

**SEEU2012  
Electronics  
20212022/2**

# **Chapter 4 Bipolar Junction Transistor (BJT) AC Analysis**

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# Course Learning Outcomes

1

Apply the basic law and theorems of electronic devices to describe their basic operation.

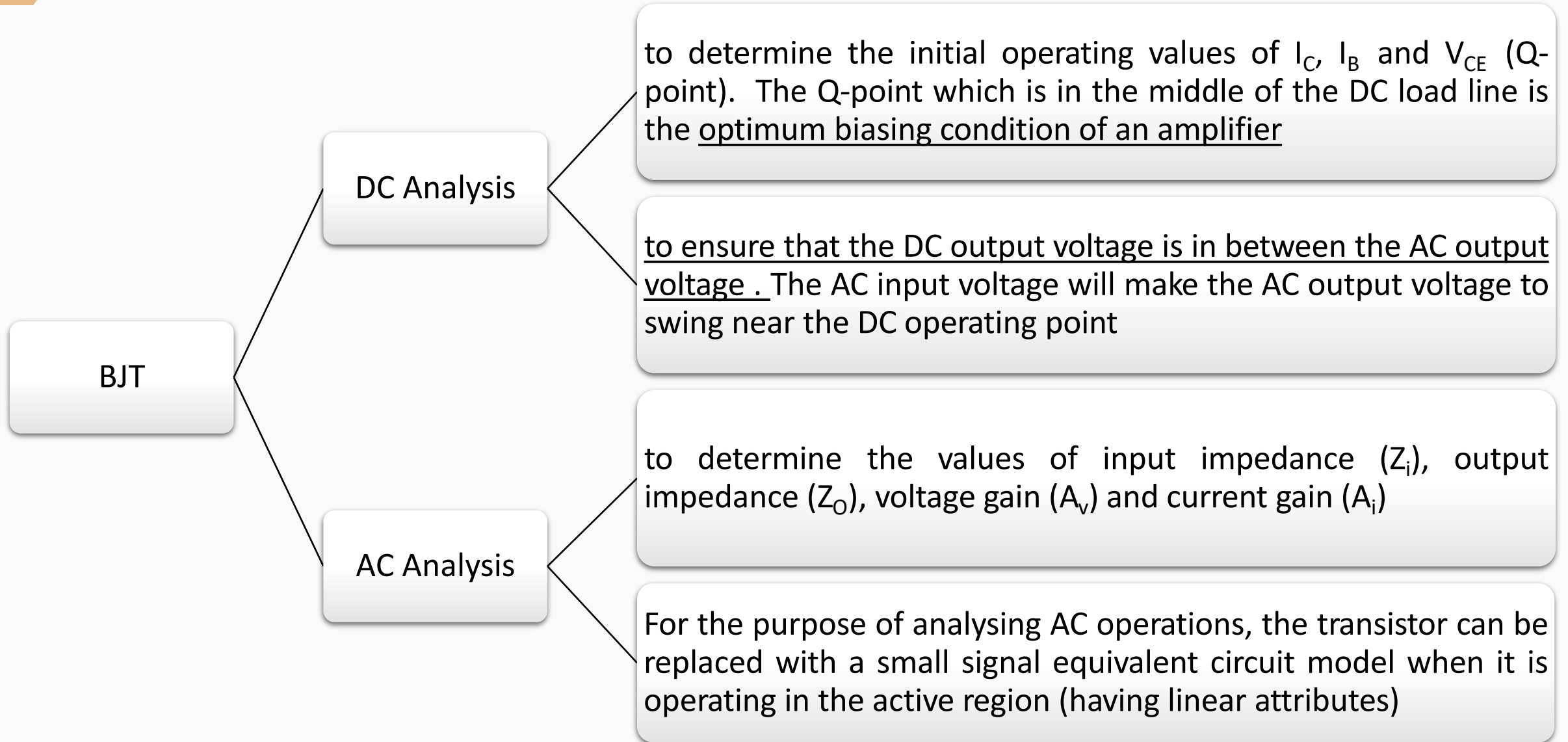
2

Apply the basic law, theorems and methods of analysis to solve complex problem related to circuitry.

3

Work in a team and communicate effectively.

# Small Signal Circuit Analysis

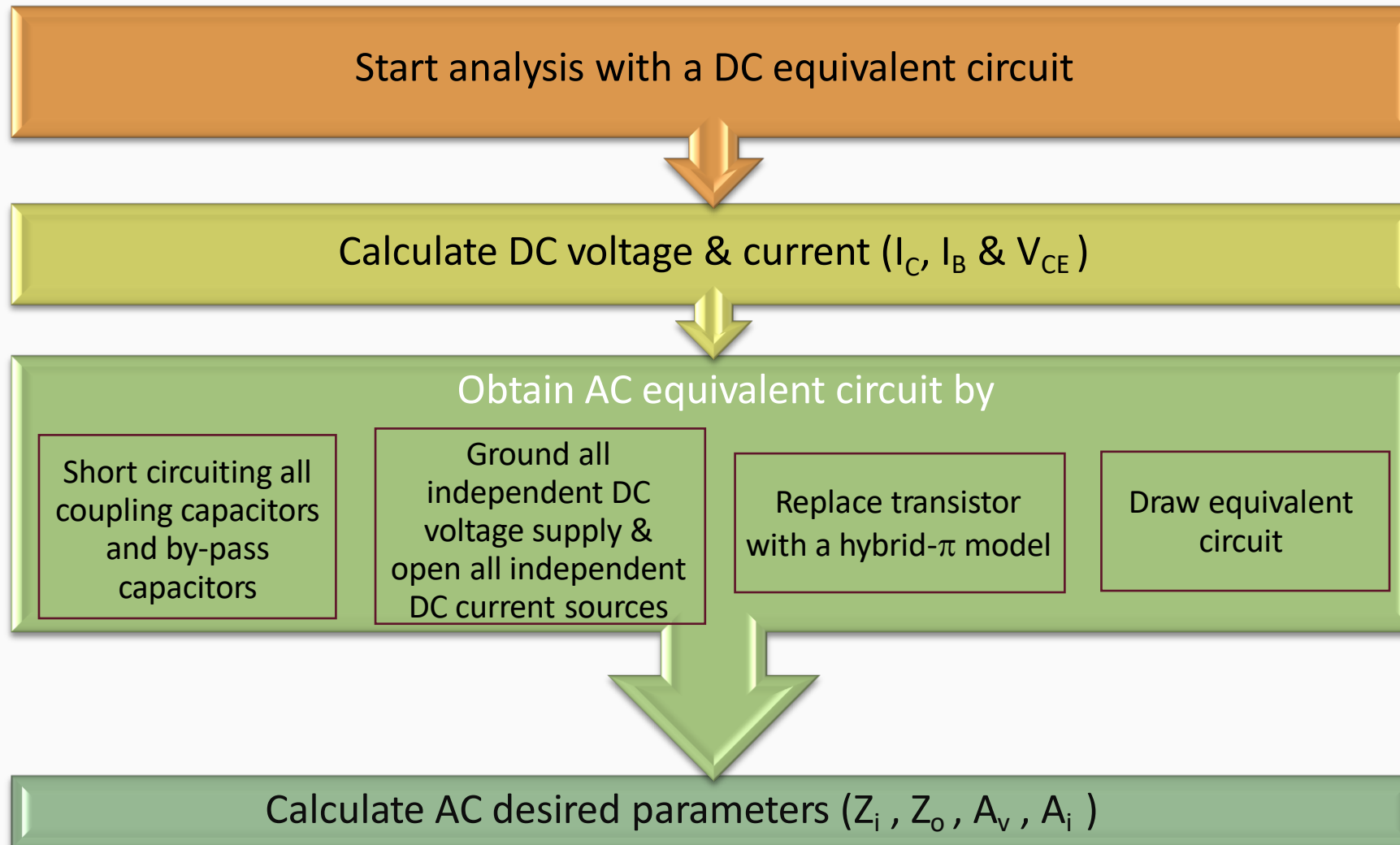


All DC supply is removed – replaced  
with zero potential (ground)

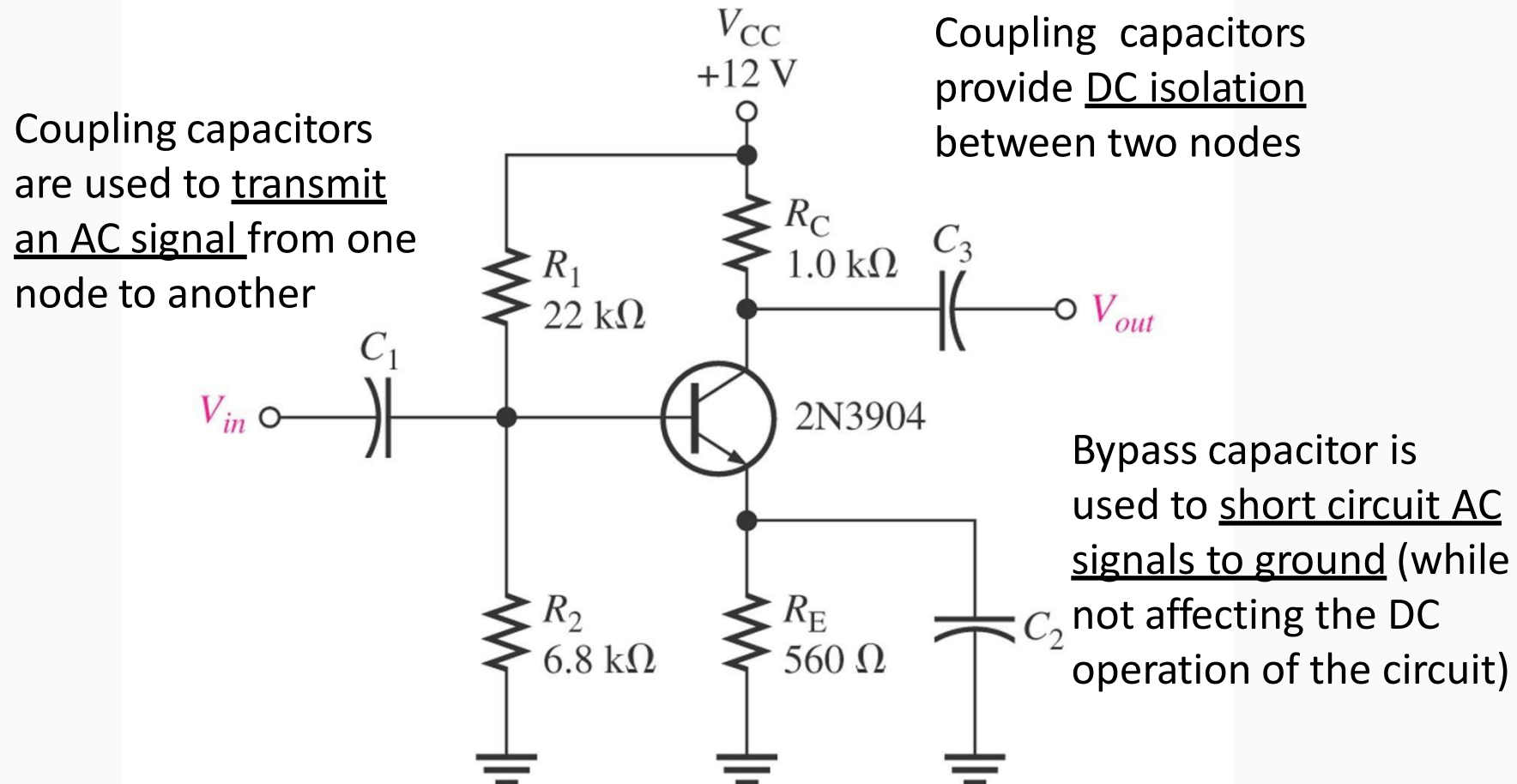
Reactance becomes low & capacitors  
can be considered short circuit

Determine the following quantities

- Input impedance,  $Z_i$
- Output impedance,  $Z_o$
- Voltage gain,  $A_v$
- Current gain,  $A_i$
- Power gain,  $A_p$

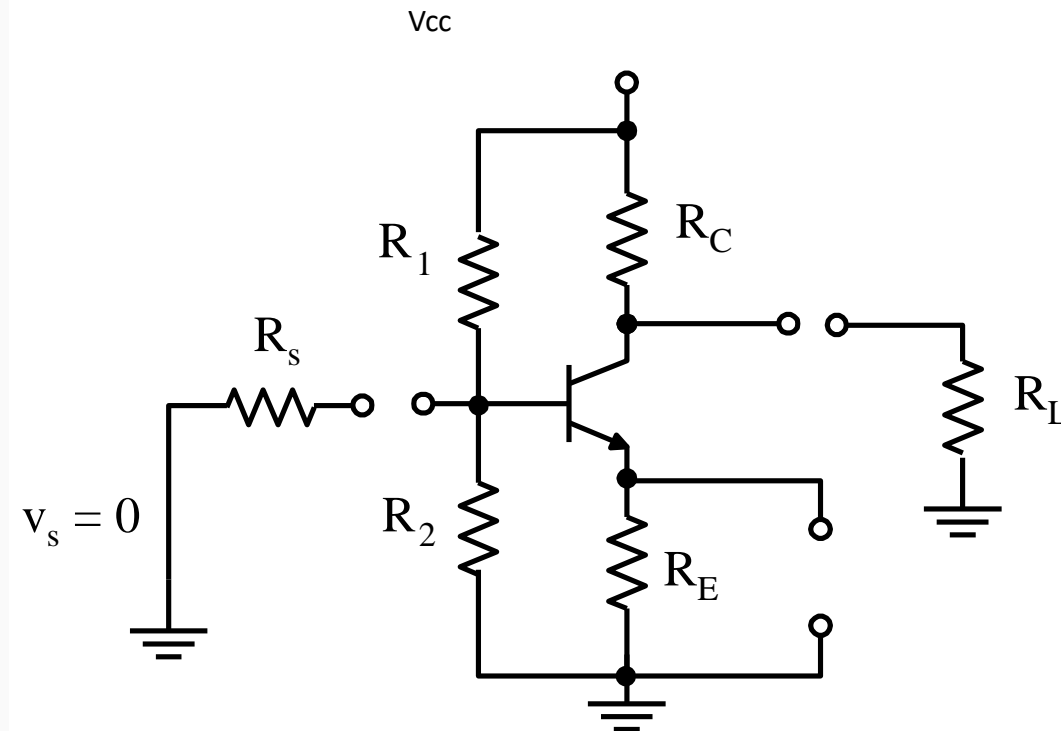


# Function Of Capacitors In Amplifiers



# DC Analysis

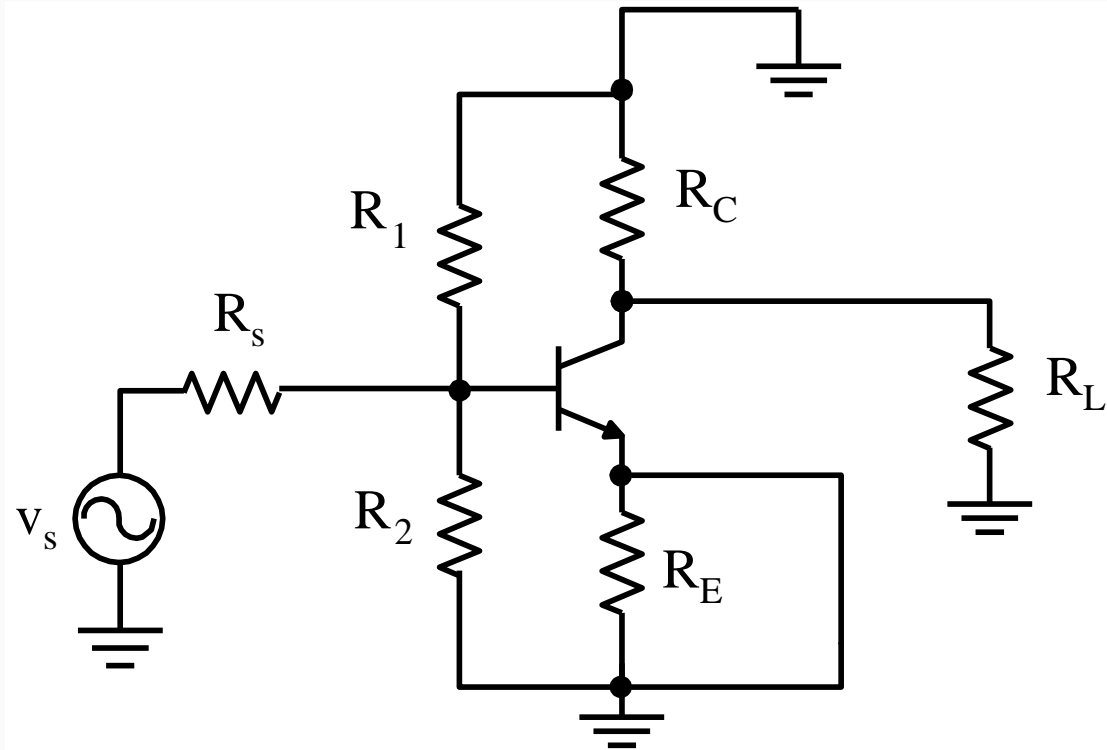
- ☐ Set AC source to zero.
- ☐ Replace the coupling capacitors and bypass capacitor with open circuits.



**DC Equivalent Circuit**

# AC Analysis

- ❑ Set DC source to zero (ground)
- ❑ Replace the coupling capacitors and bypass capacitors with short circuit
- ❑ Analyze the AC operation



**AC Equivalent Circuit**



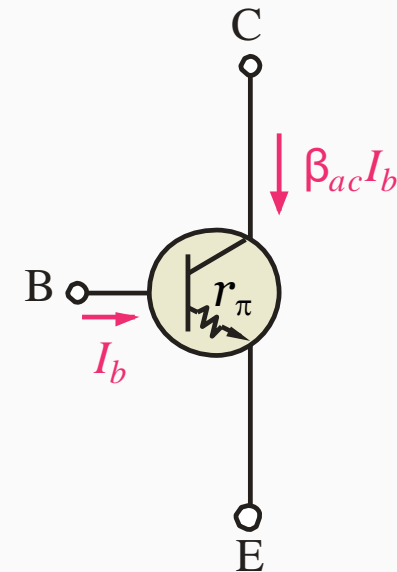
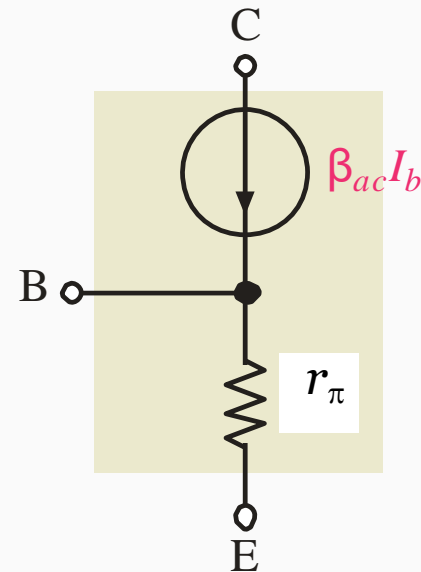
# AC Equivalent Models

- ❑ Linear transistor can be replaced by AC equivalent model.
- ❑ Transistor AC equivalent models are:
  - ❑ Parameter-h Model
  - ❑  $r_e$  Model
  - ❑ Parameter-y Model
  - ❑ Hybrid- $\pi$  Model

# Transistor AC Models

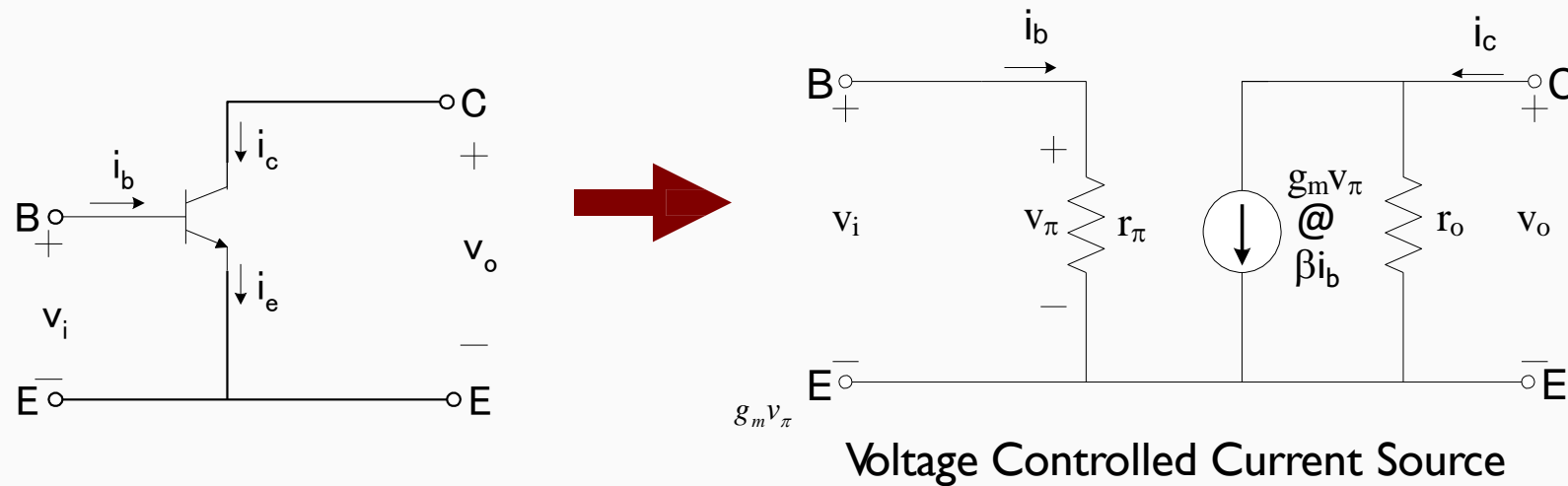
The simplified Hybrid- $\pi$  are shown in relation to the transistor model

An important Hybrid- $\pi$  is  $r_{\pi}$ .  
 It appears as a small AC resistance between the Base and Emitter



# Hybrid - $\pi$ Model

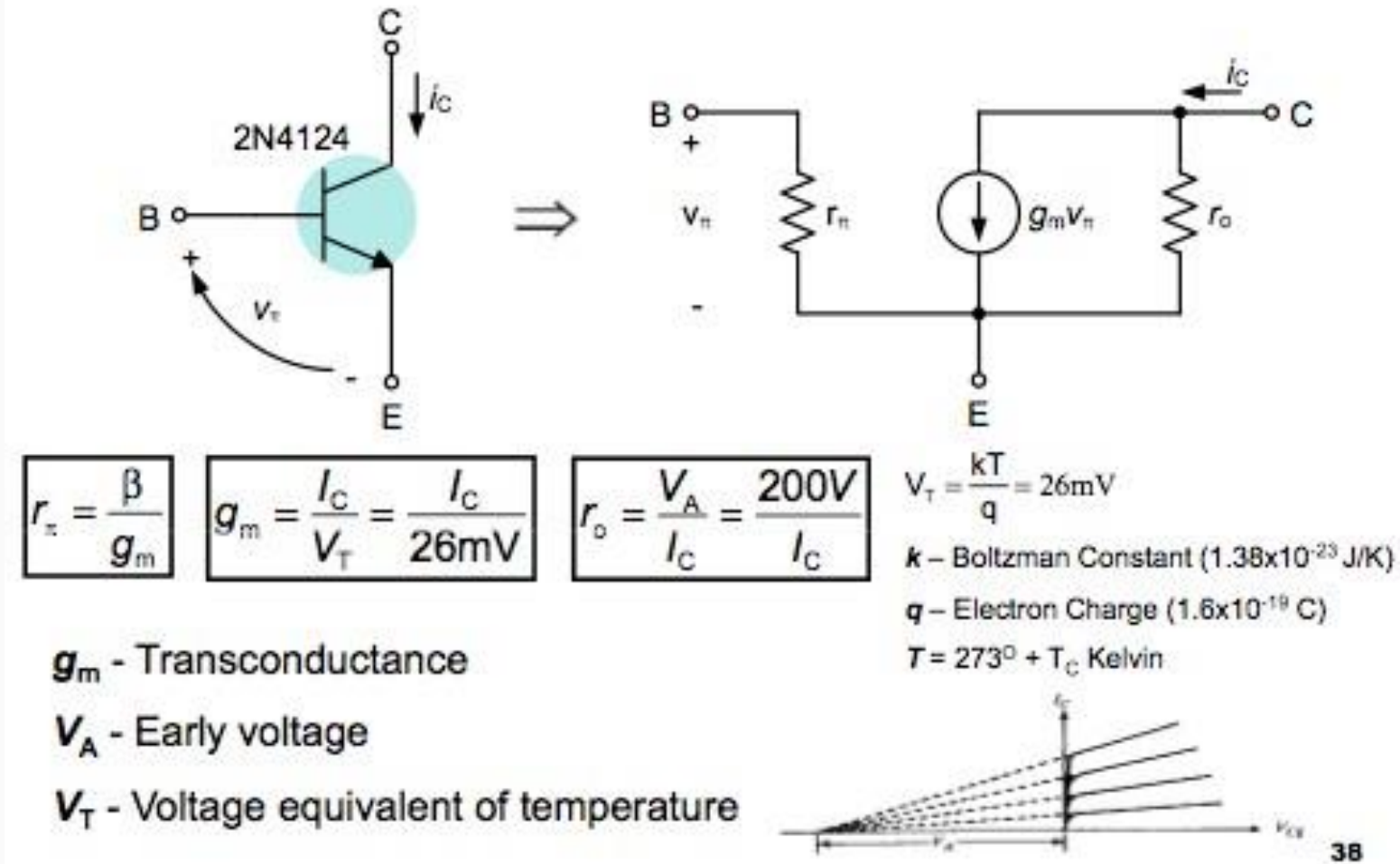
10



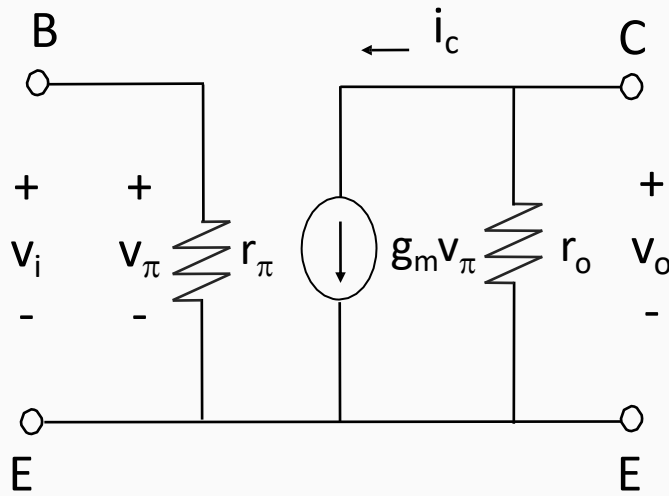
$$\beta = h_{fe} \quad r_o = \frac{1}{h_{oe}} = \frac{V_A}{I_C} \quad g_m = \frac{I_C}{V_T} \quad r_\pi = \frac{\beta}{g_m}$$

- ❑ In the Current Controlled Current Source (CCCS) model =  $\beta i_b$
- ❑ In the Voltage Controlled Current Source (VCCS) model =  $g_m v_\pi$
- ❑ Internal output impedance,  $r_o$  is very high & can be neglected (open circuit)
- ❑ Equivalent voltage temperature,  $V_T = 26\text{mV}$  at room temperature ( $25^\circ\text{C}$ )
- ❑ Early Voltage,  $V_A \cong 200\text{V}$

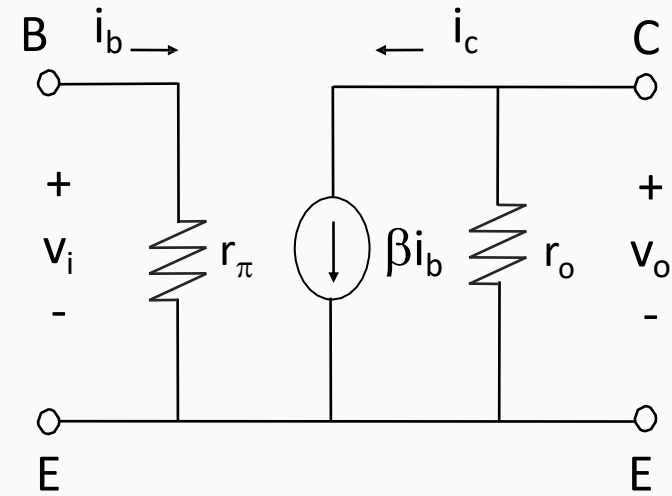
# Hybrid - $\pi$ Model



# Hybrid - $\pi$ Model



VCCS Model



CCCS Model

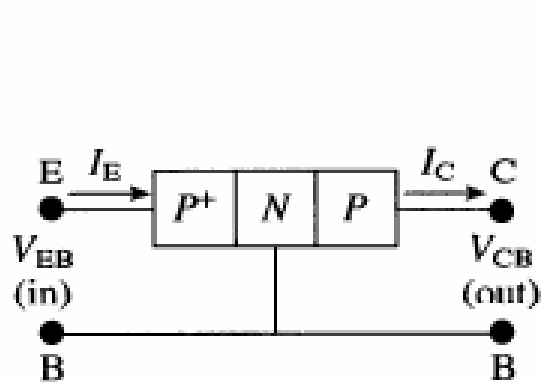
**EQUATION TO REMEMBER!**

$$\beta = h_{fe} \quad r_o = \frac{1}{h_{oe}} = \frac{V_A}{I_C} \quad g_m = \frac{I_C}{V_T} \quad r_\pi = \frac{\beta}{g_m}$$

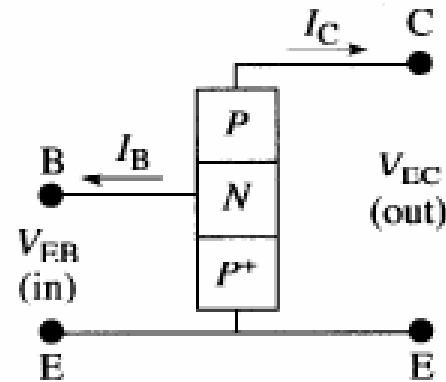


# Transistor Configuration

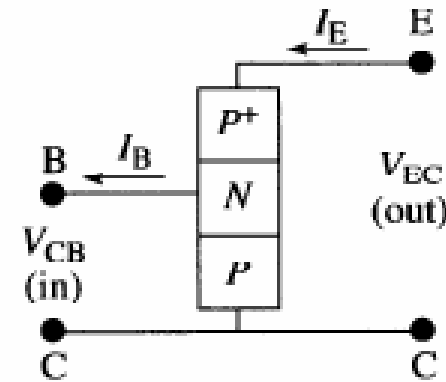
- ❑ Transistor configuration – is a connection of transistor to get **variety operation**.
- ❑ 3 types of transistor configuration:
  - Common Collector (CC).
  - Common Base (CB).
  - Common Emitter (CE).
- ❑ Common means the circuit has a single reference for both the input voltage to the transistor and the output voltage



(a) Common base



(b) Common emitter



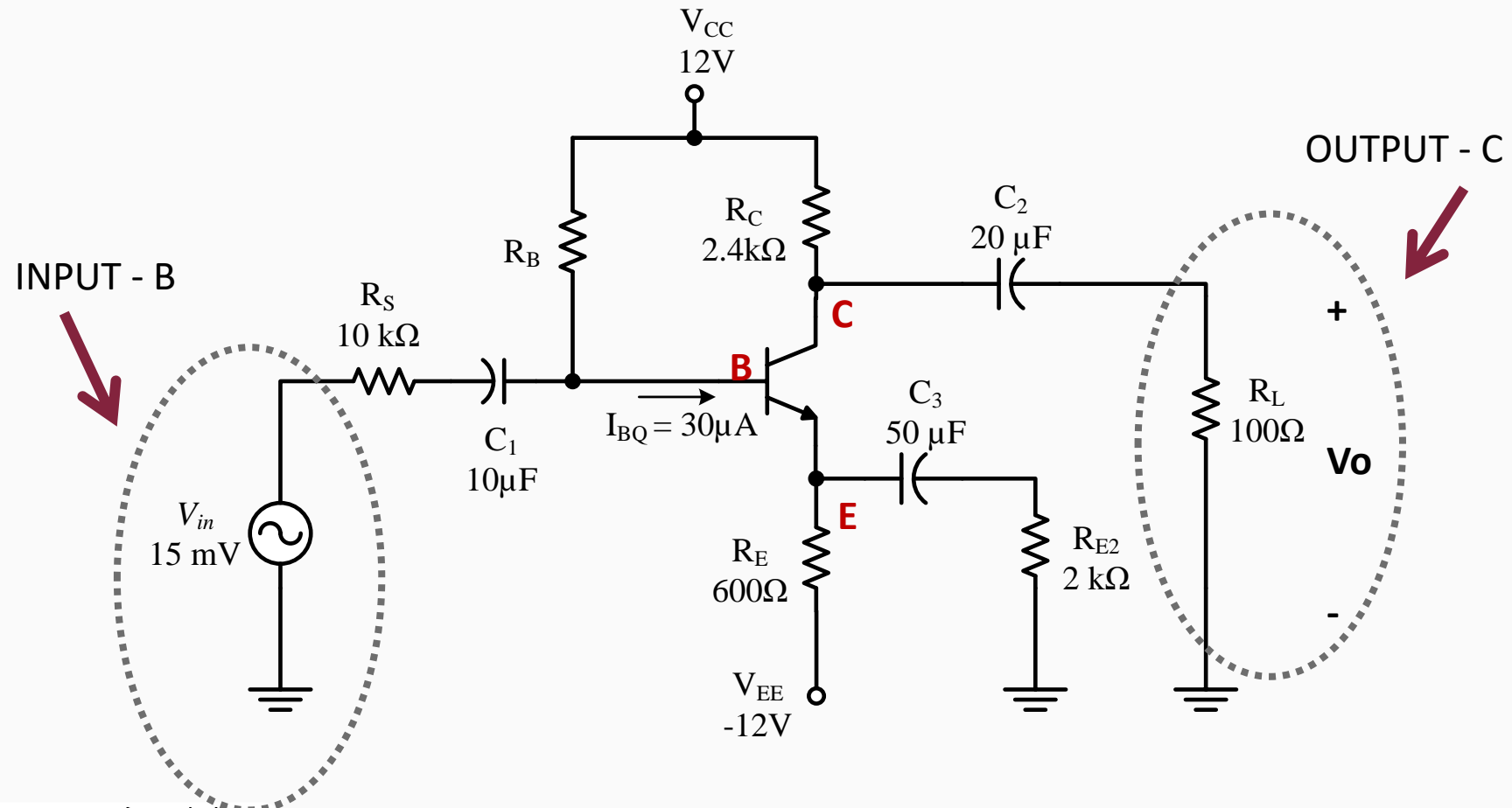
(c) Common collector

# Transistor Configuration

|                 | Common Emitter | Common Collector | Common Base |
|-----------------|----------------|------------------|-------------|
| Input terminal  | Base           | Base             | Emitter     |
| Output Terminal | Collector      | Emitter          | Collector   |
| Common (Gnd)    | Emitter        | Collector        | Base        |

# Example

Determine the configuration of the following BJT circuit?

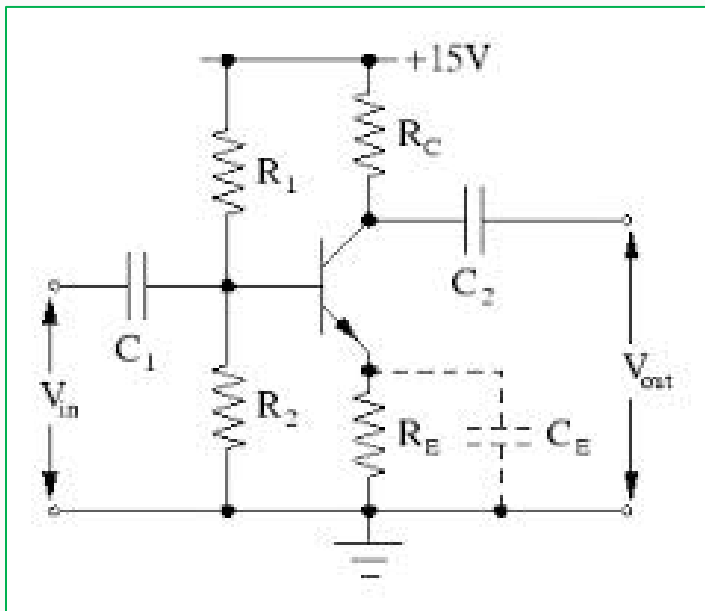




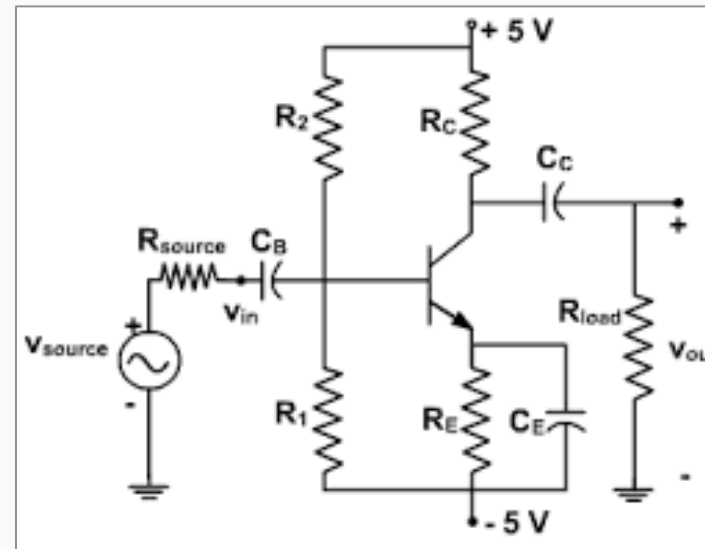
# Exercise

Determine the configuration of the following BJT circuit?

A



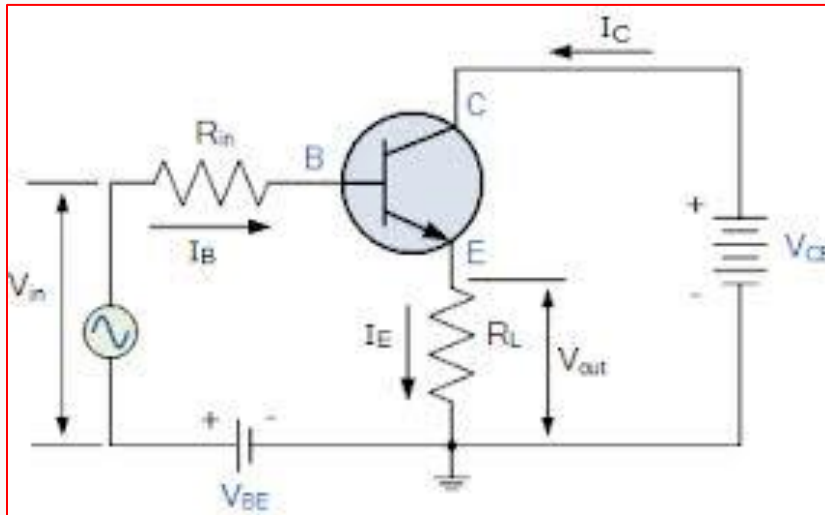
B



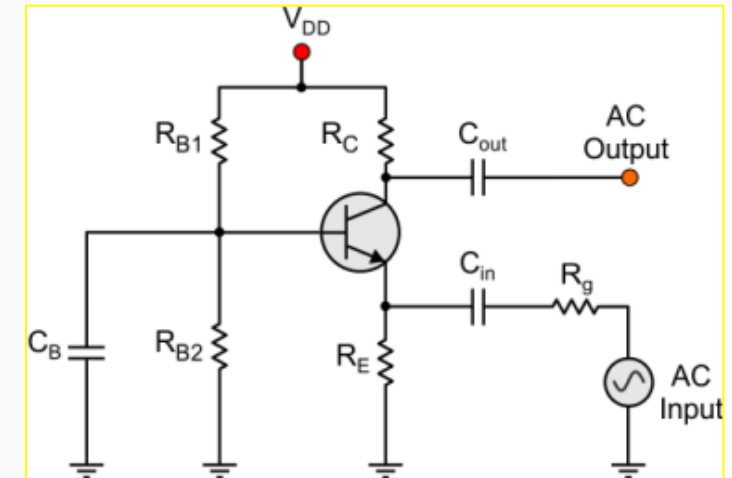
# Exercise

Determine the configuration of the following BJT circuit?

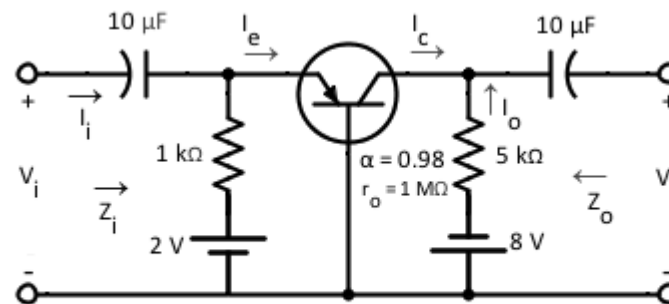
C



D

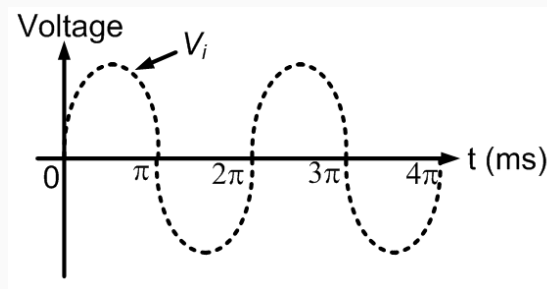
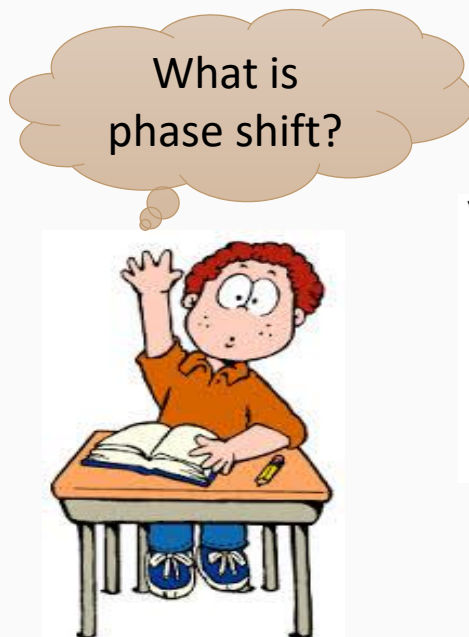


E

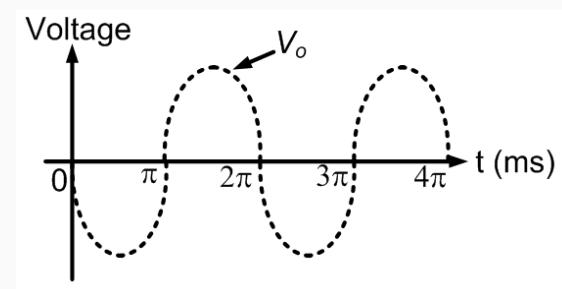


# Common Emitter

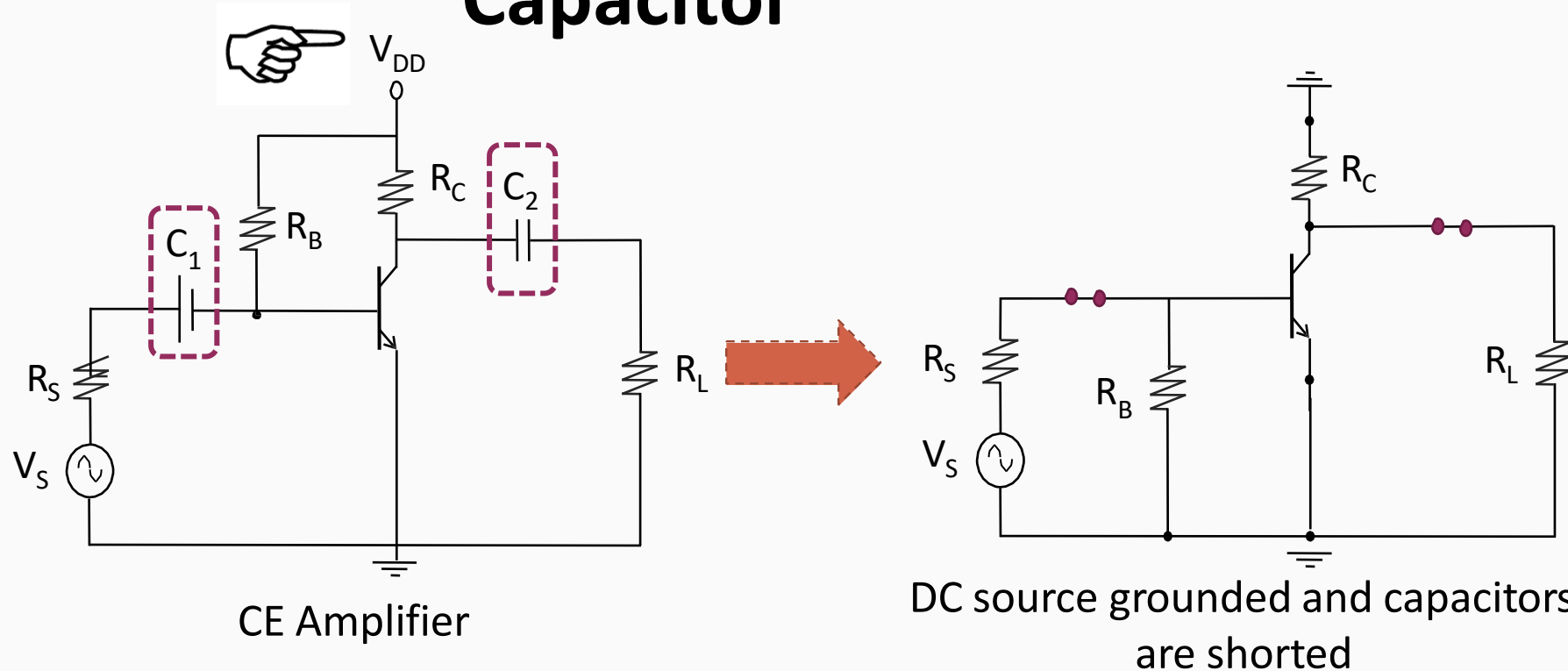
- ❑ Input – Applied to BASE
- ❑ Output – From COLLECTOR
- ❑ High Voltage Gain,  $A_v$  and high Current Gain,  $A_i$
- ❑ Phase shift between input and output is  $180^\circ$



Phase shift

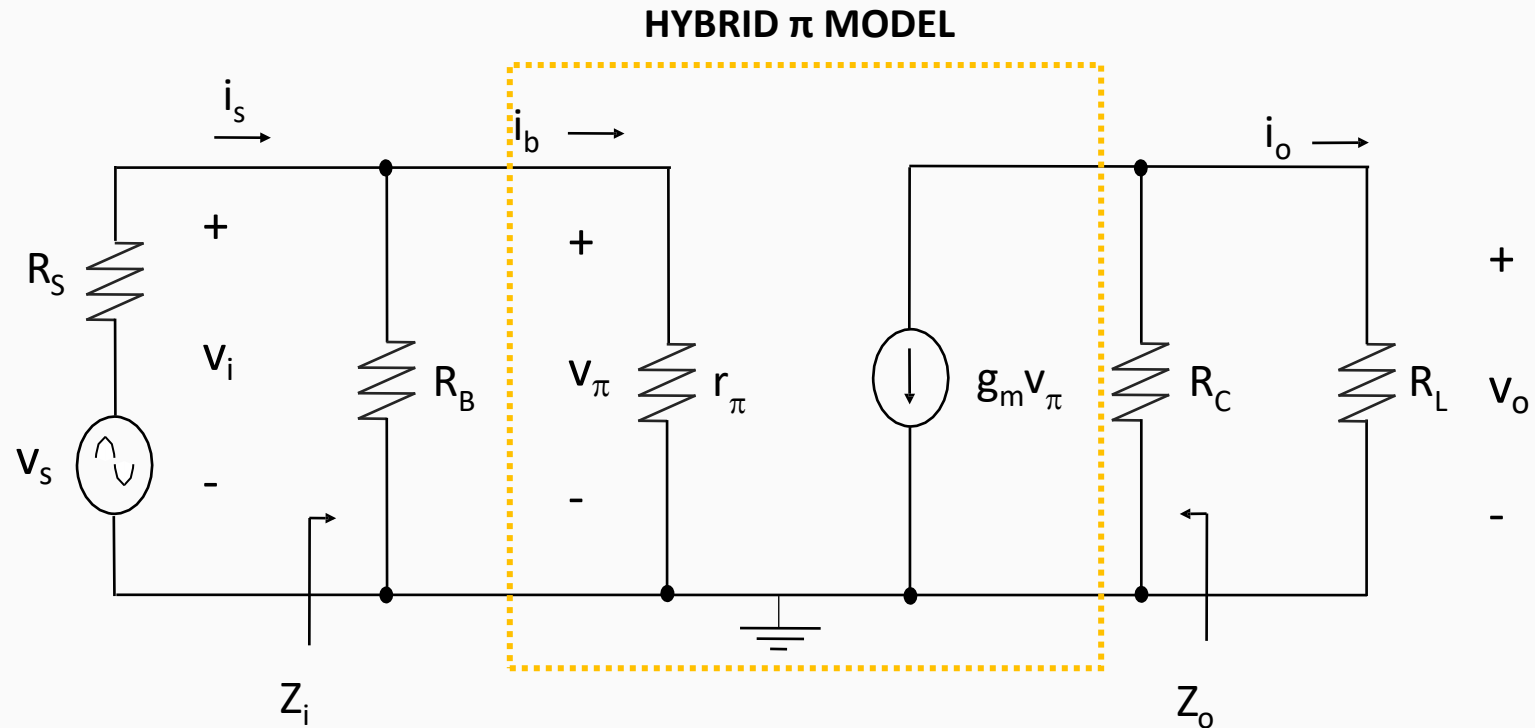


# Common Emitter: Fixed Bias Without By Pass Capacitor



- ❑ Set all DC source to zero/ground
- ❑ Replace the coupling capacitors and bypass capacitors with short circuit
- ❑ Rearrange circuit to make it simple and draw the AC equivalent circuit.

# Common Emitter: Fixed Bias



Input impedance:

$$Z_i = R_B \parallel r_\pi$$

Output impedance:

$$Z_o = R_C$$

# Common Emitter : Fixed Bias

**Voltage gain:**

$$A_{vs} = \frac{v_o}{v_s}$$

$$v_o = -g_m v_\pi (R_C \parallel R_L)$$

$$v_\pi = v_i = \frac{Z_i}{Z_i + R_S} v_s$$

$$A = \frac{v_o}{v_\pi} \times \frac{v_\pi}{v_i} \times \frac{v_i}{v_s}$$

$$A_{vs} = -g_m (R_C \parallel R_L) \frac{Z_i}{Z_i + R_S}$$

**Current gain:**

$$A_i = \frac{i_o}{i_i}$$

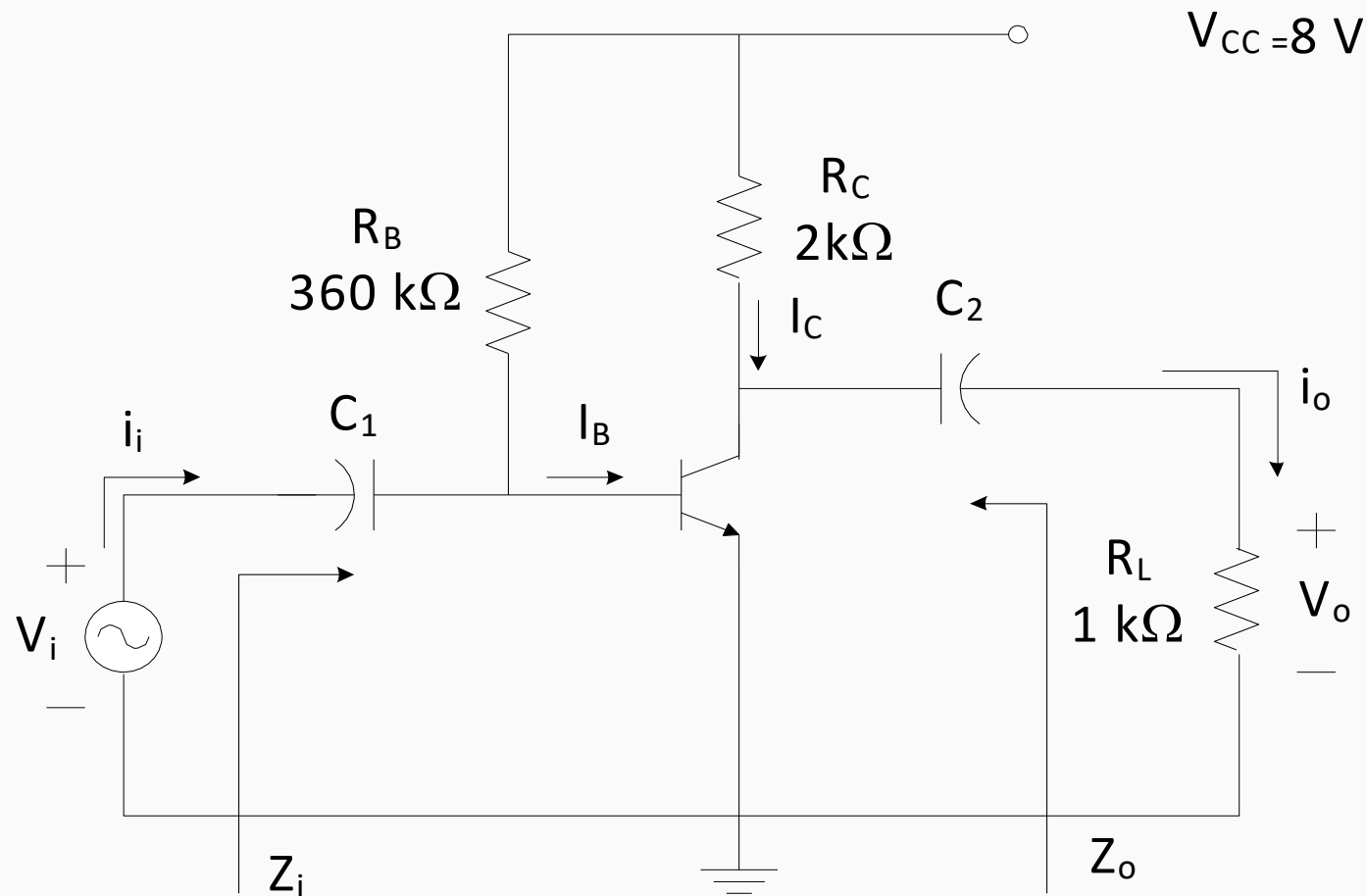
$$i_o = \frac{R_C}{R_C + R_L} (-g_m v_\pi)$$

$$v_\pi = v_i = i_i Z_i$$

$$A_i = \frac{i_o}{v_\pi} \times \frac{v_\pi}{v_i} \times \frac{v_i}{i_i}$$

$$A_i = - \frac{R_C}{R_C + R_L} g_m Z_i$$

# Common Emitter : Fixed Bias (Exercise)



$$V_{BE} = 0.7 \text{ V}$$

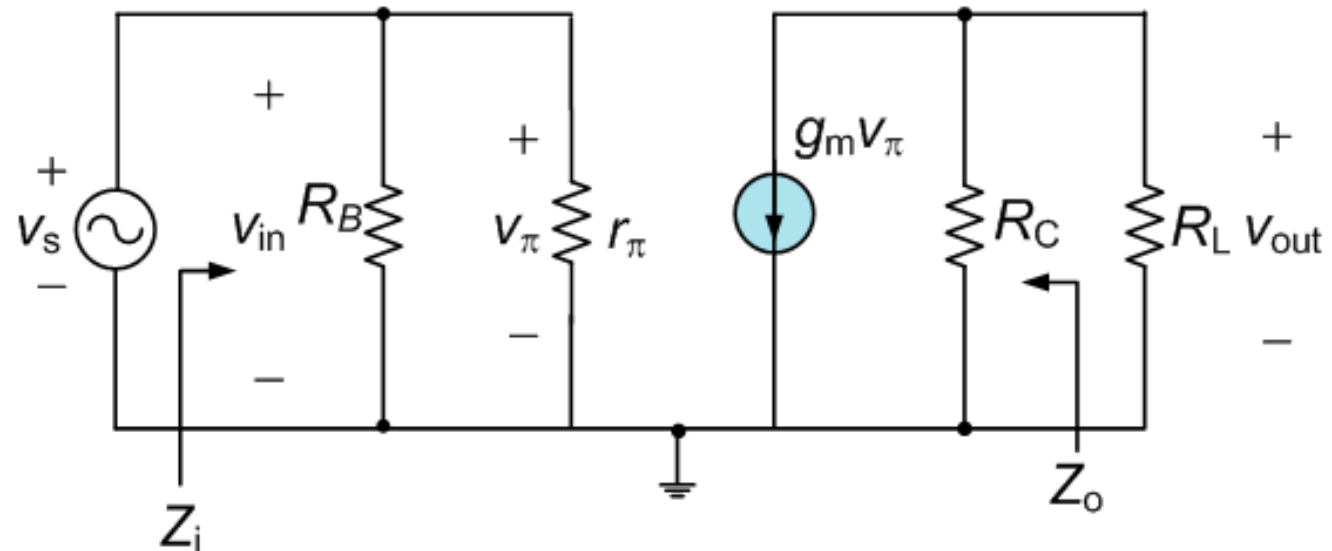
$$\beta_{DC} = \beta_{AC} = 100$$

$$V_T = 26 \text{ mV}$$

Draw the AC equivalent circuit and find  $A_v$  and  $A_i$ .

# Common Emitter : Fixed Bias (Solution)

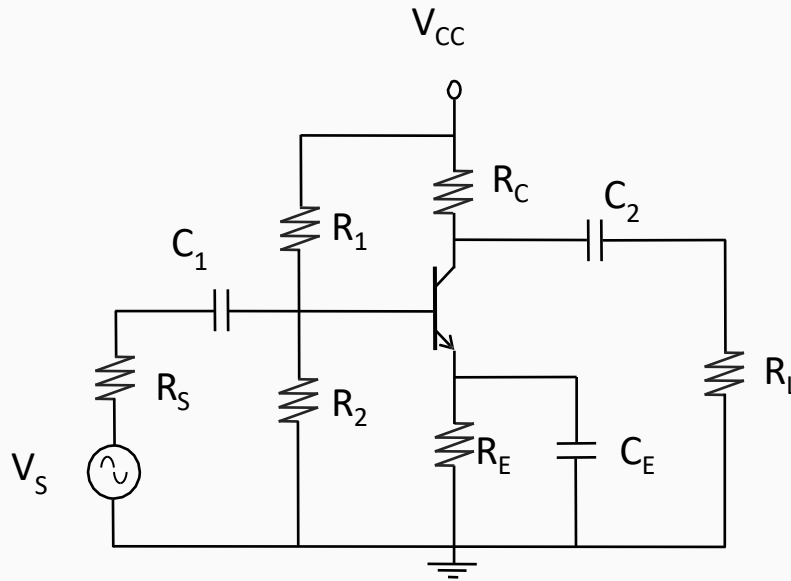
- 1) Draw the DC equivalent circuit – ground all DC supply and short all capacitors.
- 2) Draw the AC equivalent circuit



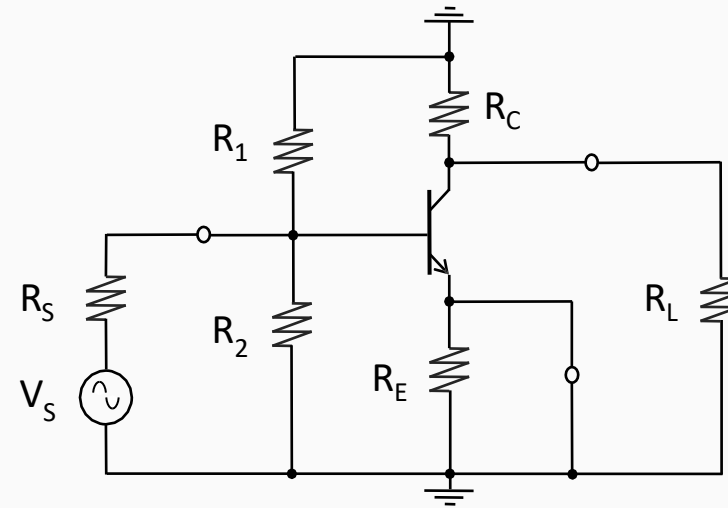


# Common Emitter: Voltage Divider Bias

## □ Voltage Divider Bias

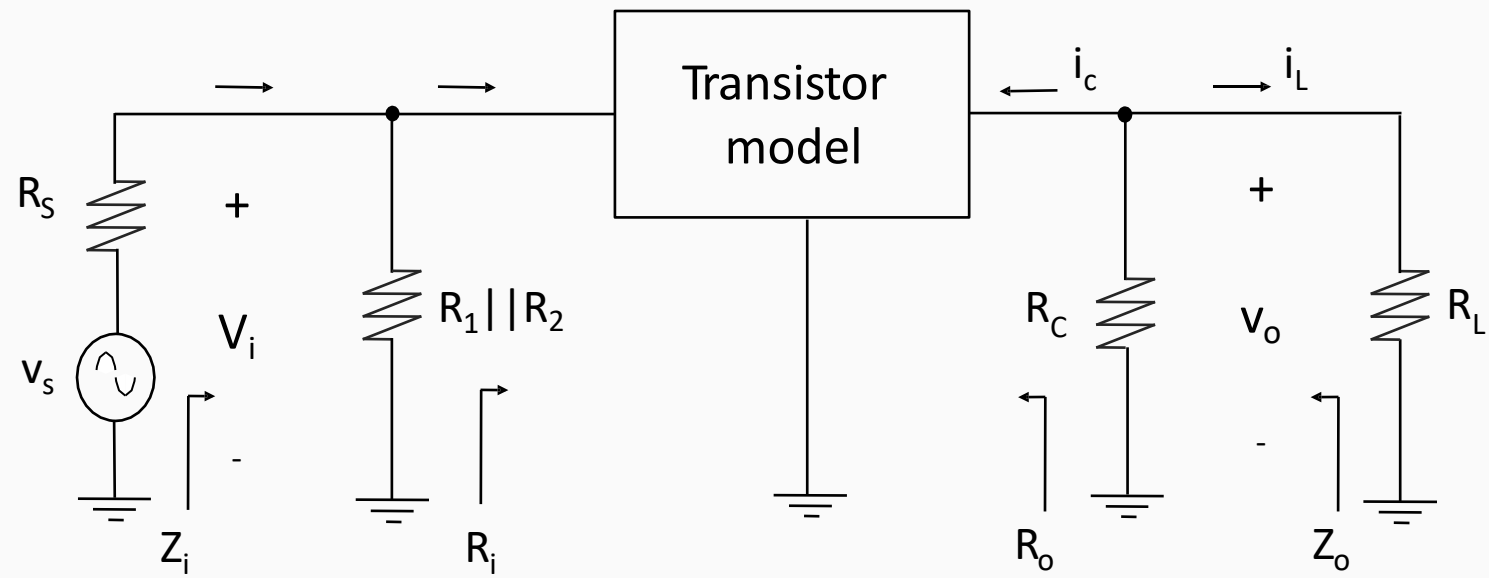


CE Amplifier



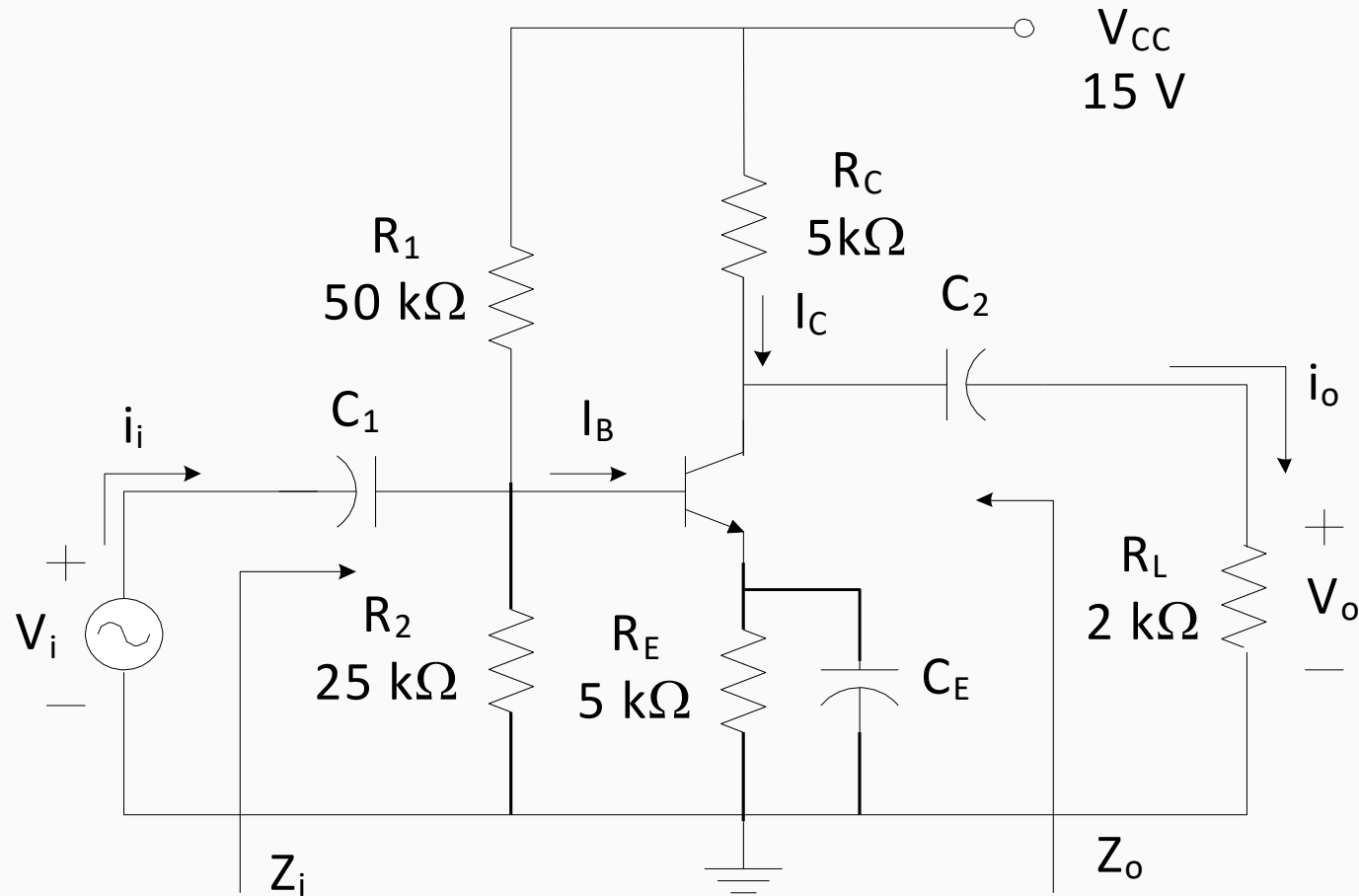
DC source grounded and capacitors are shorted

# Common Emitter: Voltage Divider Bias



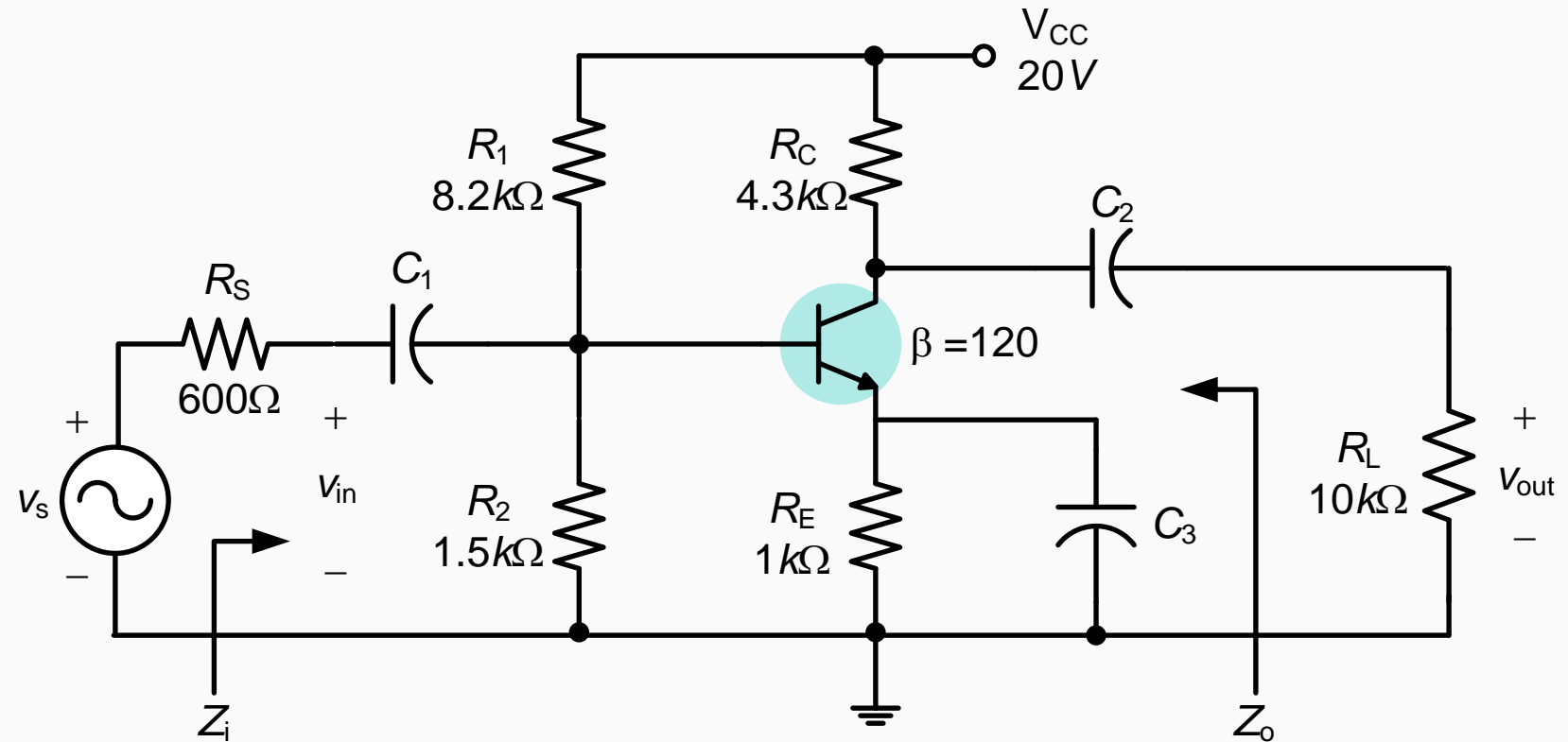
# Exercise

Draw the AC equivalent circuit for the following voltage divider bias circuit:

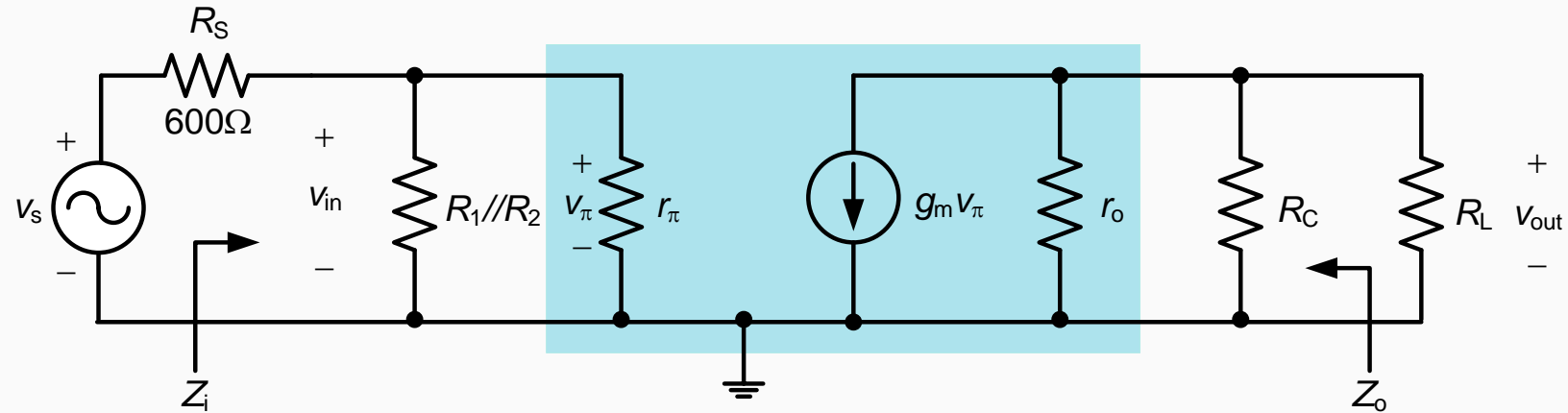


# Common Emitter: Voltage Divider Bias Example

Determine the values of  $Z_i$ ,  $Z_o$ ,  $A_{v(oc)}$ ,  $A_v$ ,  $A_{vs}$ ,  $A_i$  and  $A_{is}$  for the amplifier circuit below.  
 Given  $V_A = 200V$  and  $I_C = 2.37mA$



# Solution



**Input impedance:**  $Z_i = R_1 \parallel R_2 \parallel r_\pi = 8.2k\Omega \parallel 1.5k\Omega \parallel 1.32k\Omega = 647\Omega$

**Output impedance:**  $Z_o = r_o \parallel R_C = 84.4k\Omega \parallel 4.3k\Omega = 4.09k\Omega$

**Voltage gain:**  $A_{v(oc)} = \frac{V_{out}}{V_{in}} = -g_m (r_o \parallel R_C) = -(91.2mS)(4.09k\Omega) = -373$

$$A_v = \frac{V_{out}}{V_{in}} = A_{v(oc)} \left( \frac{R_L}{Z_o + R_L} \right) = (-373) \left( \frac{10k\Omega}{4.09k\Omega + 10k\Omega} \right) = -265$$



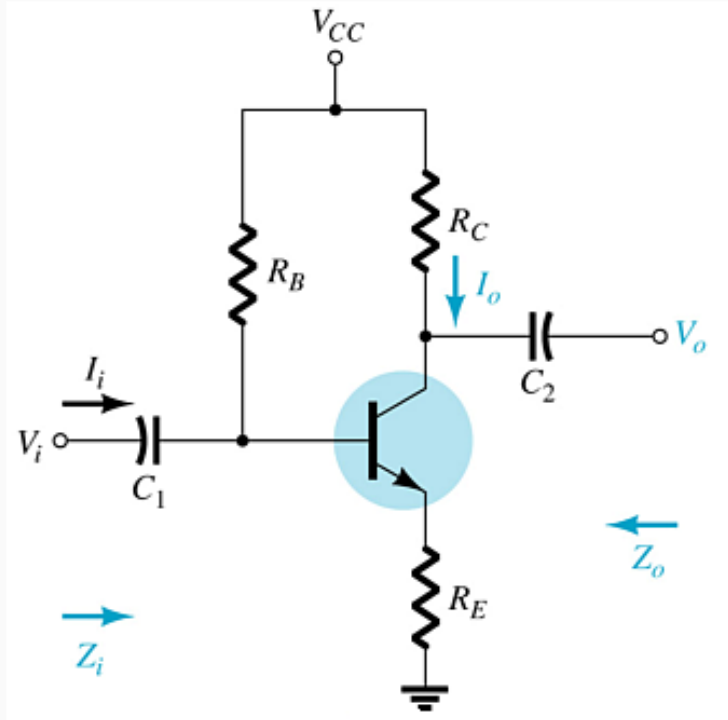
$$A_{vs} = \frac{V_{out}}{V_s} = A_v \left( \frac{Z_i}{R_s + Z_i} \right) = (-265) \left( \frac{647 \Omega}{600 \Omega + 647 \Omega} \right) = -137.5$$

**Current gain:**

$$A_i = \frac{i_{out}}{i_{in}} = A_{v(oc)} \left( \frac{Z_i}{Z_o + R_L} \right) = (-373) \left( \frac{647 \Omega}{4.09 k\Omega + 10 k\Omega} \right) = -17.13$$

$$A_{is} = \frac{i_{out}}{i_s} = A_i \left( \frac{R_s}{R_s + Z_i} \right) = (-17.13) \left( \frac{600 \Omega}{600 \Omega + 647 \Omega} \right) = -8.24$$

# Common Emitter: Unbypassed $R_E$



The removal of the bypass capacitor results in:

- ❑ an increase in the input impedance,  $Z_i$  & output impedance,  $Z_o$
- ❑ a reduction in its voltage gain,  $A_v$

# Common Emitter: Unbypassed $R_E$

**Input impedance:**

$$Z_i = R_B \parallel Z_b$$

$$Z_b = r_\pi + (\beta + 1)R_E$$

**Output impedance (ignore  $r_o$ ):**

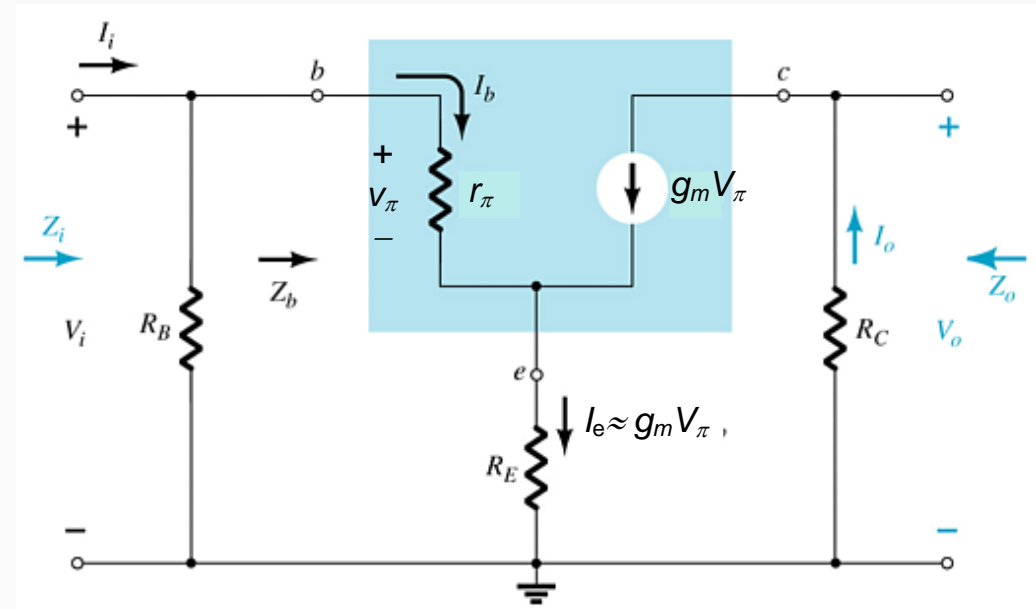
$$Z_o = R_C$$

**Voltage gain:**

$$A_{v(oc)} = \frac{v_o}{v_i} = - \frac{g_m v_\pi R_C}{i_b Z_b} \bigg|_{Z_b = r_\pi + (\beta + 1)R_E}$$

$$= - \frac{g_m i_b r_\pi R_C}{i_b (r_\pi + g_m r_\pi R_E)} = - \frac{g_m R_C}{1 + g_m R_E}$$

$$A_{v(oc)} = \frac{v_o}{v_i} \cong - \frac{R_C}{R_E} \bigg|_{g_m R_E \gg 1}$$



**Current gain:**

$$A_i = \frac{i_o}{i_i} = - \frac{g_m r_\pi R_B}{R_B + Z_b} = - \frac{\beta R_B}{R_B + Z_b}$$

**Current gain from voltage gain:**

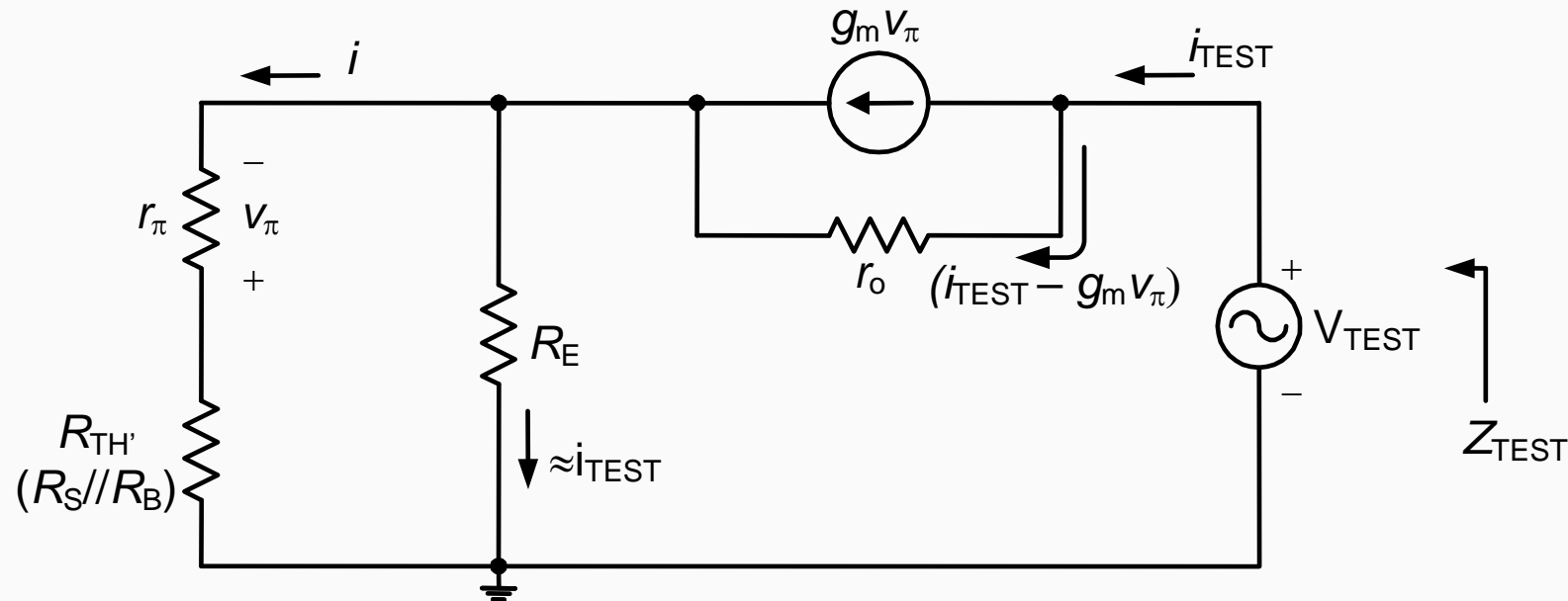
$$A_i = A_{v(oc)} \left( \frac{Z_i}{Z_o + R_L} \right) = A_{v(oc)} \left( \frac{Z_i}{R_C} \right)$$





# Common Emitter: Unbypassed $R_E$

To determine  $Z_o$  using imaginary voltage source (alternative approach)



$$Z_{TEST} = \frac{V_{TEST}}{i_{TEST}}$$

$$\begin{aligned} V_{TEST} &\approx (i_{TEST} - g_m v_\pi) r_o + i_{TEST} R_E \\ &\approx i_{TEST} r_o - g_m v_\pi r_o + i_{TEST} R_E \end{aligned}$$

# Common Emitter: Unbypassed $R_E$

$$i = \frac{R_E}{R_E + (r_\pi + R_{TH'})} \times i_{TEST}$$

$$v_\pi = -ir_\pi = \frac{-R_E r_\pi}{R_E + r_\pi + R_{TH'}} \times i_{TEST}$$

$$v_{TEST} = i_{TEST} r_O - g_m r_O \left[ \frac{-R_E r_\pi}{R_E + r_\pi + R_{TH'}} \right] \times i_{TEST} + i_{TEST} R_E$$

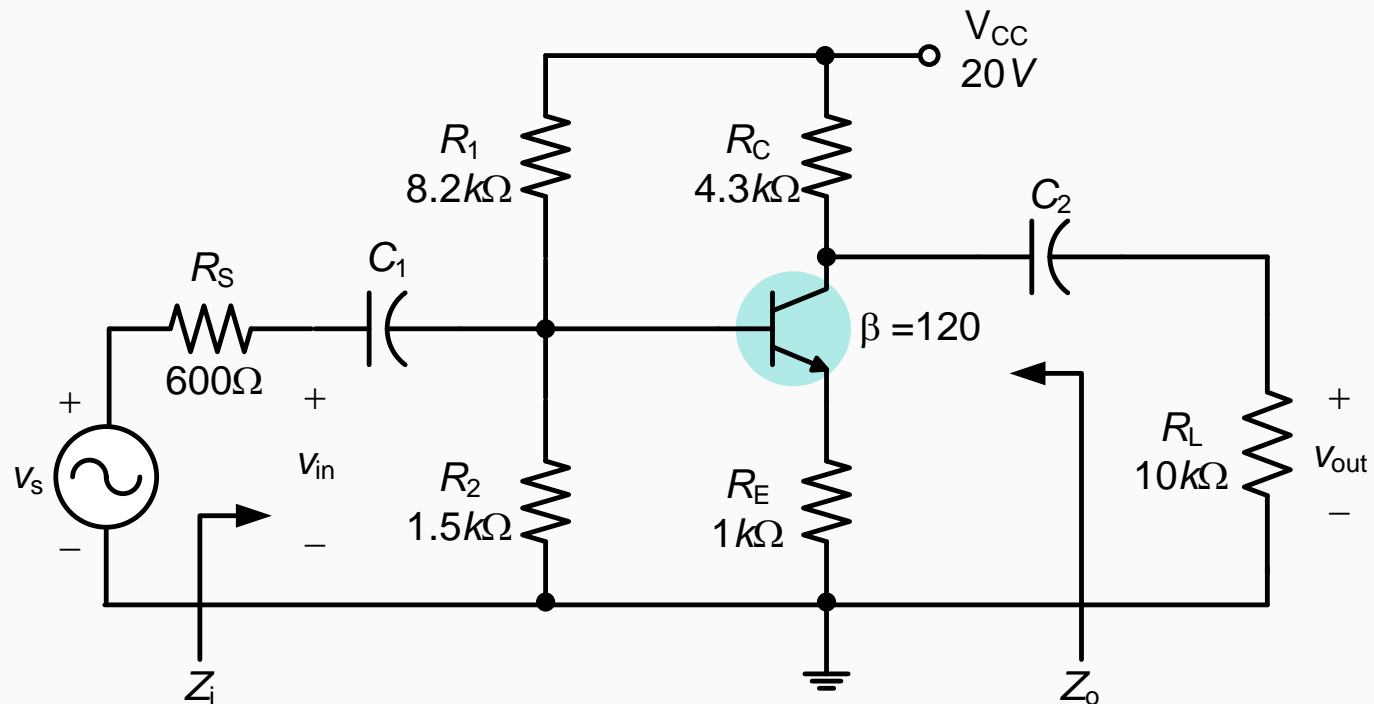
$$= i_{TEST} \left[ r_O + \frac{g_m r_O R_E r_\pi}{R_E + r_\pi + R_{TH'}} + R_E \right]$$

$$\therefore Z_{TEST} = \frac{v_{TEST}}{i_{TEST}} = r_O + \frac{g_m r_O R_E r_\pi}{R_E + r_\pi + R_{TH'}} + R_E$$

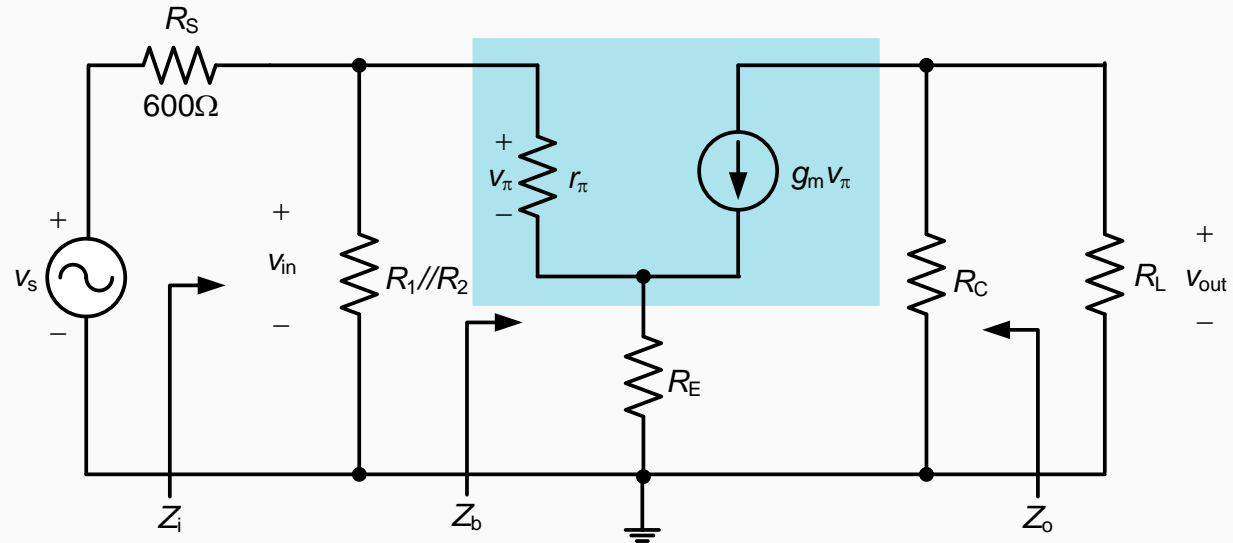
$$\therefore Z_O = (Z_{TEST} \parallel R_C) \approx R_C$$

# Example of Common Emitter: Unbypassed $R_E$

Determine the values of  $Z_i$ ,  $Z_o$ ,  $A_{v(oc)}$ ,  $A_v$ ,  $A_{vs}$ ,  $A_i$ ,  $A_{is}$  and  $A_p$  for the amplifier circuit shown below. Given  $V_A = \infty$  and  $I_C = 2.37\text{mA}$



# Example of Common Emitter: Unbypassed $R_E$



**Input impedance:**

$$Z_b = r_\pi + (\beta + 1)R_E = 1.32k\Omega + (121)(1k\Omega) = 122.32k\Omega$$

$$Z_i = R_1 \parallel R_2 \parallel Z_b = 8.2k\Omega \parallel 1.5k\Omega \parallel 122.32k\Omega = 1.26k\Omega$$

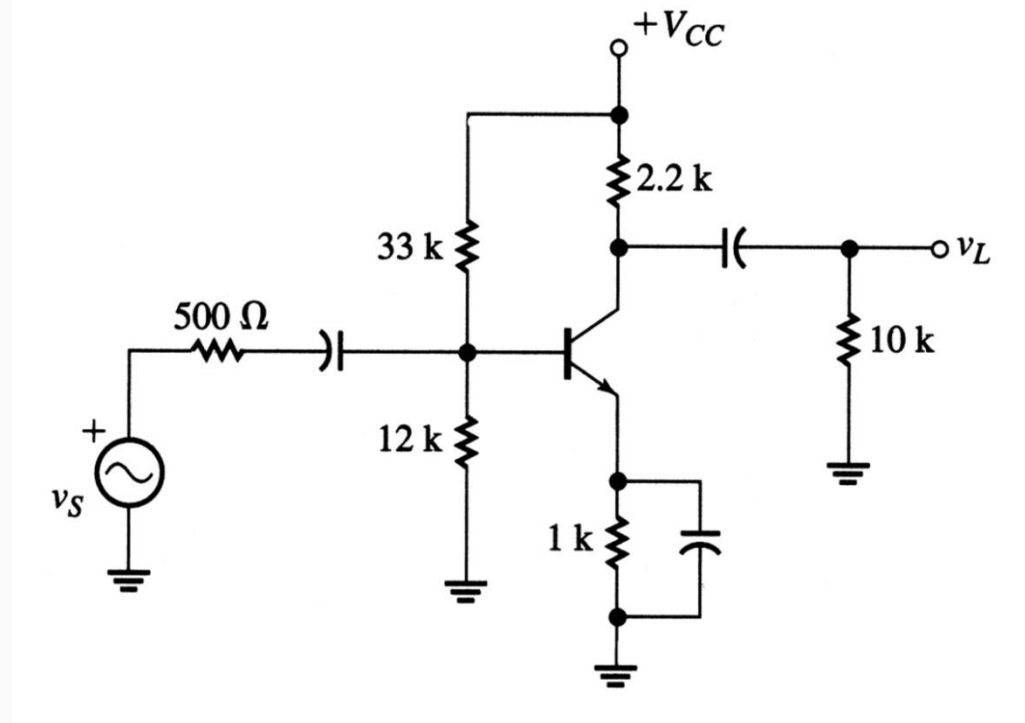
**Output impedance:**  $Z_o = R_C = 4.3k\Omega$

**Voltage gain:**  $A_{v(oc)} = \frac{V_{out}}{V_{in}} = -\frac{g_m R_C}{1 + g_m R_E} = -\frac{(91.2mS)(4.09k\Omega)}{1 + (91.2mS)(1k\Omega)} = -4.25$

# Exercise

Draw the small signal ac equivalent circuit. If  $+V_{CC} = 12V$ ,  $V_A = \infty$ ,  $V_{BE} = 0.7V$  and  $\beta = 80$ , calculate the values of :

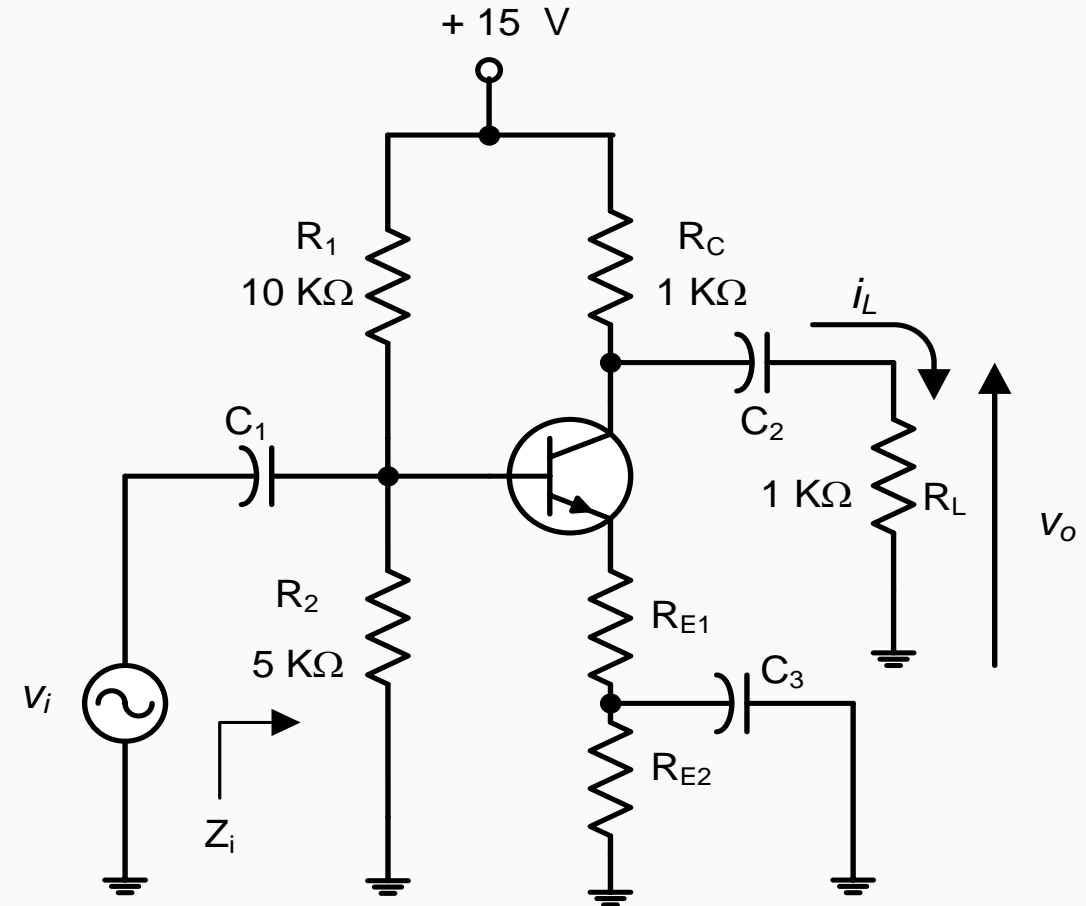
- (a) Input and output impedances
- (b) Voltage gain  $A_V$  and  $A_{VS}$



# Exercise

Given  $\beta = h_{fe} = 200$ ,  $V_{BE} = 0.6 \text{ V}$ ,  $V_{CEQ} = 10 \text{ V}$ ,  $V_A \rightarrow \infty$ ,  $A_v(\text{dB})$  at middle frequency = 14dB.

- Draw the mid-frequency AC equivalent circuit.
- Determine  $R_{E1}$  and  $R_{E2}$ .
- Determine the amplifier input impedance,  $Z_i$ .
- Ratio of  $i_L/v_i$ .



$$R_{E1} = 56.67 \Omega; R_{E2} = 7.27 \text{ k}\Omega;$$

$$Z_i = 2.86 \text{ k}\Omega; i_L/v_i = 4.99 \text{ mS}$$