A commercial refrigeration with refrigerant-134a as the working fluid is used to keep the refrigerated space at -30°C by rejecting its waste heat to cooling water that enters the condenser at 18°C at a rate of 0.25kg/s and leaves at 26°C. The refrigerant enters the condenser at 1.2MPa and 65°C and leaves at 42°C. The inlet state of the compressor is 60kPa and -34°C and the compressor is estimated to gain a net heat of 450W from the surroundings. Determine,

- a. the quality of the refrigerant at the evaporator inlet
- b. the refrigeration load
- c. the COP of the refrigerator
- d. the theoretical maximum refrigeration load for the same power input to the compressor



a)

From table,

 $h_{1,60kPa,-34^{\circ}C} = 230.03 \text{ kJ/kg}$   $h_{2,1200kPa,65^{\circ}C} = 295.16 \text{ kJ/kg}$   $h_{3,f,1200kPa,42^{\circ}C} = 111.23 \text{ kJ/kg}$   $h_{3} = h_{3} = 111.23 \text{ kJ/kg}$   $P_{4} = 60 \text{ kPa}$   $h_{4} = h_{f,4} + x_{4}h_{fg,4}$   $x_{4} = \frac{111.23 - 3.841}{227.79} = 0.47$ 

b) Using saturated liquid enthalpy at given temperature for water

$$\begin{split} h_{water,1} &= h_{f,18^\circ C} = 75.47 \text{ kJ/kg} \\ h_{water,2} &= h_{f,26^\circ C} = 108.94 \text{ kJ/kg} \end{split}$$

Using energy balance:

$$\begin{split} \dot{m}_{R134}(h_2 - h_3) &= \dot{m}_{water}(h_{water,2} - h_{water,1}) \\ \dot{m}_{R}(295.16 - 111.23) &= 0.25(108.94 - 75.47) \\ \dot{m}_{R} &= 0.0455 \text{kg} / \text{s} \end{split}$$

The waste heat transferred from the refrigerant are;

$$\begin{split} \dot{Q}_{\rm H} &= \dot{m}_{\rm R134} (h_2 - h_3) = 0.0455 (295.16 - 111.23) = 8.367 \rm{kW} \\ \dot{W}_{\rm in} &= \dot{m}_{\rm R} (h_2 - h_1) - \dot{Q}_{\rm in} = 0.0455 (295.16 - 230.03) - 0.45 \rm{kW} = 2.513 \rm{kW} \\ \dot{Q}_{\rm L} &= \dot{Q}_{\rm H} - \dot{W}_{\rm in} = 8.367 - 2.513 = 5.85 \rm{kW} \end{split}$$

c)

$$COP = \frac{\dot{Q}_{L}}{\dot{W}_{in}} = \frac{5.85}{2.513} = 2.33$$

d)

$$COP_{max} = \frac{1}{\frac{T_{H}}{T_{H}} - 1} = \frac{1}{\frac{18 + 273}{-30 + 273} - 1} = 5.063$$

$$\dot{Q}_{L,max} = COP_{max}\dot{W}_{in} = 5.063 \times 2.513 = 12.72kW$$