Lecture # 07: Laminar and Turbulent Flows

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Reynolds' experiment

Fig. 9.1. Sketch of Reynolds's dye experiment, taken from his 1883 paper.

\[ \text{Re} = \frac{\rho DU}{\mu} \]

Fig. 9.2. Reynolds's drawings of the flow in his dye experiment.
Laminar Flows and Turbulence Flows

- Laminar flow, sometimes known as streamline flow, occurs when a fluid flows in parallel layers, with no disruption between the layers. Inflow dynamics laminar flow is a flow regime characterized by high momentum diffusion, low momentum convention, pressure and velocity almost independent from time. It is the opposite of turbulent flow.
  - In nonscientific terms laminar flow is "smooth," while turbulent flow is "rough."

- In fluid dynamics, turbulence or turbulent flow is a fluid regime characterized by chaotic, stochastic property changes. This includes low momentum diffusion, high momentum conversation, and rapid variation of pressure and velocity in space and time.
  - Flow that is not turbulent is called laminar flow
Turbulent Flows in a Pipe

\[ \text{Re} = \frac{\rho V D}{\mu} \]
Characterization of Turbulent Flows

\[ u = \bar{u} + u'; \quad v = \bar{v} + v'; \quad w = \bar{w} + w' \]

\[ \bar{u} = \frac{1}{T} \int_{t_0}^{t_0+T} u(x, y, z, t) \, dt; \quad \bar{v} = \frac{1}{T} \int_{t_0}^{t_0+T} v(x, y, z, t) \, dt; \quad \bar{w} = \frac{1}{T} \int_{t_0}^{t_0+T} w(x, y, z, t) \, dt \]

**Figure 7.7** Velocity components in a turbulent pipe flow: (a) $x$-component velocity; (b) $r$-component velocity; (c) $\theta$-component velocity.
Turbulence intensities

\( \bar{u}' = 0; \quad \bar{v}' = 0 \quad \bar{w}' = 0 \)

\[
(u')^2 = \frac{1}{T} \int_{t_0}^{t_0+T} (u')^2 \, dt > 0; \quad (v')^2 > 0 \quad (w')^2 > 0
\]
Turbulent Shear Stress

Laminar flows:
\[ \tau_{\text{lam}} = \mu \frac{\partial u}{\partial y} \]

Turbulent flows:
\[ \tau_{\text{turb}} = -\rho u'v' \]
\[ \tau = \tau_{\text{lam}} + \tau_{\text{turb}} = \mu \frac{\partial u}{\partial y} - \rho u'v' \]

A.laminar flow

b.turbulent flow
Laminar Flows and Turbulence Flows

\[ C_d = \frac{D}{\frac{1}{2} \rho U^2 A} \]

\[ \text{Re} = \frac{\rho DU}{\mu} \]

\[ C_D = \frac{1}{2} \frac{\delta}{b^2} \frac{bD}{bD} \]

\[ b = \text{length} \]

\[ \text{Re} = \frac{UD}{v} \]
Flow Around A Sphere with laminar and Turbulence Boundary Layer

Top:
Instantaneous flow past a sphere at $\text{Re}_D = 15,000$. Dye in water shows a laminar boundary layer separating ahead of the equator and remaining laminar for almost one radius. It then becomes unstable and quickly turns turbulent.

Bottom:
Instantaneous flow past a sphere at $\text{Re}_D = 30,000$ with a trip wire. A classical experiment of Prandtl and Wieselsberger is repeated here, using air bubbles in water. A wire hoop ahead of the equator trips the boundary layer. It becomes turbulent, so that it separates farther rearward than if it were laminar (compare with top photograph). The overall drag is thereby dramatically reduced, in a way that occurs naturally on a smooth sphere only at a Reynolds numbers ten times as great.
Laminar Flows and Turbulence Flows

Re=100,000

Smooth ball

Rough ball

Golf ball

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Automobile aerodynamics
Automobile Aerodynamics

Mercedes Boxfish

Vortex generator above a Mitsubishi rear window

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CONVENTIONAL AIRFOILS and LAMINAR FLOW AIRFOILS

- Laminar flow airfoils are usually thinner than the conventional airfoil.
- The leading edge is more pointed and its upper and lower surfaces are nearly symmetrical.
- The major and most important difference between the two types of airfoil is this, the thickest part of a laminar wing occurs at 50% chord while in the conventional design the thickest part is at 25% chord.
- Drag is considerably reduced since the laminar airfoil takes less energy to slide through the air.
- Extensive laminar flow is usually only experienced over a very small range of angles-of-attack, on the order of 4 to 6 degrees.
- Once you break out of that optimal angle range, the drag increases by as much as 40% depending on the airfoil

FIGURE 2: Extent of laminar flow on some famous airfoils.
Flow Separation on an Airfoil

- $\alpha = 0^\circ$
  - Separation points
  - Turbulent wake

- $\alpha = 5^\circ$
  - Separation point moves slightly forward

- $\alpha = 16^\circ$
  - Maximum lift
  - Separation point jumps forward
  - (Stall angle)

- $\alpha = 20^\circ$
  - Separated flow region expands and reduces lift
  - Large turbulent wake
  - (Reduced lift and large pressure drag)

Increasing distance downstream

Shoulder of airfoil - maximum speed outside of the boundary layer

Flow outside boundary layer is inviscid flow

Turbulent boundary layer

Stagnation point pressure = Total pressure $p_t$

Laminar boundary layer

Transition (laminar becomes turbulent)
Aerodynamic Performance of An Airfoil

\[ C_l = \frac{L}{\frac{1}{2} \rho V_w^2 c} \]

\[ C_d = \frac{D}{\frac{1}{2} \rho V_w^2 c} \]

Angle of Attack (degrees)

Lift Coefficient, \( C_l \)

Drag Coefficient, \( C_d \)

Before stall

After stall

Airfoil stall

Experimental data

Experimental data

GA(W)-1 airfoil

25 m/s

shadow region

vort: -4.5 -3.5 -2.5 -1.5 -0.5 0.5 1.5 2.5 3.5 4.5

\( \rho \)
Low-Reynolds-number airfoil (with Re<500,000) aerodynamics is important for both military and civilian applications, such as propellers, sailplanes, ultra-light man-carrying/man-powered aircraft, high-altitude vehicles, wind turbines, unmanned aerial vehicles (UAVs) and Micro-Air-Vehicles (MAVs).

Since laminar boundary layers are unable to withstand any significant adverse pressure gradient, laminar flow separation is usually found on low-Reynolds-number airfoils. Post-separation behavior of the laminar boundary layers would affect the aerodynamic performances of the low-Reynolds-number airfoils significantly.

Separation bubbles are usually found to form on the upper surfaces of low-Reynolds-number airfoils. Separation bubble would burst suddenly to cause airfoil stall at high AOA when the adverse pressure gradient becoming too big.
Surface Pressure Coefficient distributions \((Re=68,000)\)

Typical surface pressure distribution when a laminar separation bubble is formed \((Russell, 1979)\)

\(GA (W)-1\) airfoil
(also labeled as NASA LS(1)-0417)
Laminar Separation Bubble on a Low-Reynolds-number Airfoil

PIV measurement results at AOA = 10 deg, Re=68,000

(Hu et al., ASME Journal of Fluid Engineering, 2008)
Stall Hysteresis Phenomena

- **Stall hysteresis**, a phenomenon where stall inception and stall recovery do not occur at the same angle of attack, has been found to be relatively common in low-Reynolds-number airfoils.

- When stall hysteresis occurs, the coefficients of lift, drag, and moment of the airfoil are found to be multiple-valued rather than single-valued functions of the angle of attack.

- **Stall hysteresis** is of practical importance because it produces widely different values of lift coefficient and lift-to-drag ratio for a given airfoil at a given angle of attack. It could also affect the recovery from stall and/or spin flight conditions.
**Measured airfoil lift and drag coefficient profiles**

- The hysteresis loop was found to be clockwise in the lift coefficient profiles, and counter-clockwise in the drag coefficient profiles.
- The aerodynamic hysteresis resulted in significant variations of lift coefficient, $C_l$, and lift-to-drag ratio, $l/d$, for the airfoil at a given angle of attack.
- The lift coefficient and lift-to-drag ratio at $AOA = 14.0$ degrees were found to be $C_l = 1.33$ and $l/d = 23.5$ when the angle is at the increasing angle branch of the hysteresis loop.
- The values were found to become $C_l = 0.8$ and $l/d = 3.66$ for the same $AOA=14.0$ degrees when the angle is at the deceasing angle branch of the hysteresis loop.

**GA(W)-1 airfoil, $Re_C = 160,000$**

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PIV Measurement results

(Hu, Yang, Igarashi, Journal of Aircraft, Vol. 44. No. 6, 2007)
Refined PIV Measurement Results

(Hu, Yang, Igarashi, Journal of Aircraft, Vol. 44. No. 6, 2007)
Lab 6: Airfoil Wake Measurements and Hotwire Anemometer Calibration

\[ \sum F_x = -D + \int_{c_s} (p\hat{n}dA)_x \]

\[ = -D + \int_1 p_{up} dA - \int_2 p(y) dA \]

Since \( p_{up} = p_\infty \); \( p(y) \approx p_\infty \)

\[ \implies \sum F_x = -D \]

\[ \implies \sum F_x = -D = \rho U_\infty^2 \int_2 \left[ \frac{U(y)}{U_\infty} \left( \frac{U(y)}{U_\infty} - 1 \right) \right] dA \]

\[ \implies D = \rho U_\infty^2 \int_2 \left[ \frac{U(y)}{U_\infty} \left( 1 - \frac{U(y)}{U_\infty} \right) \right] dA \]

\[ C_D = \frac{D}{\frac{1}{2} \rho U_\infty^2 C} = \frac{\frac{1}{2} \rho U_\infty^2 C}{\frac{1}{2} \rho U_\infty^2 C} \]

\[ \implies C_D = \frac{2}{C} \int_2 \left[ \frac{U(y)}{U_\infty} \left( 1 - \frac{U(y)}{U_\infty} \right) \right] dy \]

- Compared with the drag coefficients obtained based on airfoil surface pressure measurements at the same angles of attack!
Pressure rake with 41 total pressure probes (the distance between the probes $d=2\text{mm}$)
Lab 3: Airfoil Wake Measurements and Hotwire Anemometer Calibration

Flow Field

\[ \text{Current flow through wire} \]

\[ mc \frac{dT_w}{dt} = i^2 R_w - \dot{q}(V, T_w) \]

- Constant-temperature anemometry

CTA hotwire probe
To quantify the relationship between the flow velocity and voltage output from the CTA probe.

\[ y = a + bx + cx^2 + dx^3 + ex^4 \]

- \( a = 10.8 \)
- \( b = 3.77 \)
- \( c = -26.6 \)
- \( d = 13.2 \)
- \( r^2 = 1.00 \)

Maximum deviation: 0.166
Required Measurement Results

**Required Plots:**

- *C<sub>p</sub> distribution in the wake (for each angle of attack) for the airfoil wake measurements*
- *C<sub>d</sub> vs angle of attack (do your values look reasonable?) based on the airfoil wake measurements*
- *Your hot wire anemometer calibration curve: Velocity versus voltage output of hotwire anemometer (including a 4<sup>th</sup> order polynomial fit)*

**Please briefly describe the following details:**

- *How you calculated your drag—you should show your drag calculations*
- *How these drag calculations compared with the drag calculations you made in the previous experiment.*
- *Reynolds number of tests and the incoming flow velocity*