600	550	610	625	450	720	575	675
Post-test	850	790	850	775	700	775	700	850	690	775	540	680
Difference	-340	-180	-210	-100	-100	-225	-90	-225	-240	-55	35	-5
$H_0: \mu_d = 0$												
$H_1: \mu_d < 0$												
Where μ_d is chess train Conduct the	ing and	d stude	ents w	ho ha	ve cor	nplete	d che	ss trai	ning	with r	סר	
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Table below lists of 10 students sufficient eviden course is effect significance level.	too ice tive	ka toq	pre conc	epar lude	ratoi e th	ry o nat	our the	se. pre	ls tl bara	here tory
Student	A	В	C	D	Е	F	G	н	I	J
Student SAT score before course	A 700	B 840	C 830	D 860	E 840	F 690	G 830	H 1180	ا 930	J 1070
			-		-	•	-			-
SAT score before course	700	840	830	860	840	690	830	1180	930	1070