

# SOIL STRESS

- \*TOTAL STRESS,  $\sigma$
- \*PORE PRESSURE,  $u$
- \*EFFECTIVE STRESS,  $\sigma'$

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# STRESS

$$\sigma \text{ (kN/m}^2\text{)} = \gamma \cdot z$$

where:

$\gamma$  = unit weight of soil (kN/m<sup>3</sup>)

$z$  = depth / thickness from ground surface (m)

## TOTAL NORMAL STRESS

- Generated by the mass in the soil body, calculated by sum up the unit weight of all the material (soil solids + water) multiplied by soil thickness or depth.
- Denoted as  $\sigma$ ,  $\sigma_v$ ,  $P_0$
- The unit weight of soil is in natural condition and the water influence is ignored.
- Total stress increases with depth and with unit weight:  
Vertical total stress at depth  $z$

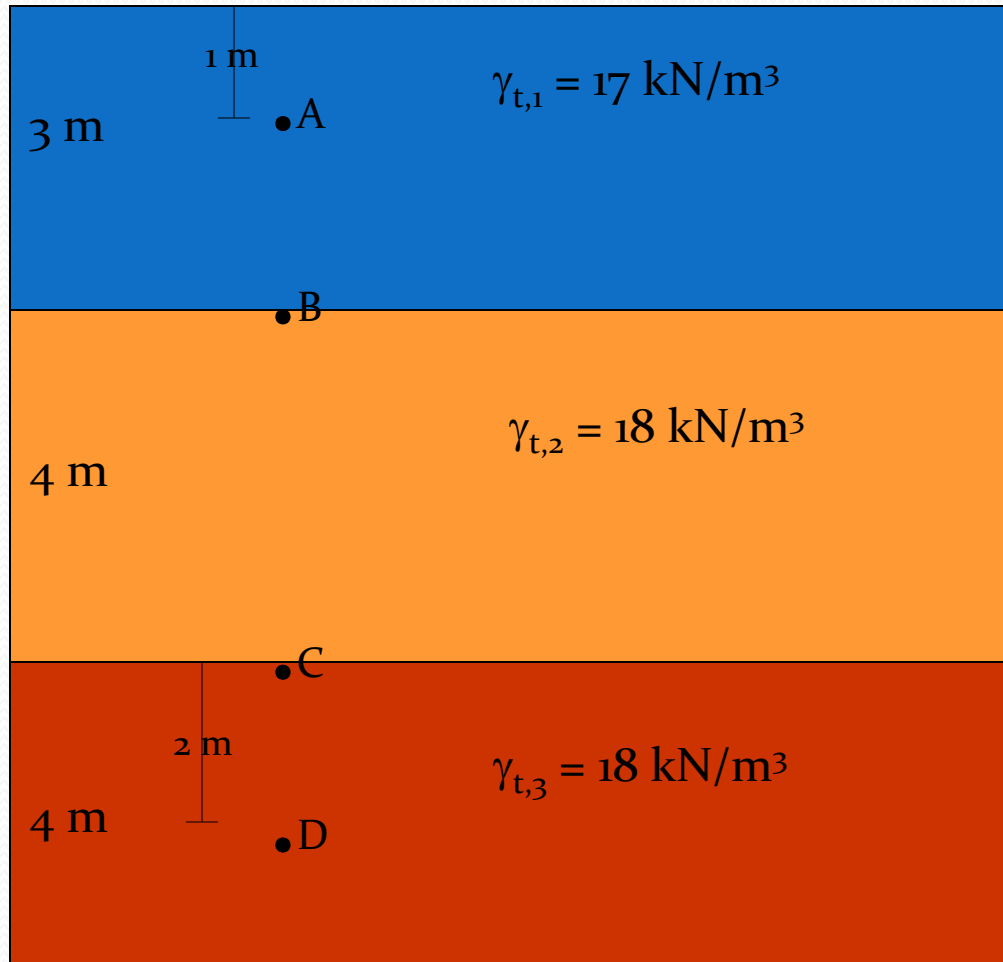
$$\sigma = \sum \gamma_t \cdot z$$

$z$  = The depth of point



## EXAMPLE 1 : Total stress in multi-layered in soil

The total stress at depth  $z$  (i.e. Point D) is the sum of the weights of soil in each layer thickness above.



$$\begin{aligned}\sigma_A &= \gamma_{t,1} \times 1 \text{ m} \\ &= 17 \text{ kN/m}^2\end{aligned}$$

$$\begin{aligned}\sigma_B &= \gamma_{t,1} \times 3 \text{ m} \\ &= 51 \text{ kN/m}^2\end{aligned}$$

$$\begin{aligned}\sigma_C &= \gamma_{t,1} \times 3 \text{ m} + \gamma_{t,2} \times 4 \text{ m} \\ &= 123 \text{ kN/m}^2\end{aligned}$$

$$\begin{aligned}\sigma_D &= \gamma_{t,1} \times 3 \text{ m} + \gamma_{t,2} \times 4 \text{ m} \\ &\quad + \gamma_{t,3} \times 2 \text{ m} \\ &= 159 \text{ kN/m}^2\end{aligned}$$

# Pore water pressure (u)

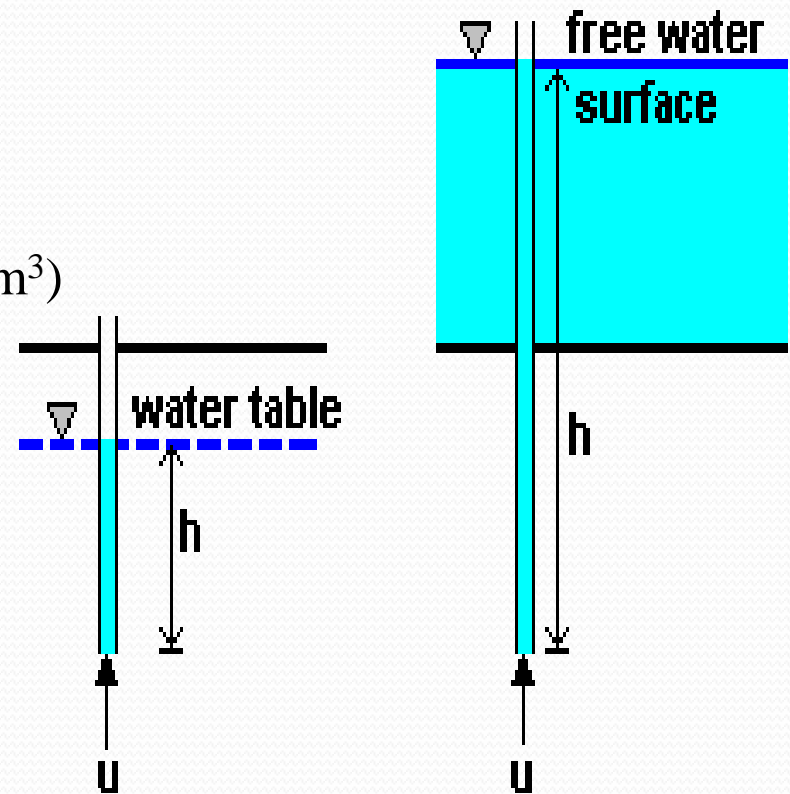
Under hydrostatic conditions (no water flow) the pore pressure at a given point is given by the **hydrostatic pressure**:

$$u = \gamma_w \cdot h_w$$

Where

$\gamma_w$  = unit weight of water ( $9.81 \text{ kN/m}^3 \approx 10 \text{ kN/m}^3$ )

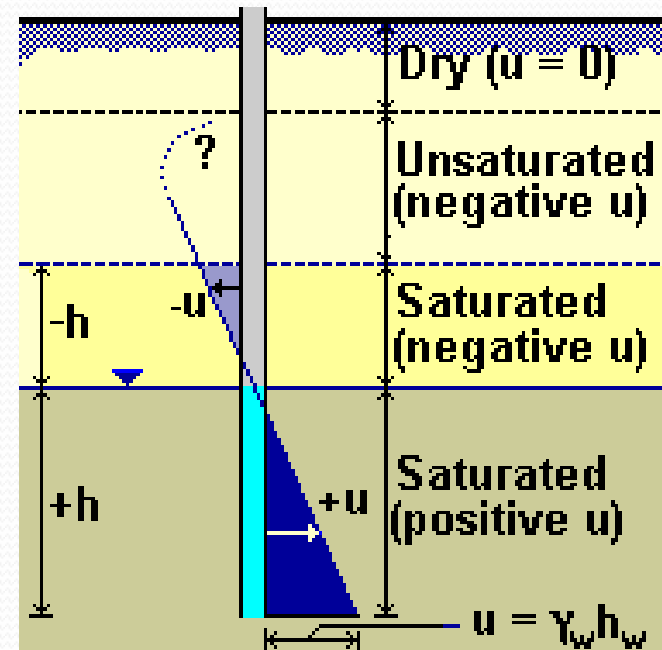
$h_w$  = depth below water table or overlying water surface



# Negative pore pressure

- Below the water table, pore pressures are **positive**.
- In dry soil, the pore pressure is **zero**.
- Above the water table, when the soil is saturated, pore pressure will be **negative**.

$$u = -(\gamma_w \cdot h_w)$$

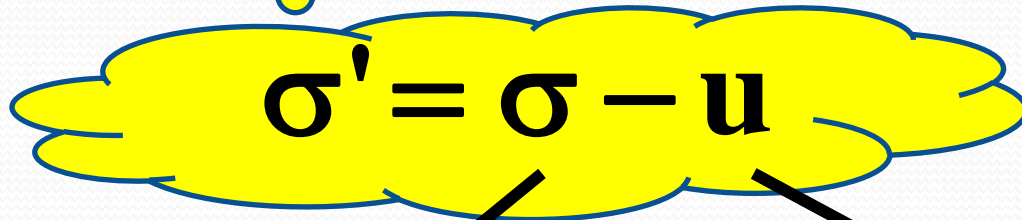


## EFFECTIVE STRESS

- Defined as soil stress which not influenced by water pressure in soil body.
- Published first time by Terzaghi at 1923 base on the experimental result
- Applied to saturated soil and has a relationship with two type of stress i.e.:
  - Total Normal Stress ( $\sigma$ )
  - Pore Water Pressure ( $u$ )
- Effective stress formula

$$\sigma' = \sigma - u$$

## EFFECTIVE STRESS


$$\sigma' = \sigma - u$$

$$\sigma = \gamma_t \cdot z$$

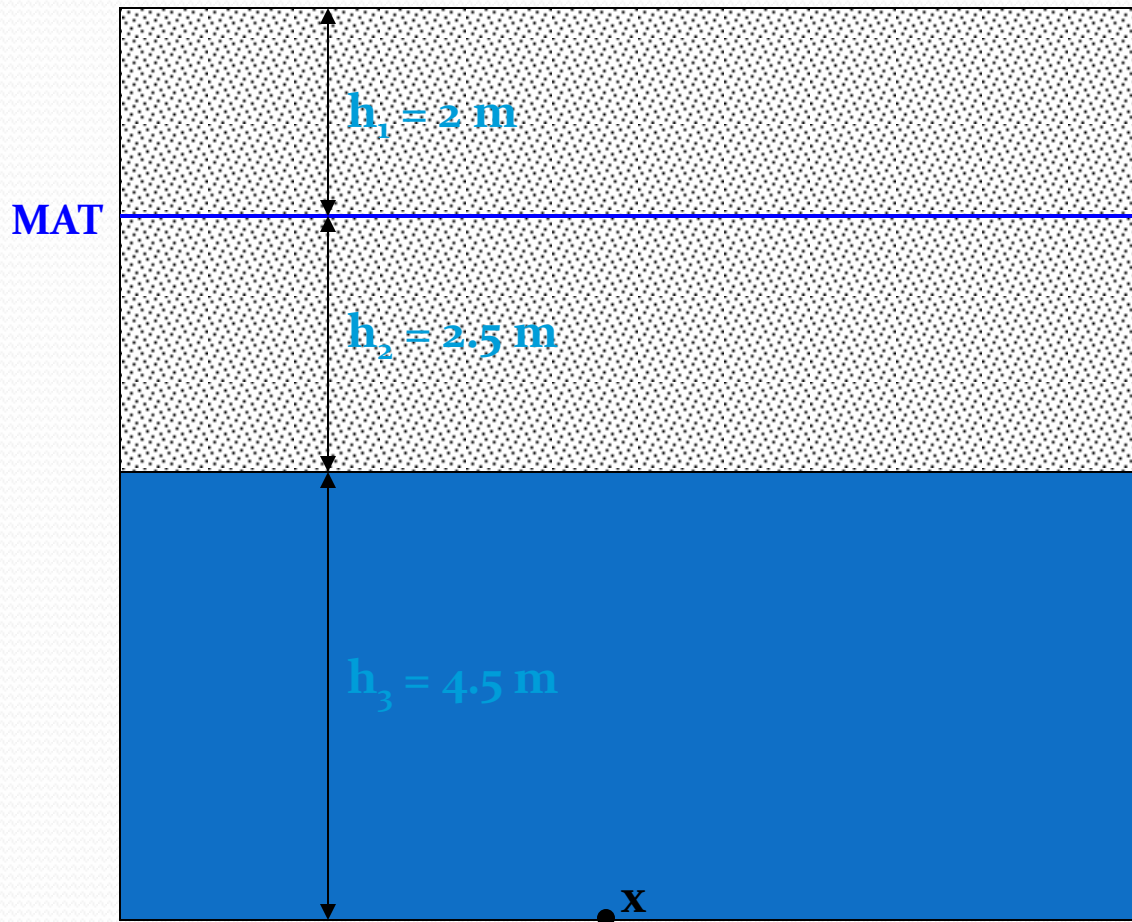
$$u = \gamma_w \cdot z$$

@

$$\sigma' = (\gamma_t - \gamma_w) \cdot z = \gamma' \cdot z$$



## EXAMPLE 2



**Sand**

$$\gamma_{\text{sat}} = 18.0 \text{ kN/m}^3$$

$$\gamma_d = 13.1 \text{ kN/m}^3$$

**Clay**

$$\gamma_{\text{sat}} = 19.80 \text{ kN/m}^3$$

## EXAMPLE

- Total Stress

$$\begin{aligned}\sigma &= \gamma_{d,1} \cdot h_1 + \gamma_{t,1} \cdot h_2 + \gamma_{t,2} \cdot h_3 \\ \sigma &= 13.1 \cdot 2 + 18 \cdot 2.5 + 19.8 \cdot 4.5 \\ &= 160.3 \text{ kN/m}^2\end{aligned}$$

- Pore Water Pressure

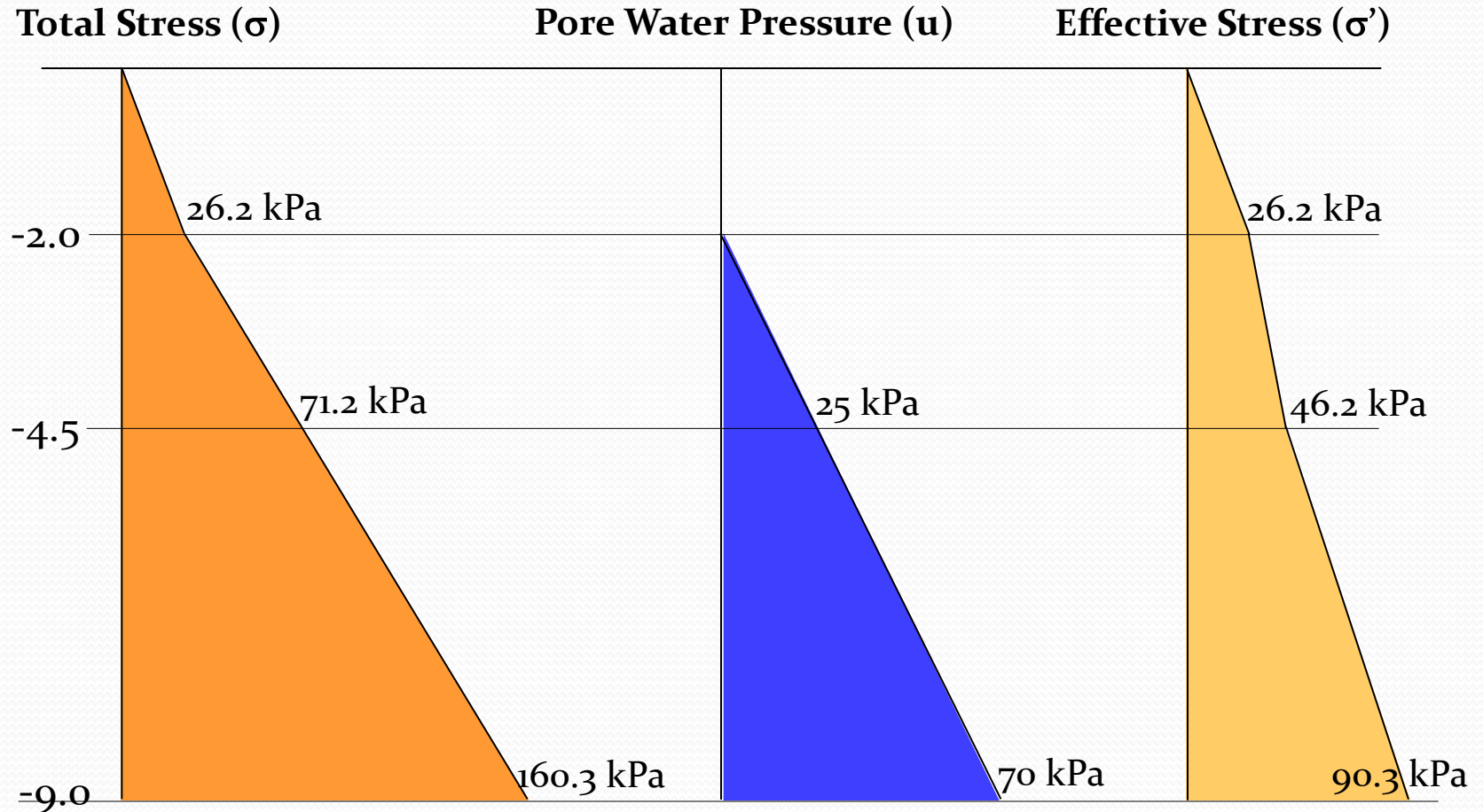
$$\begin{aligned}u &= \gamma_w \cdot (h_2 + h_3) \\ u &= 10 \cdot 7 \\ &= 70 \text{ kN/m}^2\end{aligned}$$

- Effective Stress

$$\sigma' = \sigma - u = 90.3 \text{ kN/m}^2$$

$$\begin{aligned}\sigma' &= \gamma_{d,1} \cdot h_1 + (\gamma_{t,2} - \gamma_w) \cdot h_2 + (\gamma_{t,2} - \gamma_w) \cdot h_3 \\ \sigma' &= 13.1 \cdot 2 + (18-10) \cdot 2.5 + (19.8-10) \cdot 4.5 \\ &= 90.3 \text{ kN/m}^2\end{aligned}$$

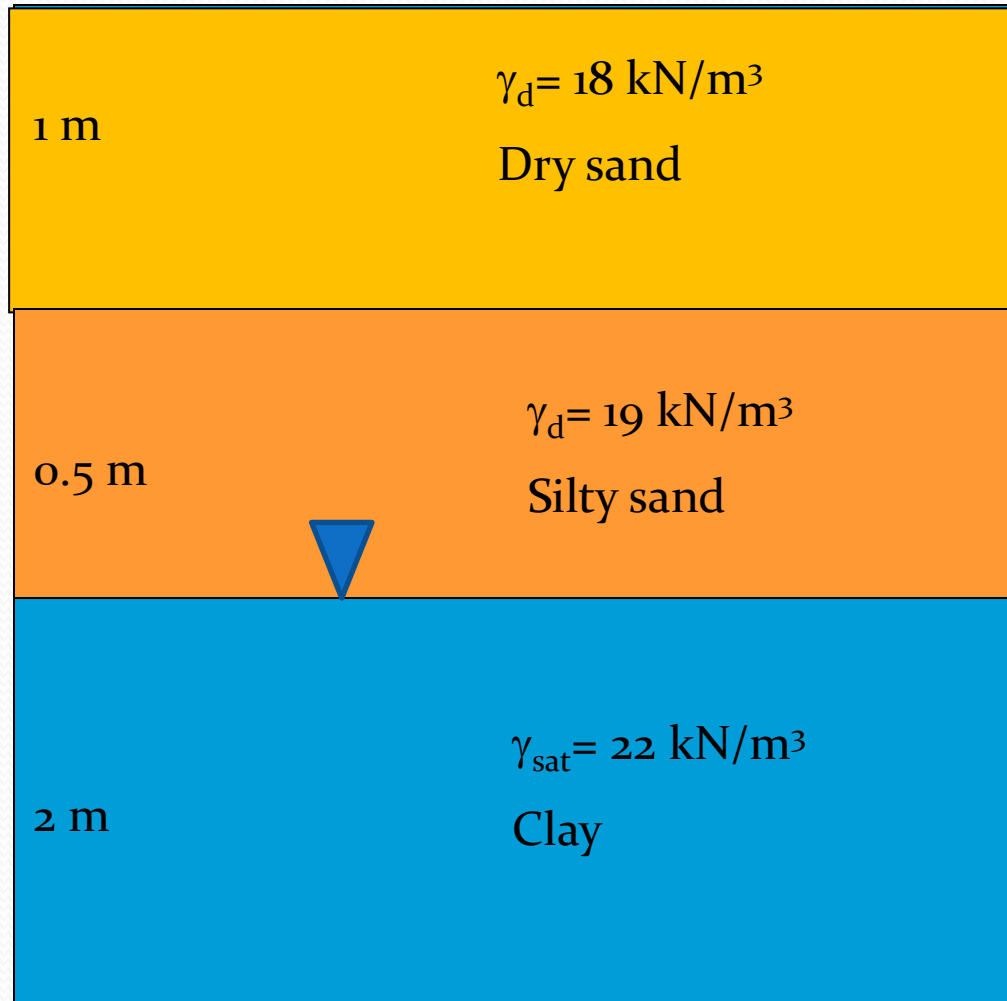
# EXAMPLE



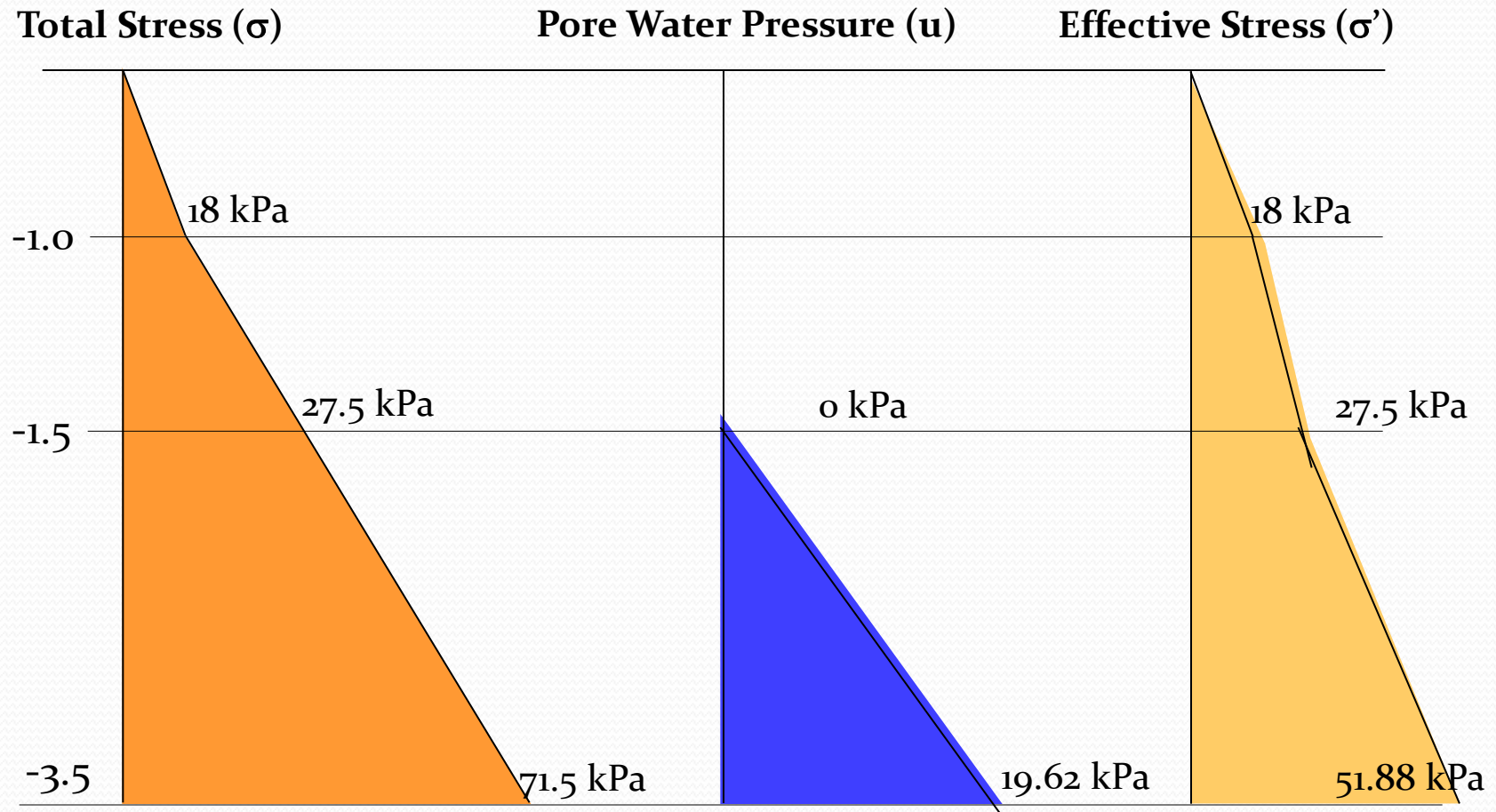
Profile of Vertical Stress / Stress distribution Diagram

## EXAMPLE 3

For the soil profile shown here, plot the stress distribution diagram including total stress, pore pressure and effective stress



## EXAMPLE 3 (answer)



Profile of Vertical Stress / Stress distribution Diagram