

# Lecture # 07: Laminar and Turbulent Flows

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# Reynolds' experiment

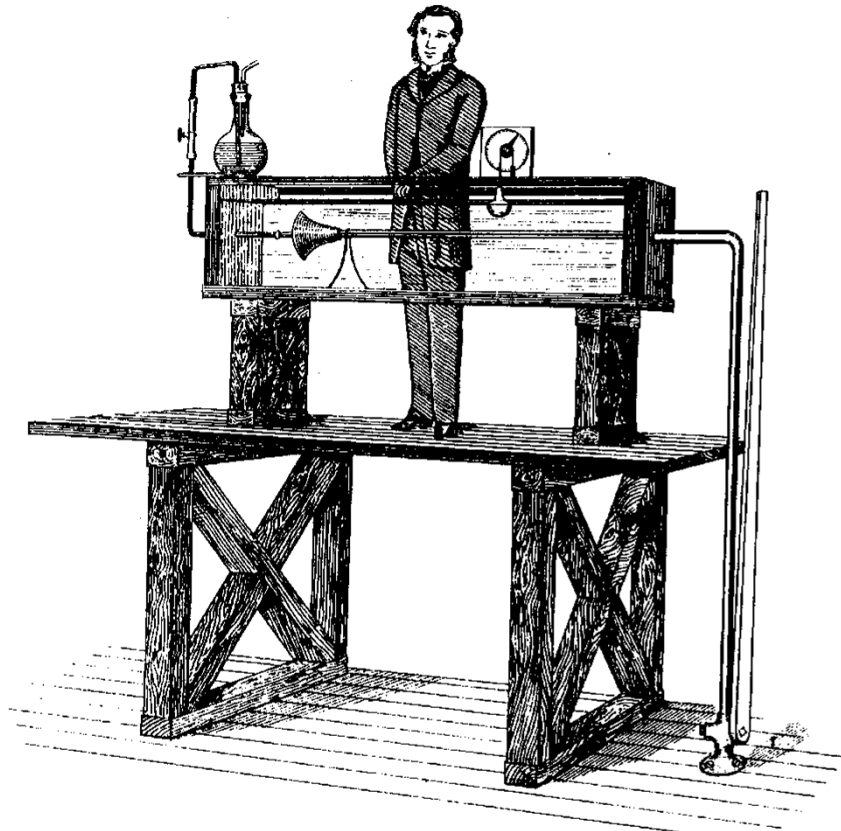


Fig. 9.1. Sketch of Reynolds' dye experiment, taken from his 1883 paper

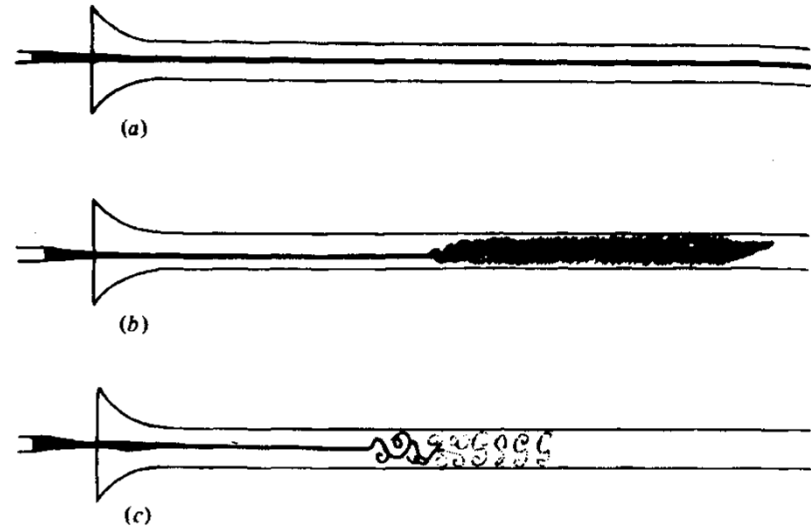
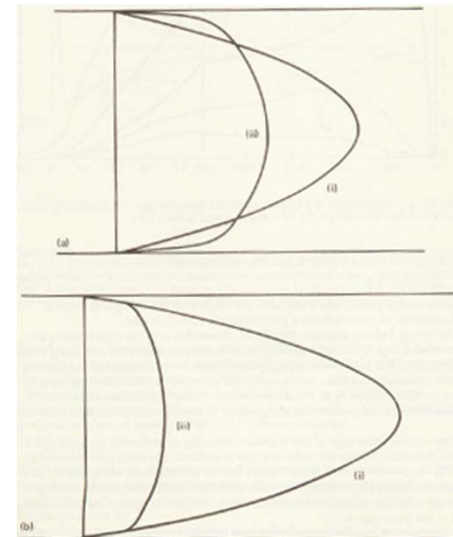


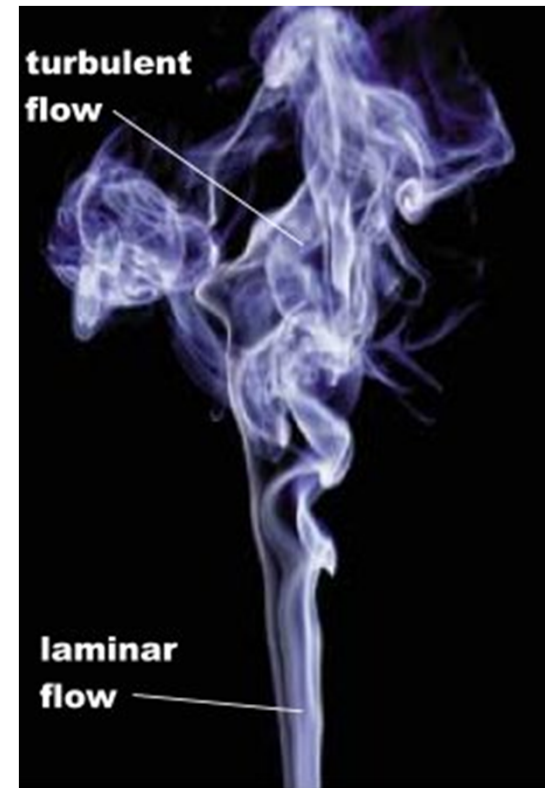
Fig. 9.2. Reynolds' drawings of the flow in his dye experiment.

$$Re = \frac{\rho DU}{\mu}$$

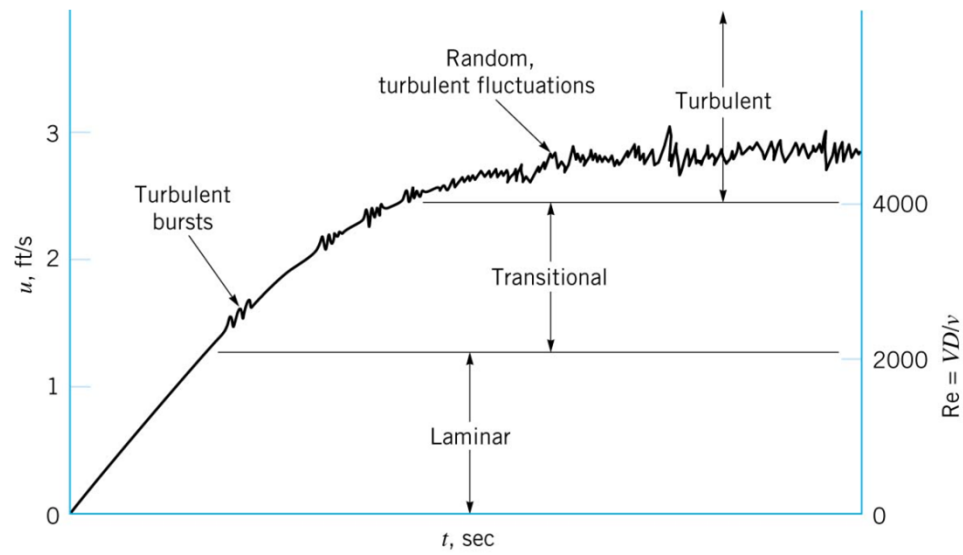
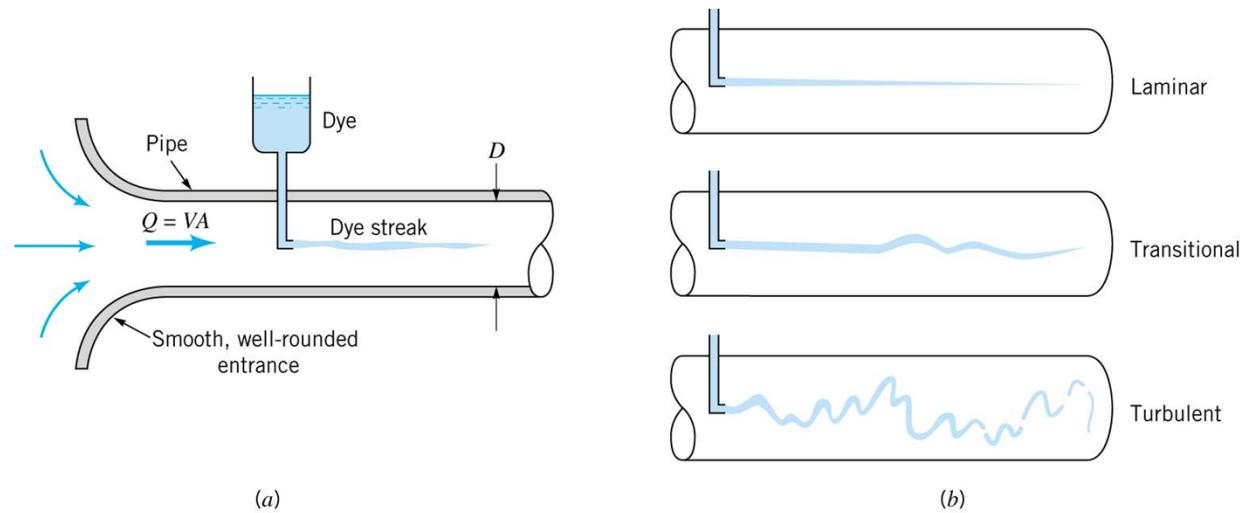


# Laminar Flows and Turbulence Flows

- *Laminar flow, sometimes known as streamline flow, occurs when a fluid flows in parallel layers, with no disruption between the layers. Inflow dynamics laminar flow is a flow regime characterized by high momentum diffusion, low momentum convection, pressure and velocity almost independent from time. It is the opposite of turbulent flow.*
  - *In nonscientific terms laminar flow is "smooth," while turbulent flow is "rough."*
- *In fluid dynamics, turbulence or turbulent flow is a fluid regime characterized by chaotic, stochastic property changes. This includes low momentum diffusion, high momentum convection, and rapid variation of pressure and velocity in space and time.*
  - *Flow that is not turbulent is called laminar flow*



# Turbulent Flows in a Pipe

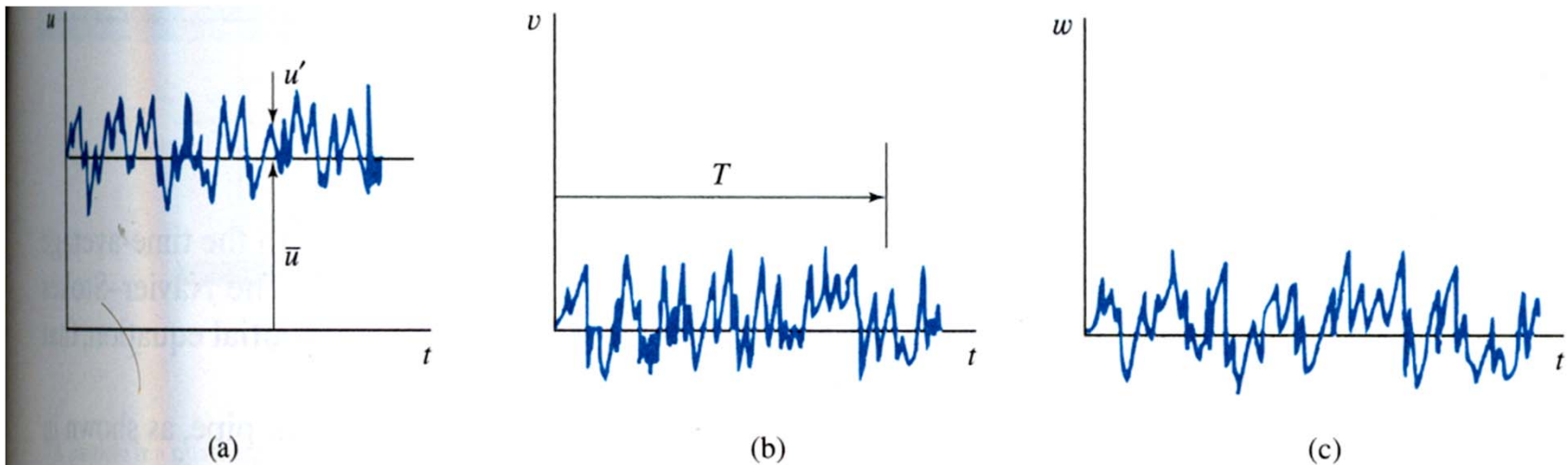


$$Re = \frac{\rho V D}{\mu}$$

# Characterization of Turbulent Flows

$$u = \bar{u} + u'; \quad v = \bar{v} + v' \quad w = \bar{w} + w'$$

$$\bar{u} = \frac{1}{T} \int_{t_0}^{t_0+T} u(x, y, z, t) dt; \quad \bar{v} = \frac{1}{T} \int_{t_0}^{t_0+T} v(x, y, z, t) dt; \quad \bar{w} = \frac{1}{T} \int_{t_0}^{t_0+T} w(x, y, z, t) dt$$

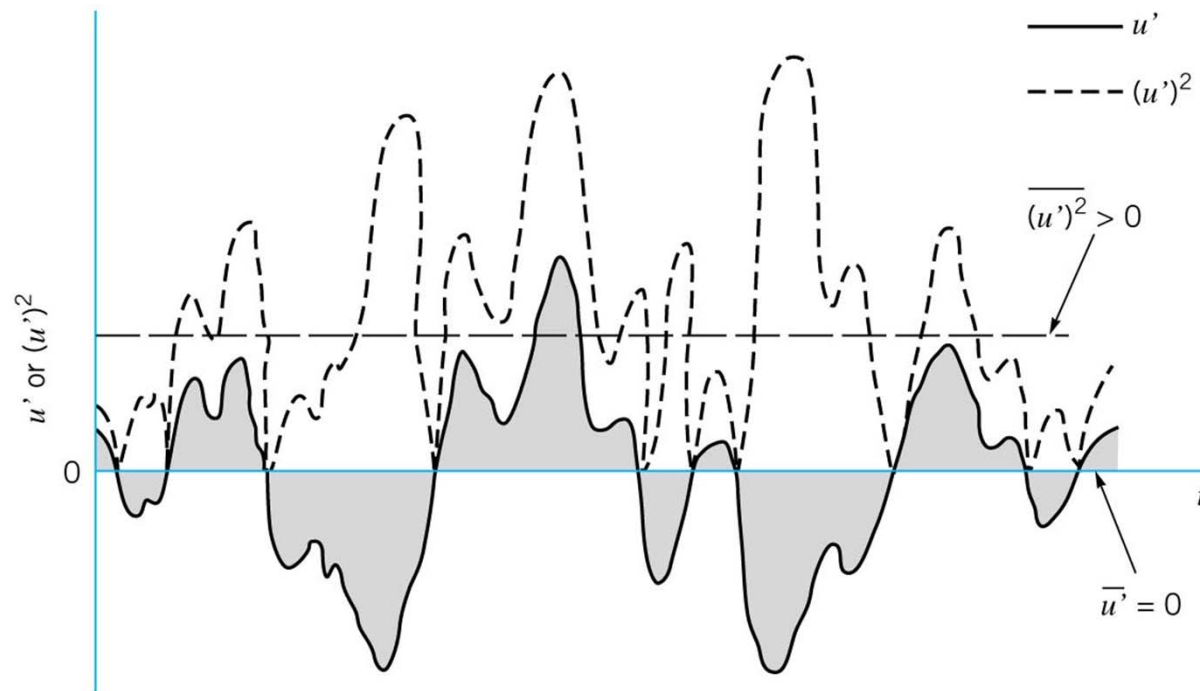


**FIGURE 7.7** Velocity components in a turbulent pipe flow: (a)  $x$ -component velocity; (b)  $r$ -component velocity; (c)  $\theta$ -component velocity.

## Turbulence intensities

$$\bar{u}' = 0; \quad \bar{v}' = 0 \quad \bar{w}' = 0$$

$$\overline{(u')^2} = \frac{1}{T} \int_{t_0}^{t_0+T} (u')^2 dt > 0; \quad \overline{(v')^2} > 0 \quad \overline{(w')^2} > 0$$



# Turbulent Shear Stress

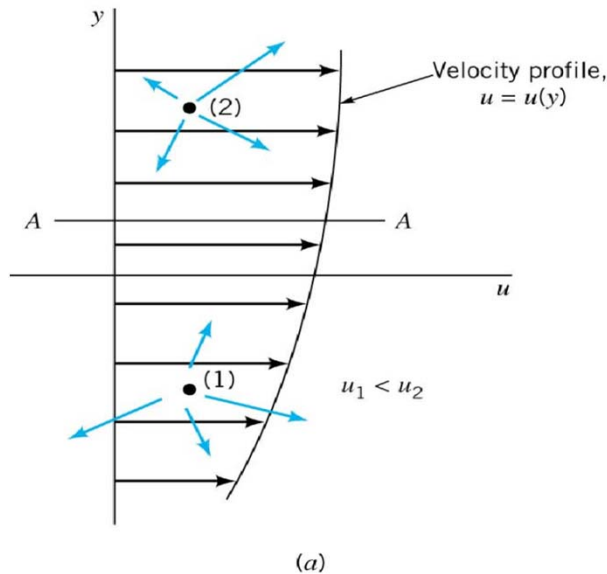
Laminar flows:

$$\tau_{lam} = \mu \frac{\partial u}{\partial y}$$

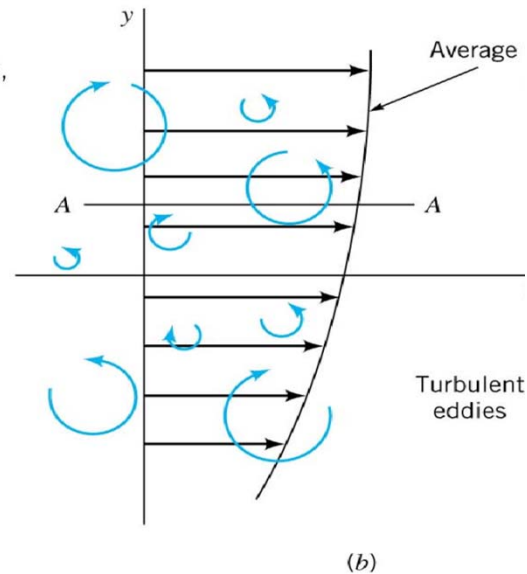
Turbulent flows:

$$\overline{\tau}_{turb} = -\rho \overline{u'v'}$$

$$\overline{\tau} = \overline{\tau}_{lam} + \overline{\tau}_{turb} = \mu \frac{\partial \overline{u}}{\partial y} - \rho \overline{u'v'}$$

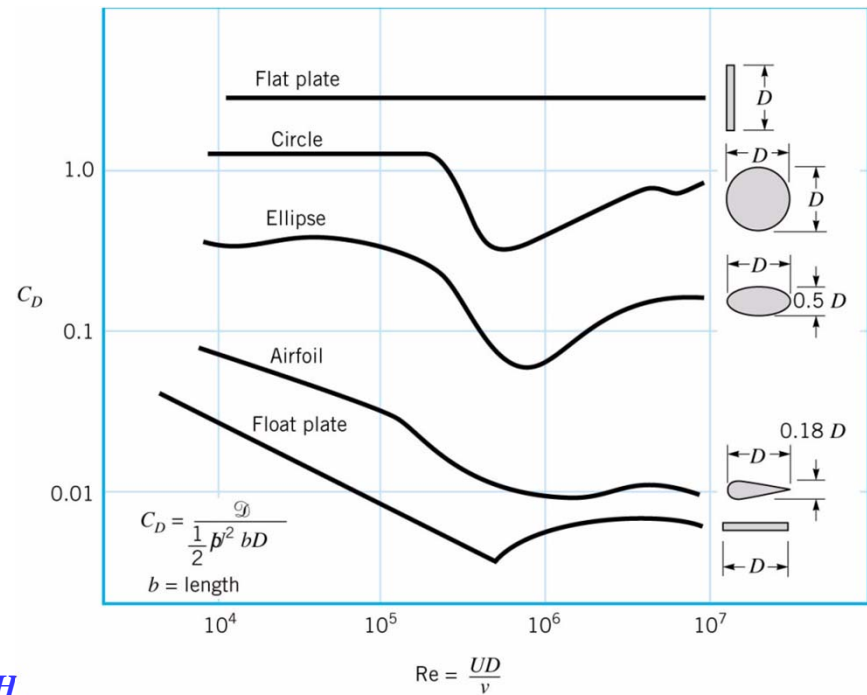
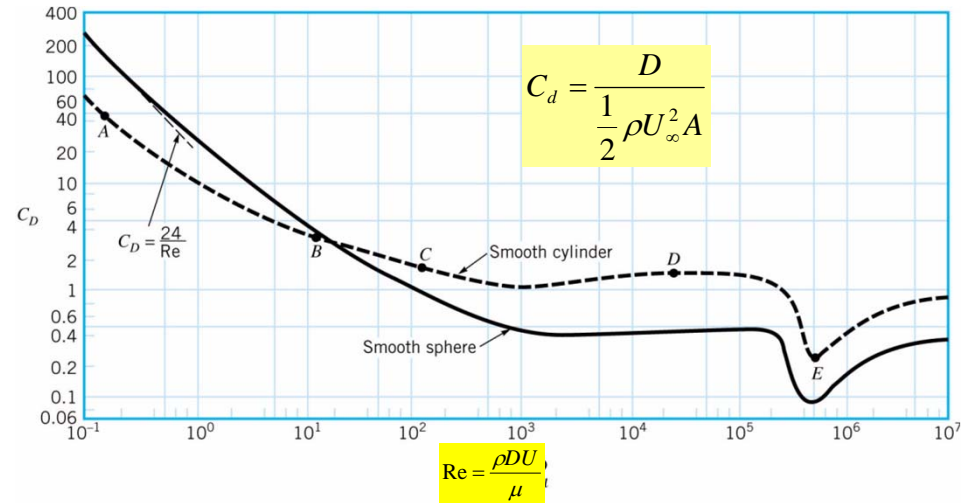
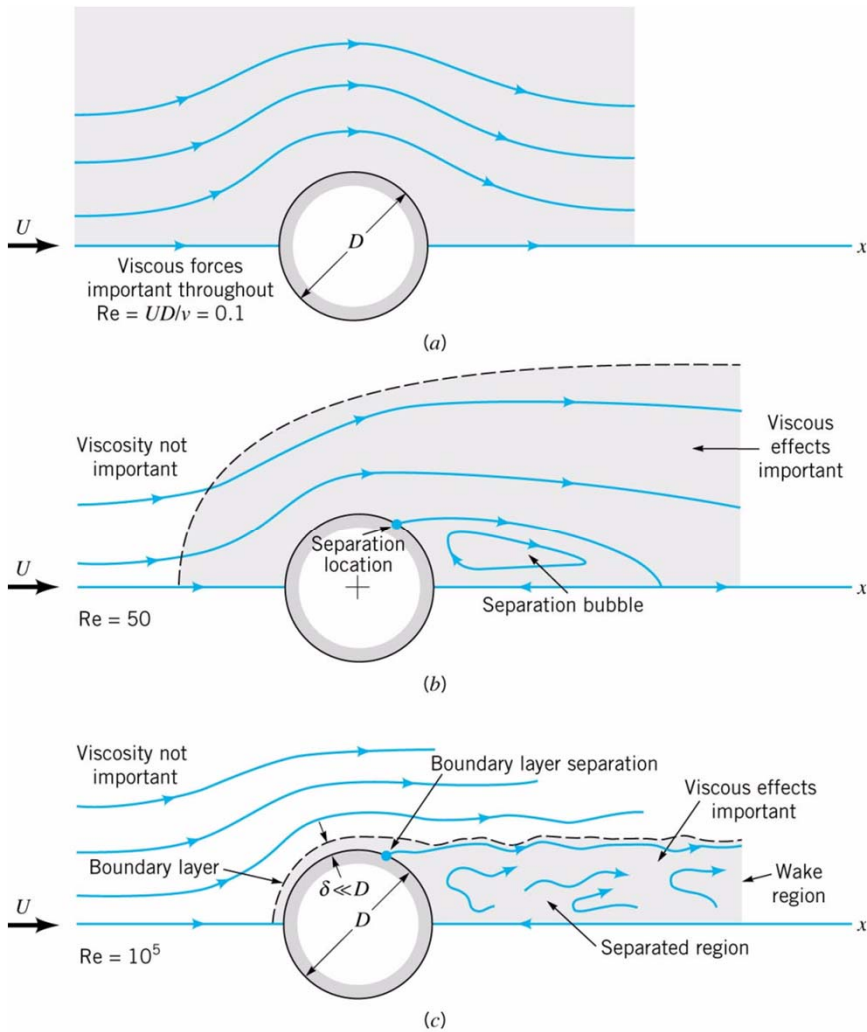


*A.laminar flow*



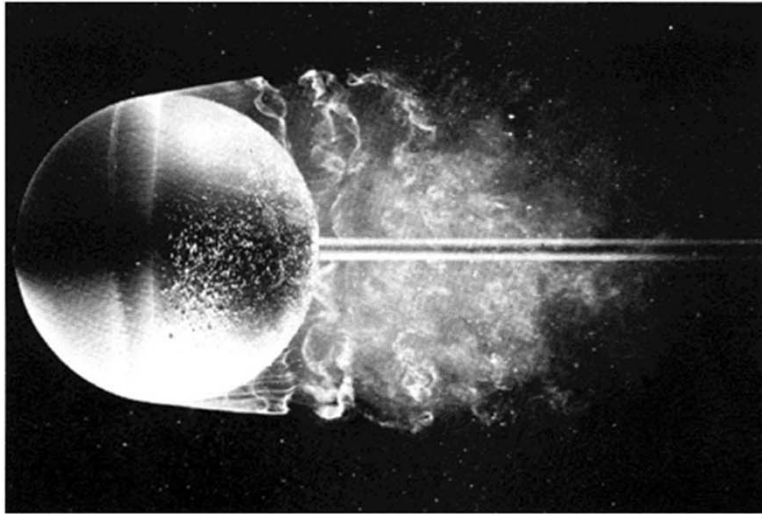
*b.turbulent flow*

# Laminar Flows and Turbulence Flows





# Flow Around A Sphere with laminar and Turbulence Boundary Layer

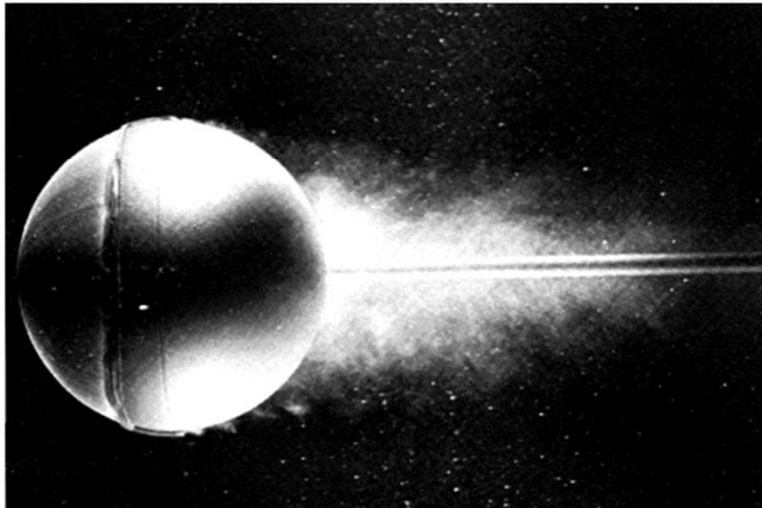


## Top:

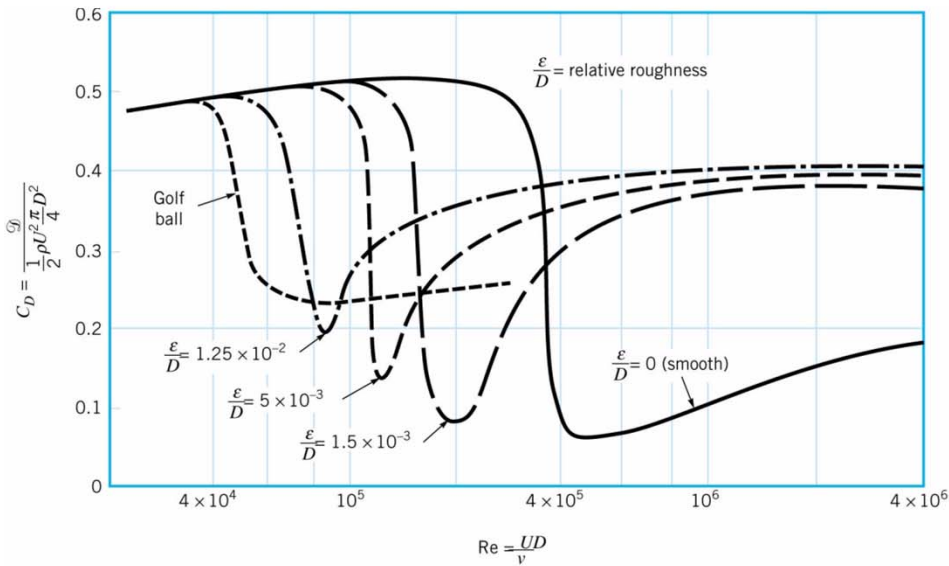
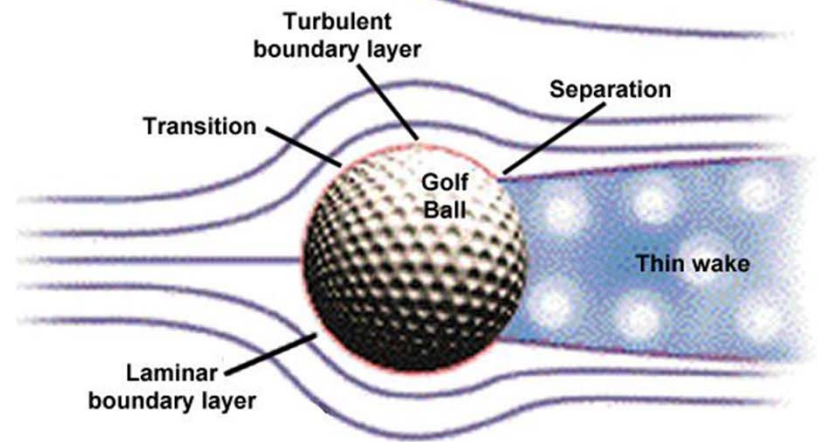
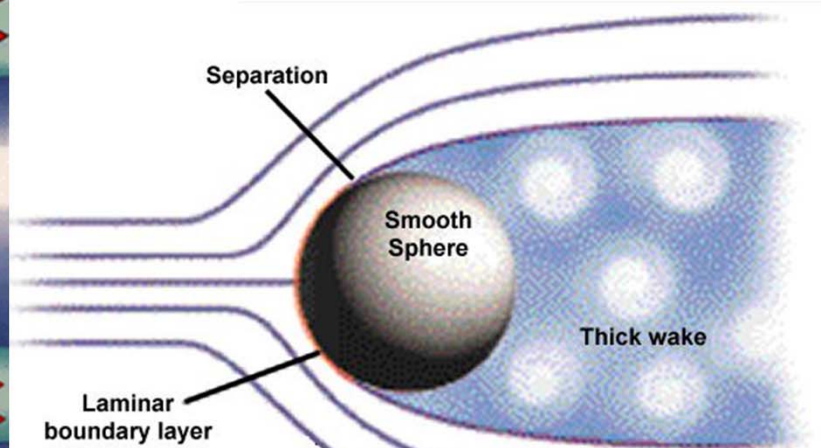
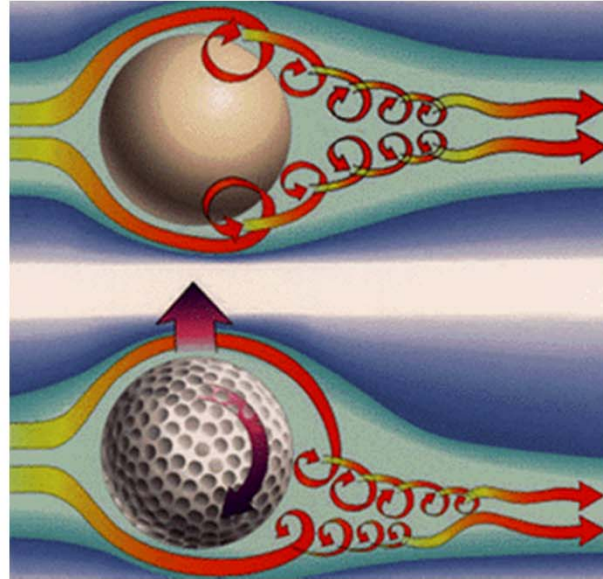
Instantaneous flow past a sphere at  $Re_D = 15,000$ . Dye in water shows a laminar boundary layer separating ahead of the equator and remaining laminar for almost one radius. It then becomes unstable and quickly turns turbulent.

## Bottom:

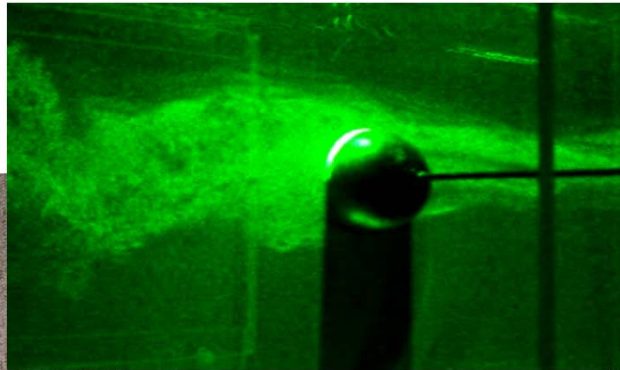
Instantaneous flow past a sphere at  $Re_D = 30,000$  with a trip wire. A classical experiment of Prandtl and Wieselsberger is repeated here, using air bubbles in water. A wire hoop ahead of the equator trips the boundary layer. It becomes turbulent, so that it separates farther rearward than if it were laminar (compare with top photograph). The overall drag is thereby dramatically reduced, in a way that occurs naturally on a smooth sphere only at a Reynolds numbers ten times as great.



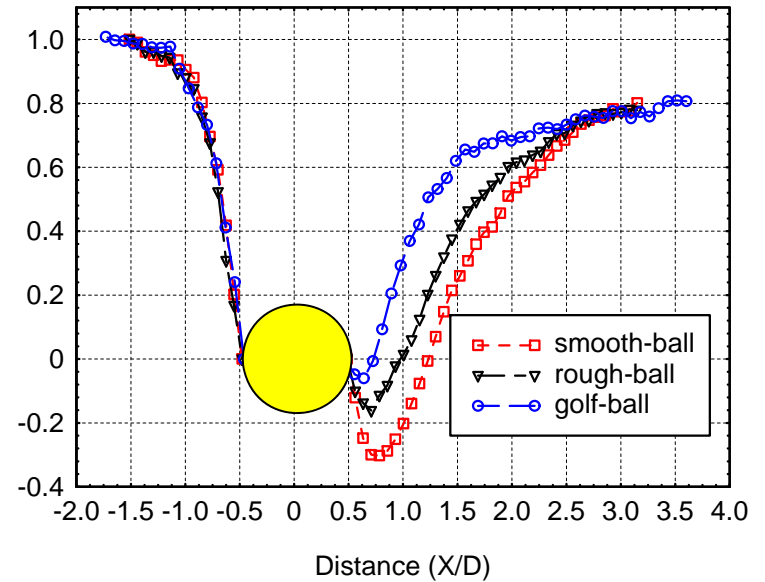
# Aerodynamics of Golf Ball



# Laminar Flows and Turbulence Flows



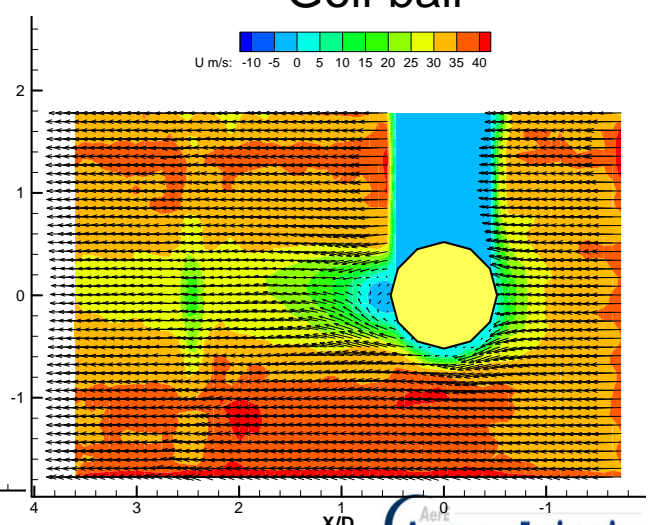
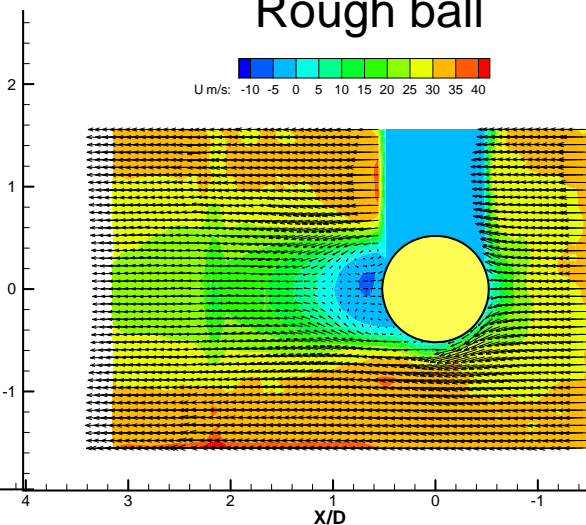
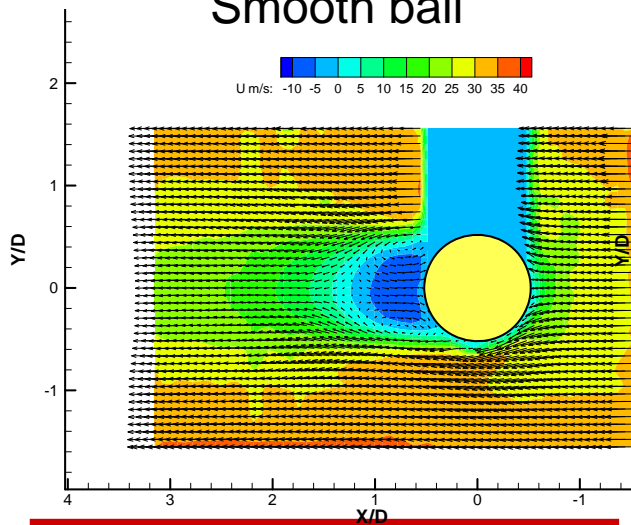
$Re=100,000$



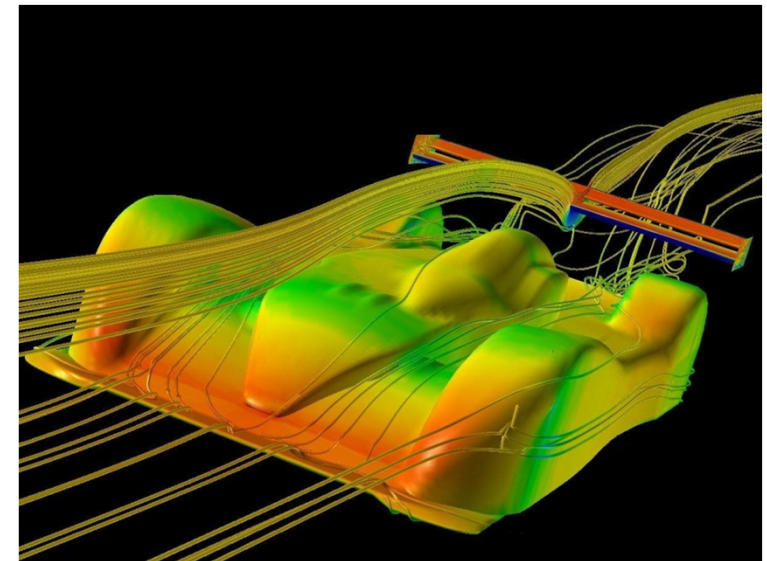
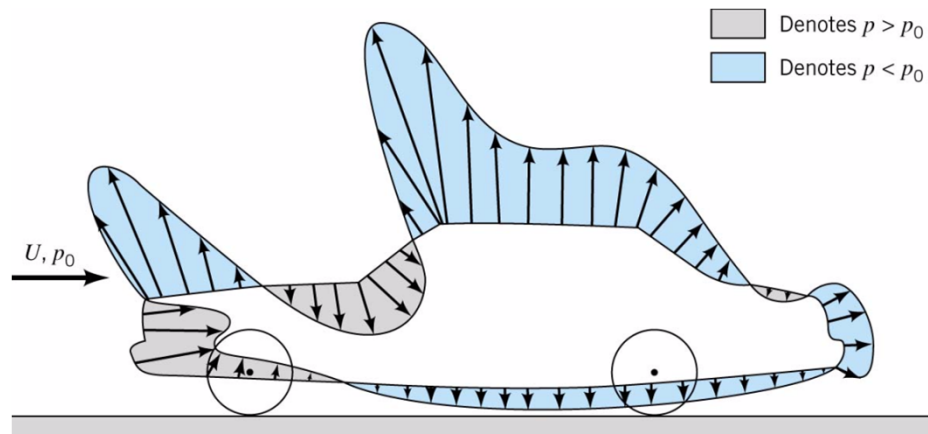
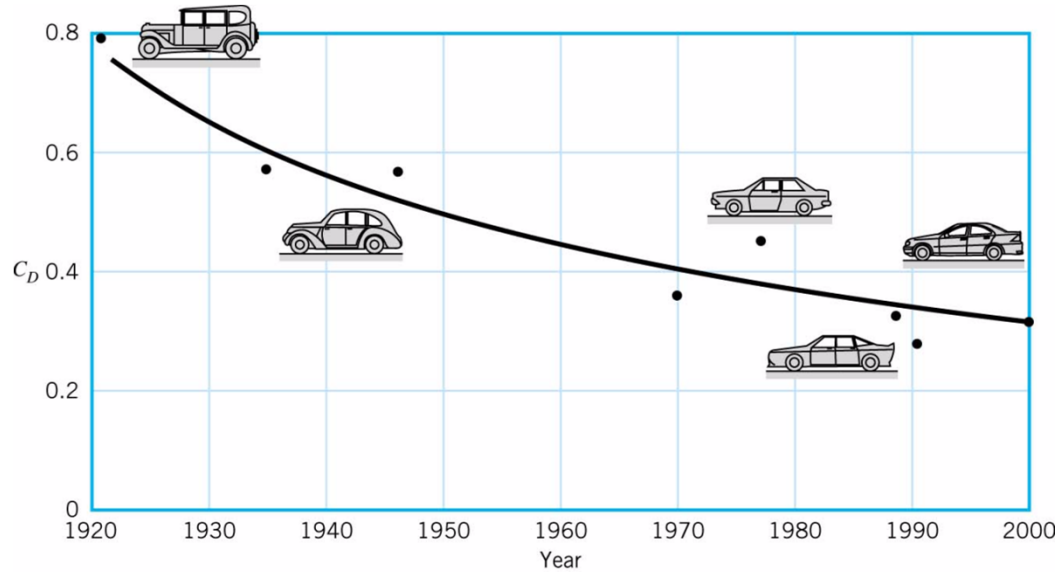
Smooth ball

Rough ball

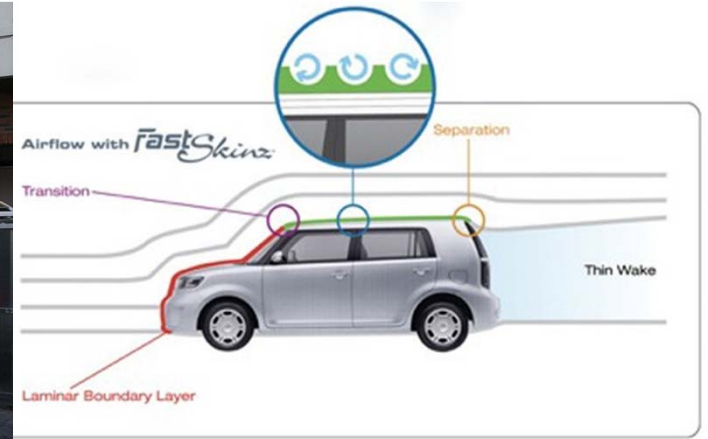
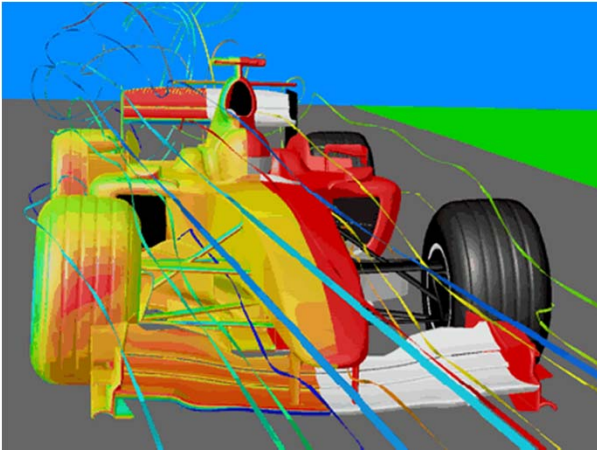
Golf ball



# Automobile aerodynamics



# Automobile Aerodynamics



Mercedes Boxfish

Vortex generator above a Mitsubishi rear window

# CONVENTIONAL AIRFOILS and LAMINAR FLOW AIRFOILS

- *Laminar flow airfoils are usually thinner than the conventional airfoil.*
- *The leading edge is more pointed and its upper and lower surfaces are nearly symmetrical.*
- *The major and most important difference between the two types of airfoil is this, the thickest part of a laminar wing occurs at 50% chord while in the conventional design the thickest part is at 25% chord.*
- *Drag is considerably reduced since the laminar airfoil takes less energy to slide through the air.*
- *Extensive laminar flow is usually only experienced over a very small range of angles-of-attack, on the order of 4 to 6 degrees.*
- *Once you break out of that optimal angle range, the drag increases by as much as 40% depending on the airfoil*

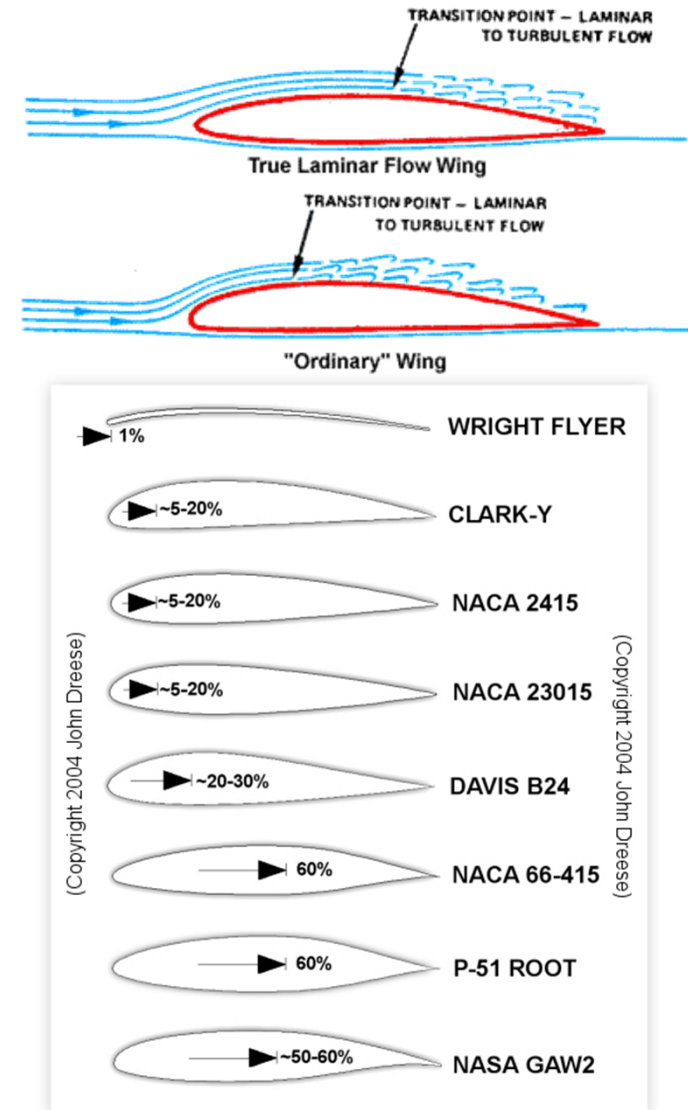
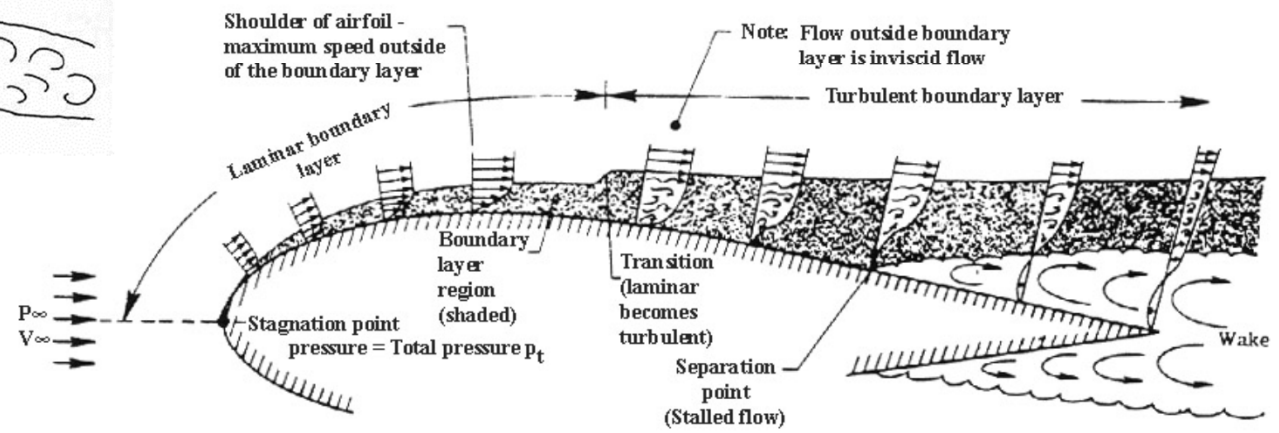
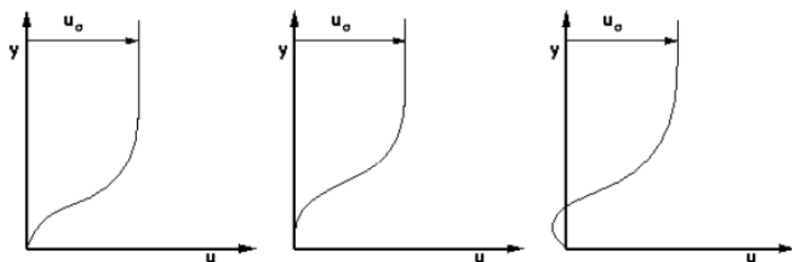
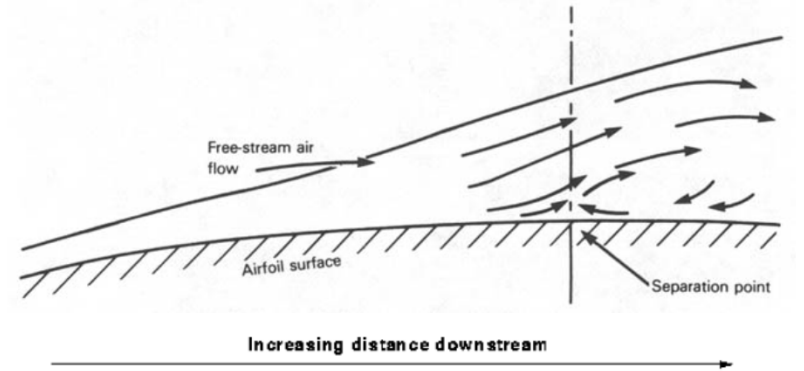
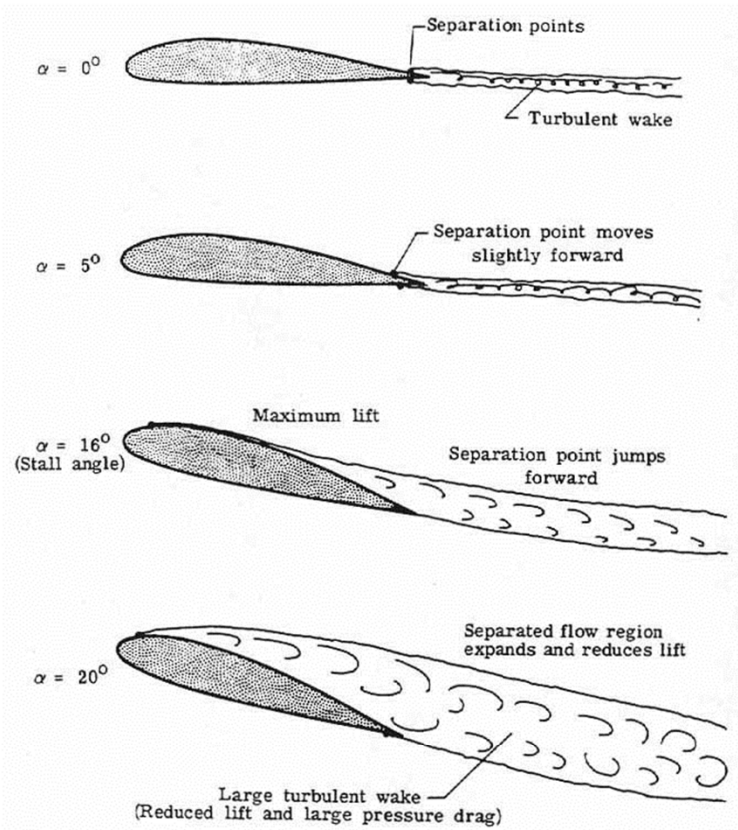
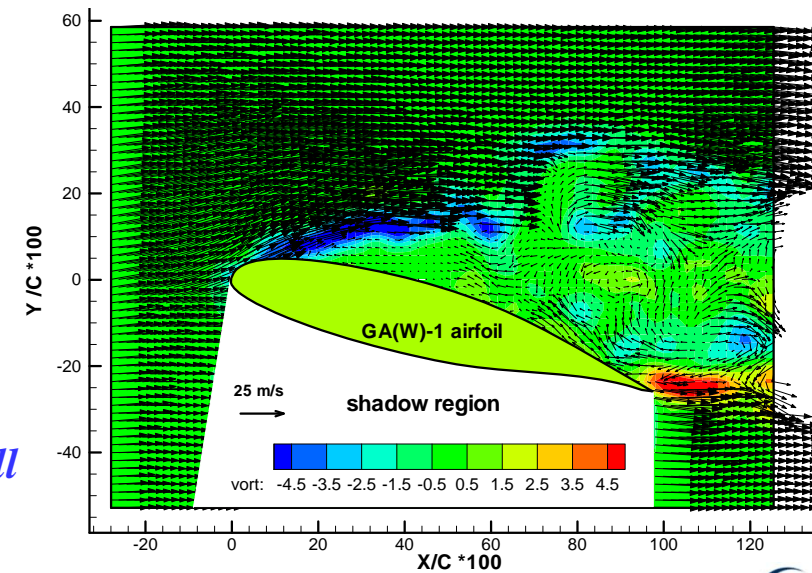
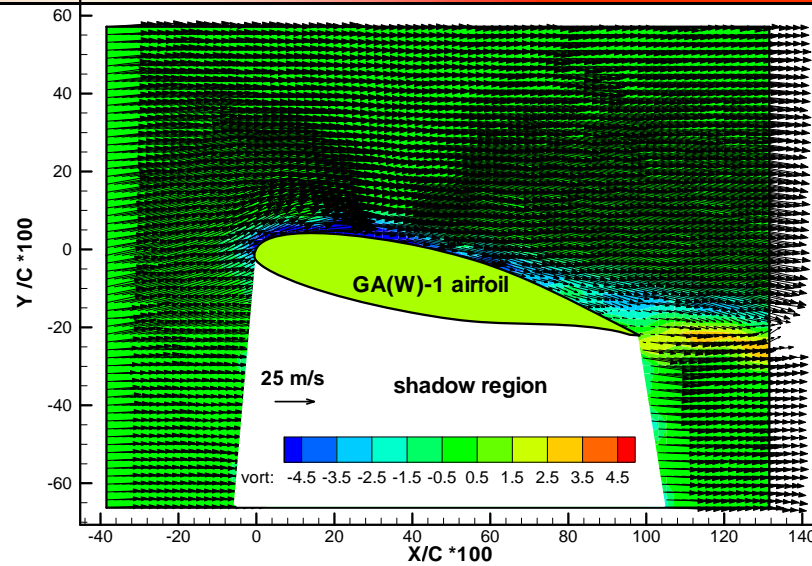
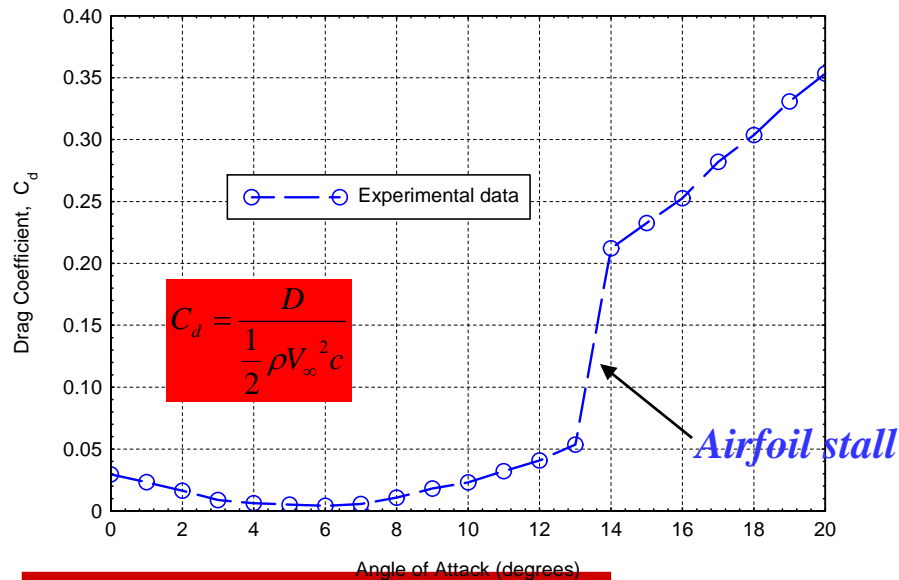
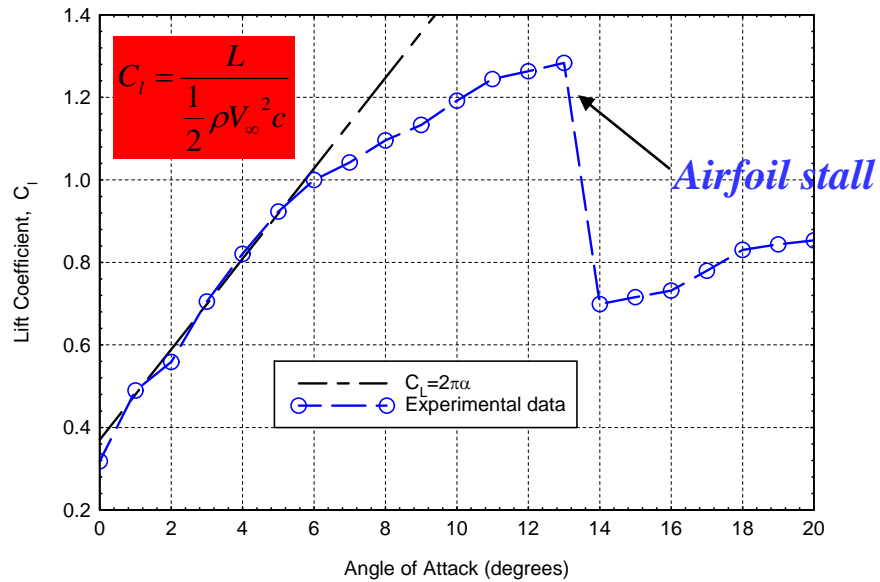


FIGURE 2: Extent of laminar flow on some famous airfoils.

# Flow Separation on an Airfoil



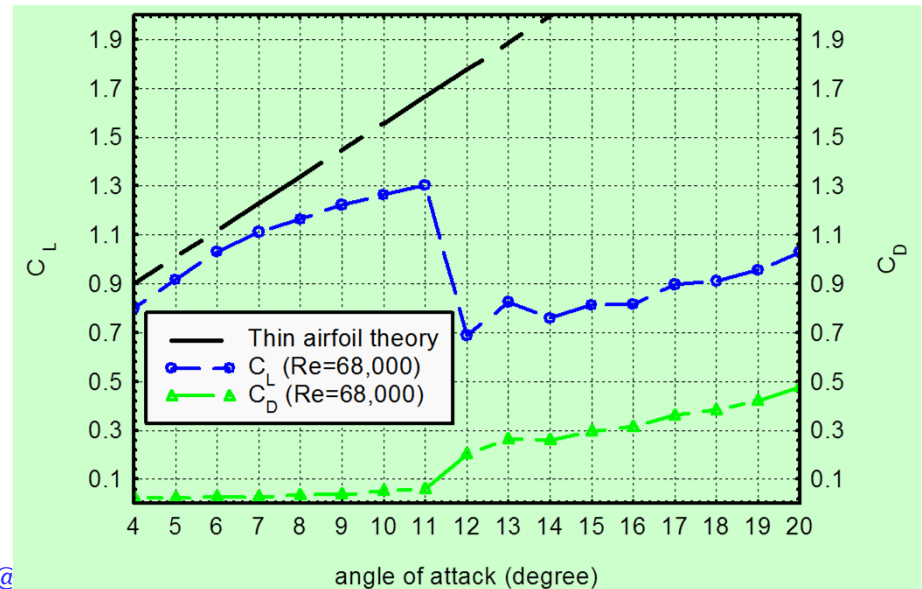
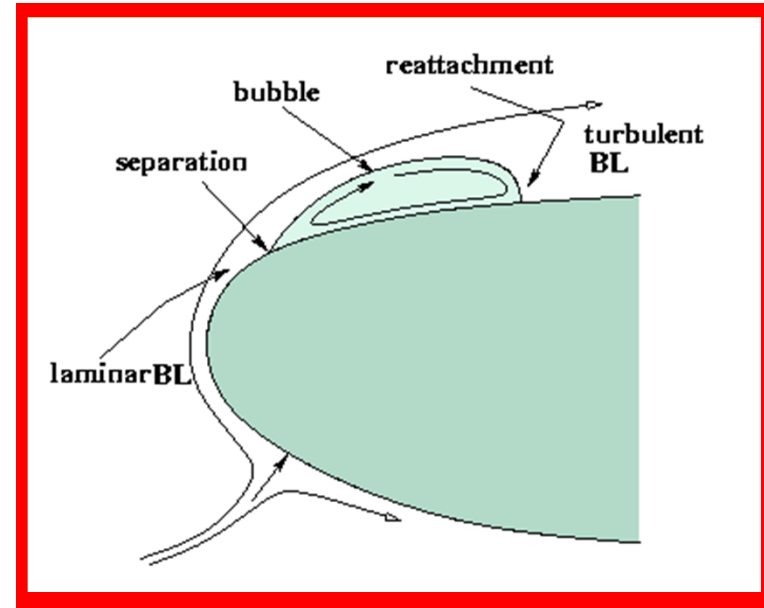
# Aerodynamic Performance of An Airfoil



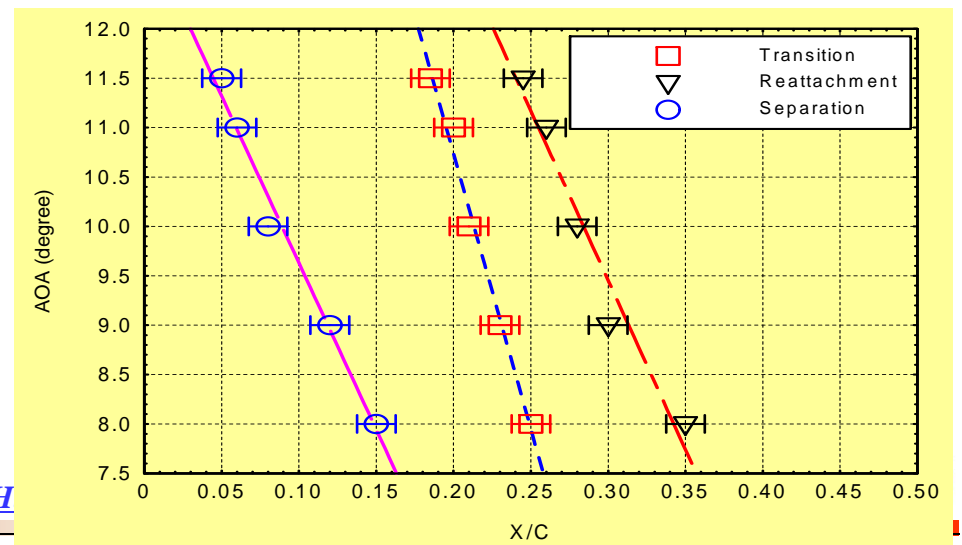
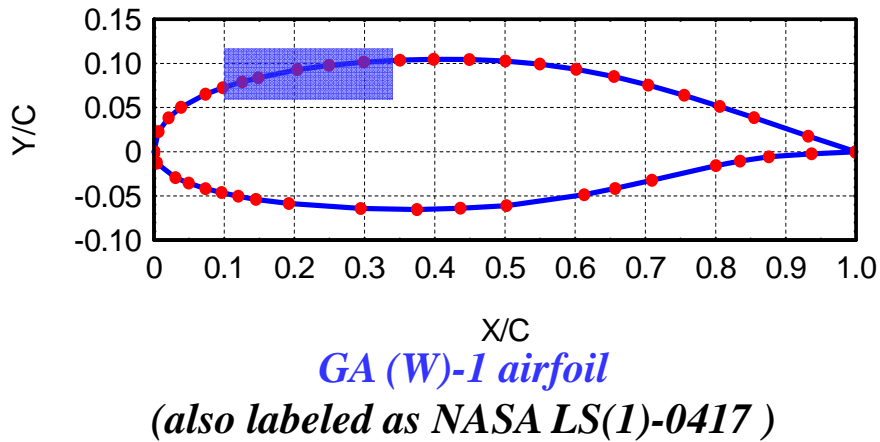
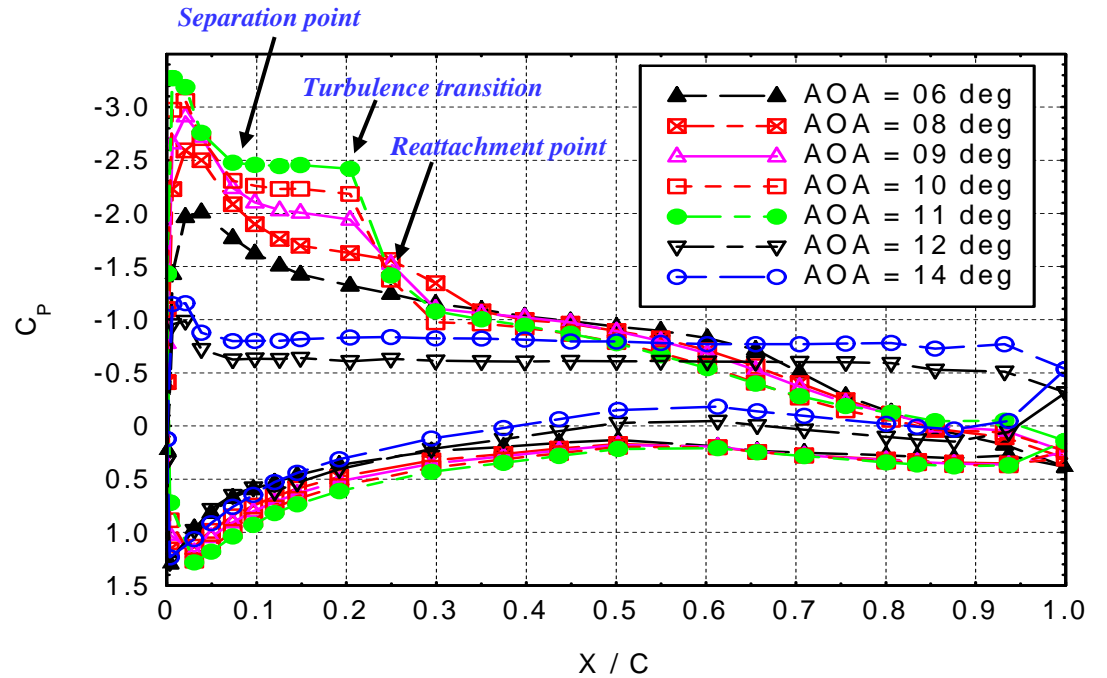
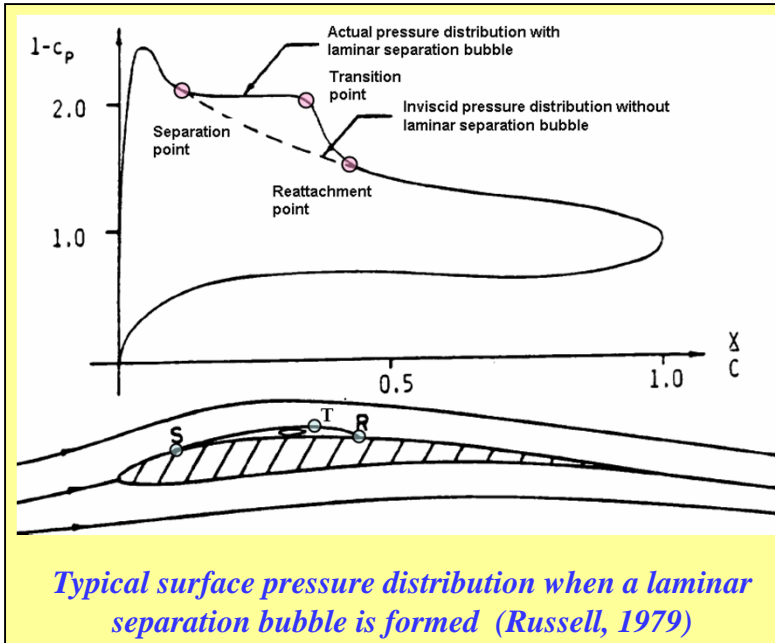


# Flow Separation and Transition on Low-Reynolds-number Airfoils

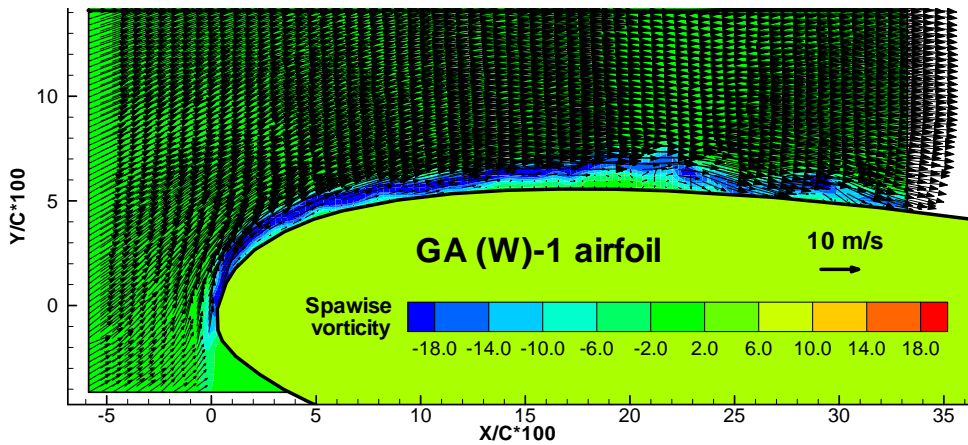
- *Low-Reynolds-number airfoil (with  $Re < 500,000$ ) aerodynamics is important for both **military** and **civilian applications**, such as **propellers, sailplanes, ultra-light man-carrying/man-powered aircraft, high-altitude vehicles, wind turbines, unmanned aerial vehicles (UAVs) and Micro-Air-Vehicles (MAVs)**.*
- *Since **laminar boundary layers** are unable to **withstand any significant adverse pressure gradient**, laminar flow separation is usually found on low-Reynolds-number airfoils. **Post-separation behavior** of the laminar boundary layers would affect the aerodynamic performances of the low-Reynolds-number airfoils significantly*
- ***Separation bubbles** are usually found to form on the upper surfaces of low-Reynolds-number airfoils. **Separation bubble would burst suddenly to cause airfoil stall at high AOA** when the **adverse pressure gradient becoming too big**.*



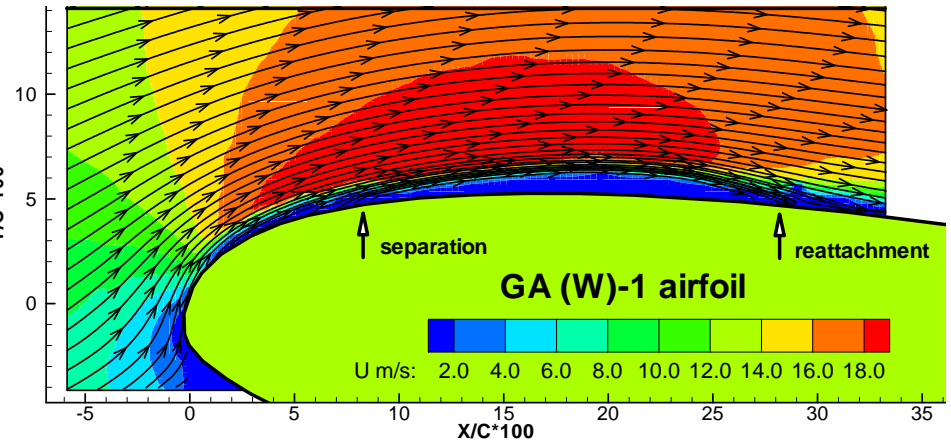
# Surface Pressure Coefficient distributions (Re=68,000)



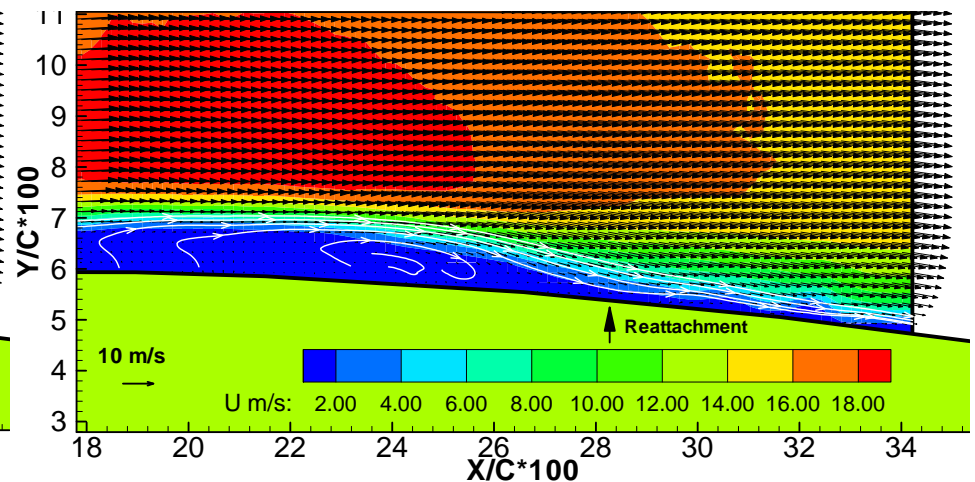
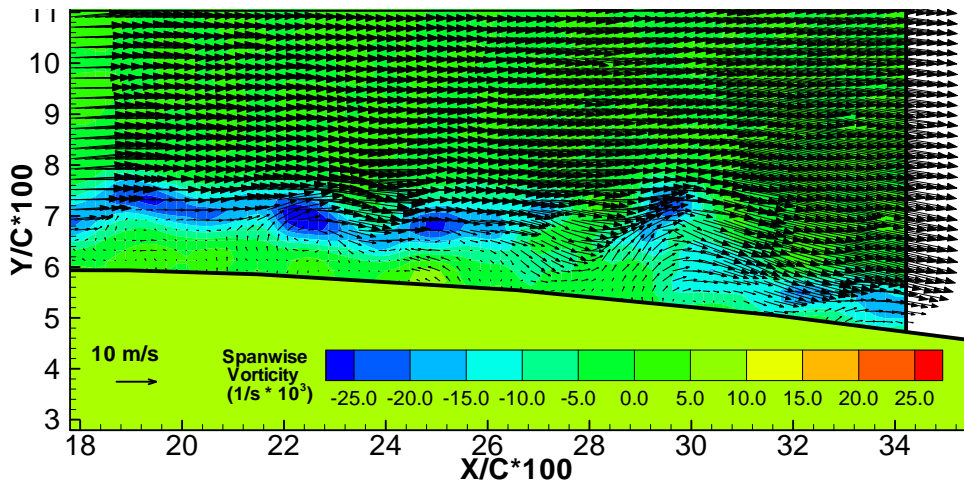
# Laminar Separation Bubble on a Low-Reynolds-number Airfoil



*Instantaneous flow field*



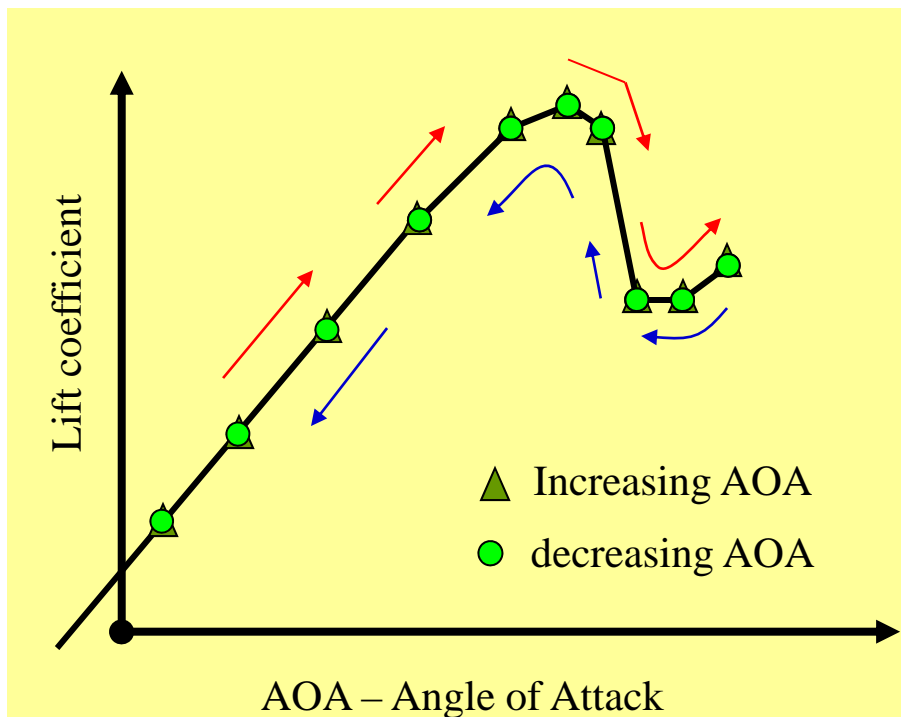
*Ensemble-averaged flow field*



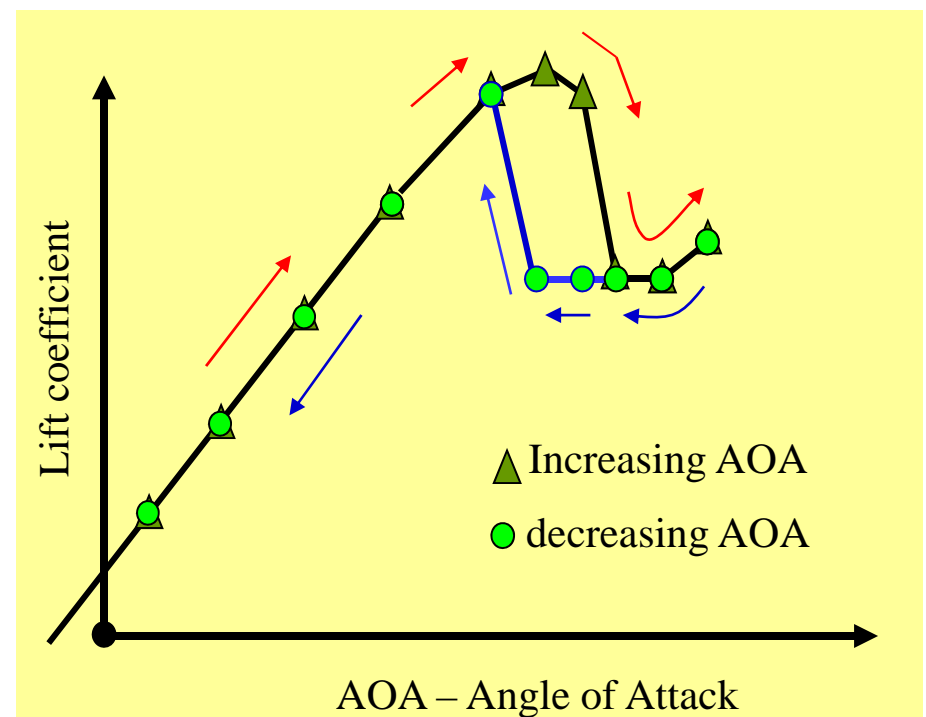
**PIV measurement results at AOA = 10 deg, Re=68,000**

# Stall Hysteresis Phenomena

- *Stall hysteresis, a phenomenon where stall inception and stall recovery do not occur at the same angle of attack, has been found to be relatively common in low-Reynolds-number airfoils.*
- *When stall hysteresis occurs, the coefficients of lift, drag, and moment of the airfoil are found to be multiple-valued rather than single-valued functions of the angle of attack.*
- *Stall hysteresis is of practical importance because it produces widely different values of lift coefficient and lift-to-drag ratio for a given airfoil at a given angle of attack. It could also affect the recovery from stall and/or spin flight conditions.*

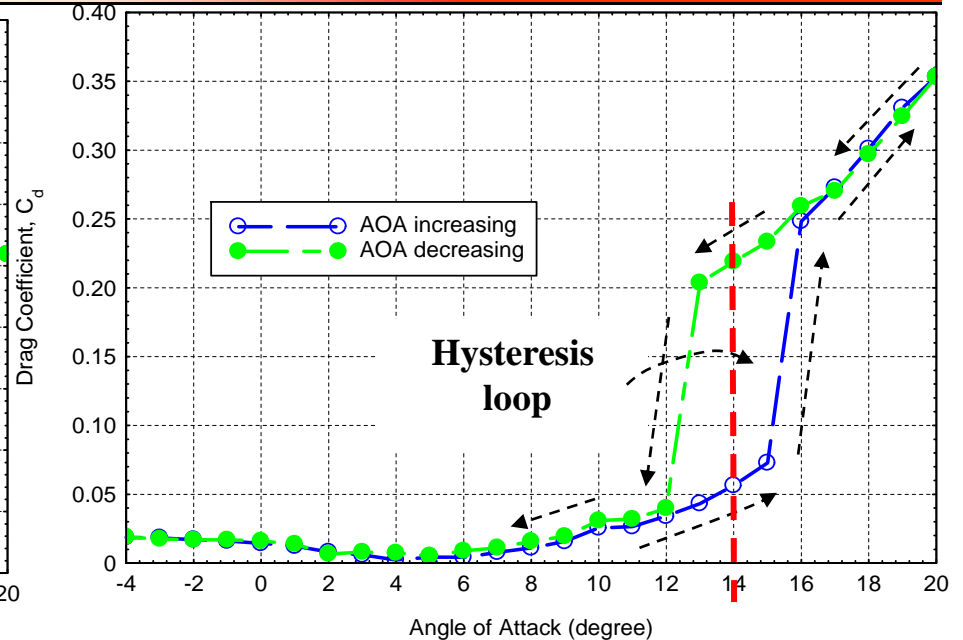
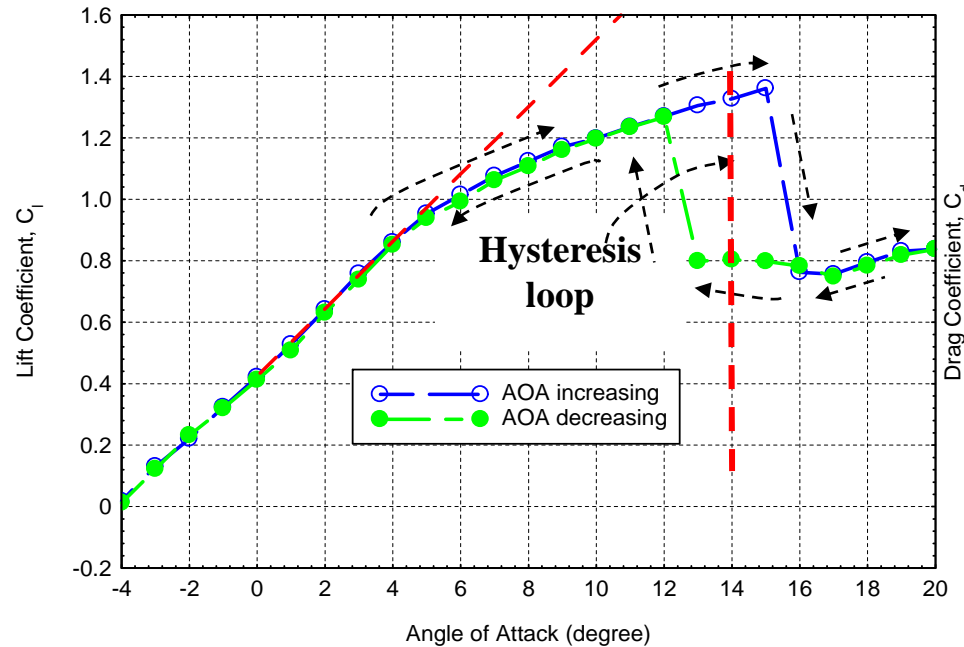


*Lift coefficient curve of a “typical” airfoil*



*Lift coefficient curve with stall hysteresis*

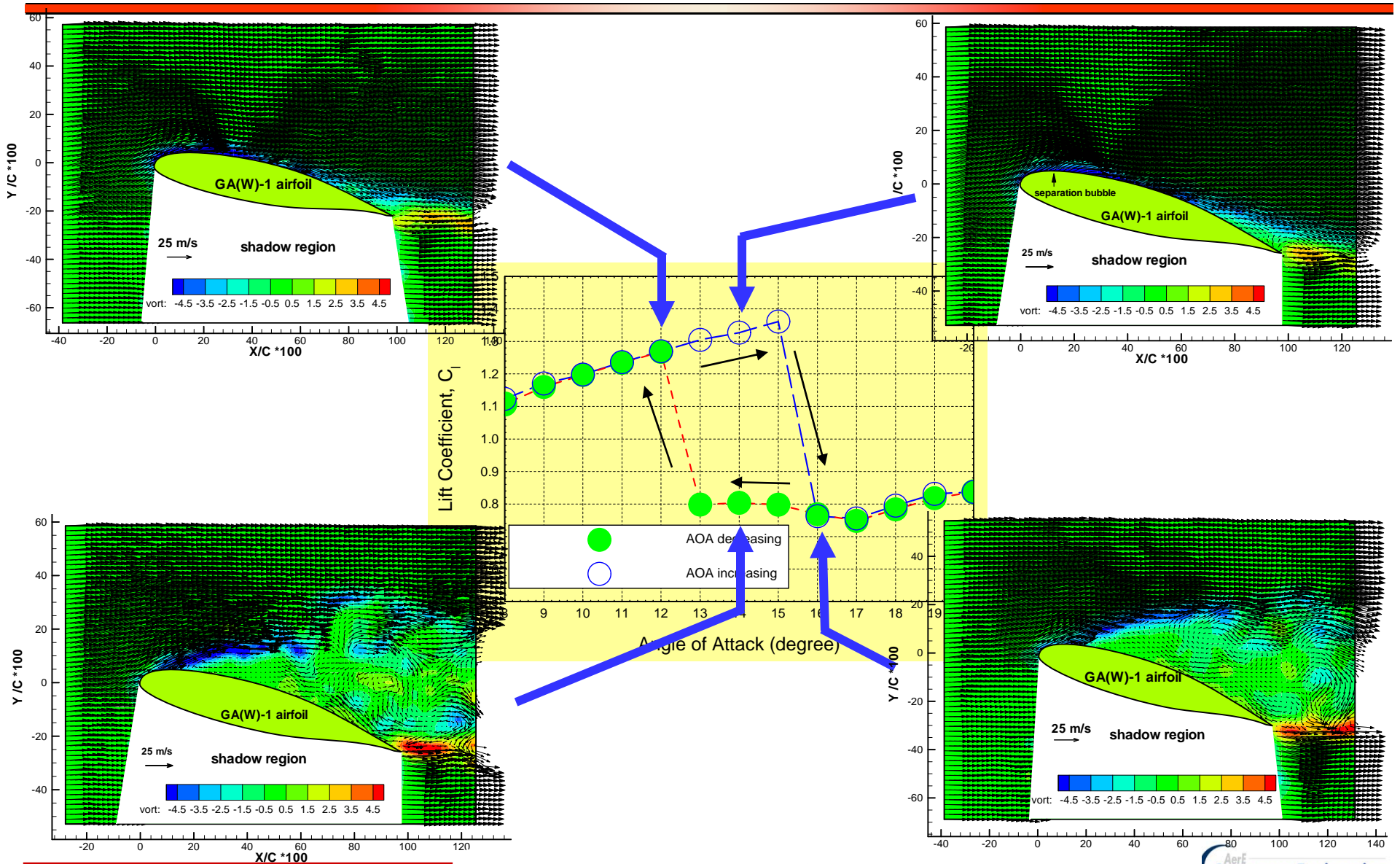
# Measured airfoil lift and drag coefficient profiles



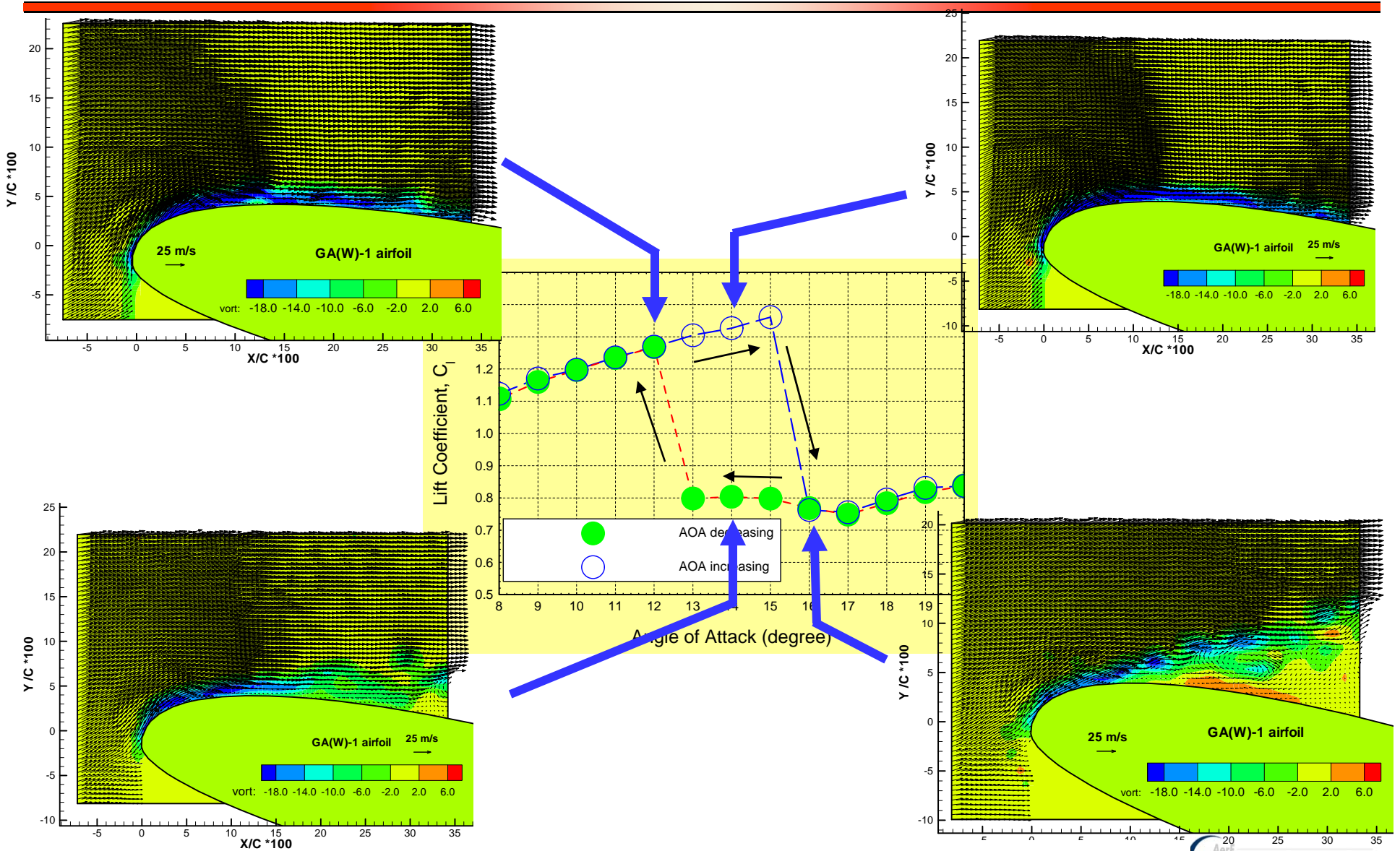
## GA(W)-1 airfoil, $Re_c = 160,000$

- The hysteresis loop was found to be *clockwise in the lift coefficient profiles, and counter-clockwise in the drag coefficient profiles.*
- The aerodynamic hysteresis resulted in *significant variations of lift coefficient,  $C_l$ , and lift-to-drag ratio,  $l/d$ , for the airfoil at a given angle of attack.*
- The lift coefficient and lift-to-drag ratio at *AOA = 14.0 degrees* were found to be  $C_l = 1.33$  and  $l/d = 23.5$  when the angle is at the *increasing angle branch of the hysteresis loop.*
- The values were found to become  $C_l = 0.8$  and  $l/d = 3.66$  for the *same AOA=14.0 degrees* when the angle is at the *decreasing angle branch of the hysteresis loop*

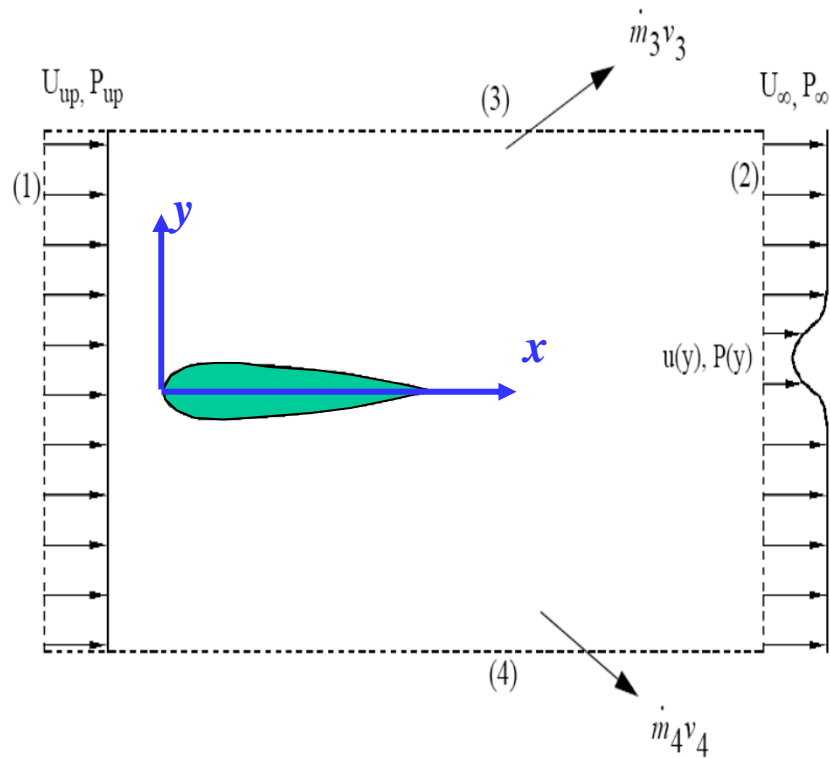
# PIV Measurement results



# Refined PIV Measurement Results



# Lab 6: Airfoil Wake Measurements and Hotwire Anemometer Calibration

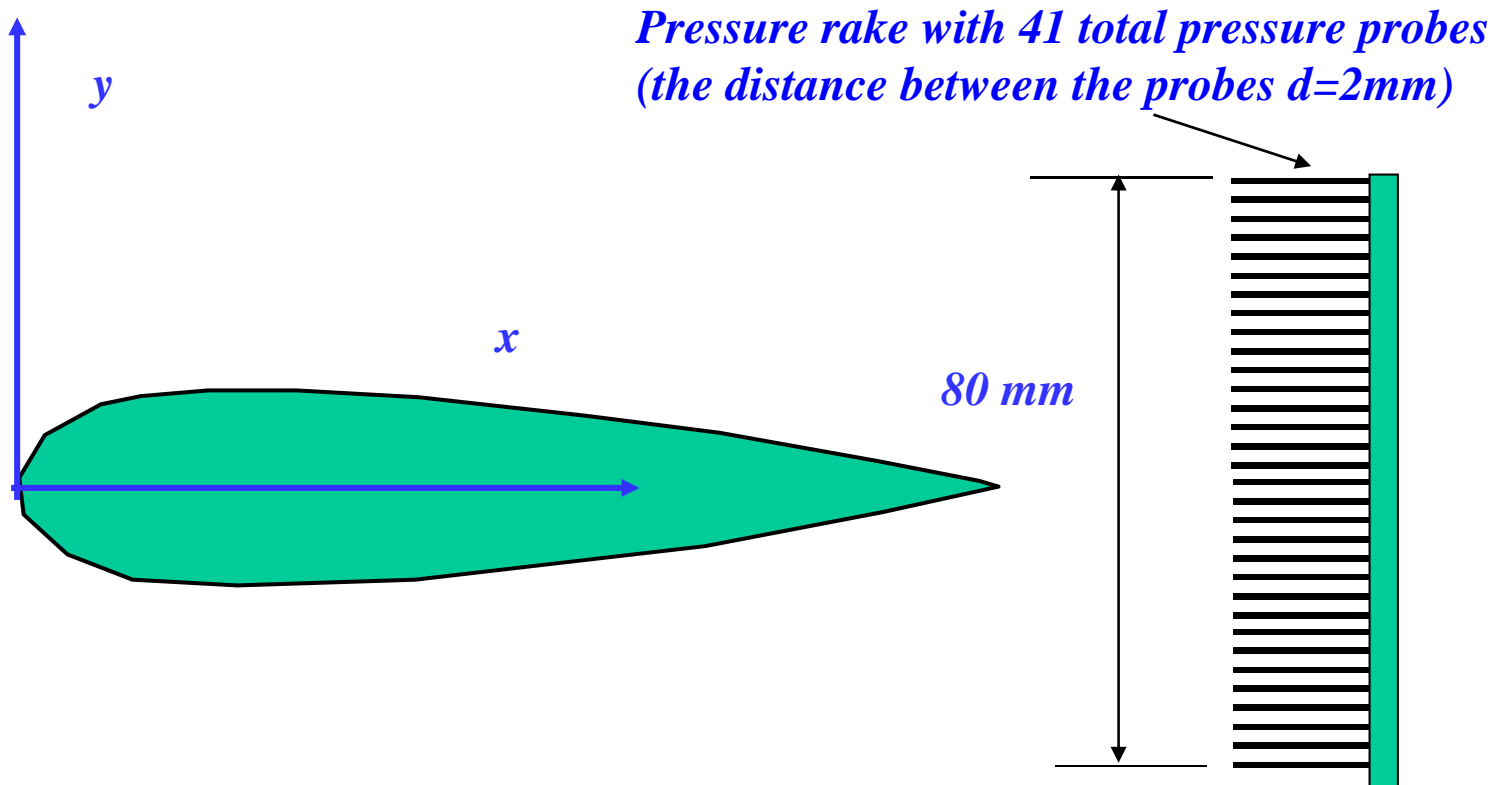


$$\begin{aligned} \sum F_x &= -D + \int_{CS} (p \hat{n} dA)_x \\ &= -D + \int_1 p_{up} dA - \int_2 p(y) dA \\ \text{Since } p_{up} &= p_{\infty}; \quad p(y) \approx p_{\infty} \\ \Rightarrow \sum F_x &= -D \\ \Rightarrow \sum F_x &= -D = \rho U_{\infty}^2 \int_2 \left[ \frac{U(y)}{U_{\infty}} \left( \frac{U(y)}{U_{\infty}} - 1 \right) \right] dA_2 \\ \Rightarrow D &= \rho U_{\infty}^2 \int_2 \left[ \frac{U(y)}{U_{\infty}} \left( 1 - \frac{U(y)}{U_{\infty}} \right) \right] dA_2 \\ C_D &= \frac{D}{\frac{1}{2} \rho U_{\infty}^2 C} = \frac{\rho U_{\infty}^2 \int_2 \left[ \frac{U(y)}{U_{\infty}} \left( 1 - \frac{U(y)}{U_{\infty}} \right) \right] dA_2}{\frac{1}{2} \rho U_{\infty}^2 C} \\ \Rightarrow C_D &= \frac{2}{C} \int_2 \left[ \frac{U(y)}{U_{\infty}} \left( 1 - \frac{U(y)}{U_{\infty}} \right) \right] dy \end{aligned}$$

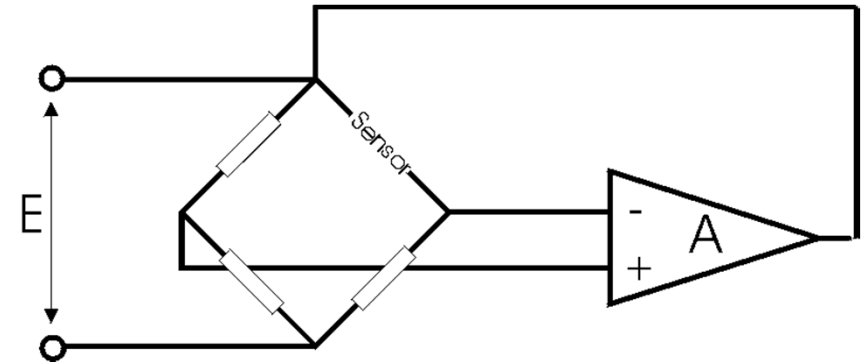
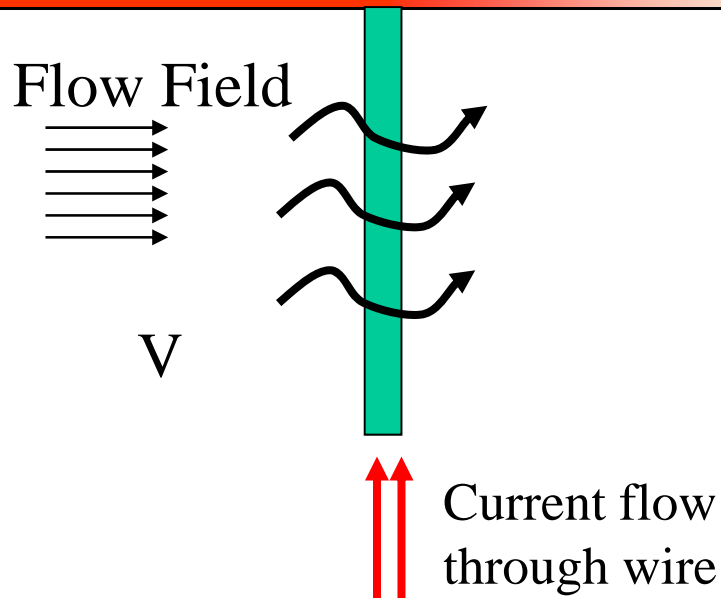
- *Compared with the drag coefficients obtained based on airfoil surface pressure measurements at the same angles of attack!*



# Lab 3: Airfoil Wake Measurements and Hotwire Anemometer Calibration

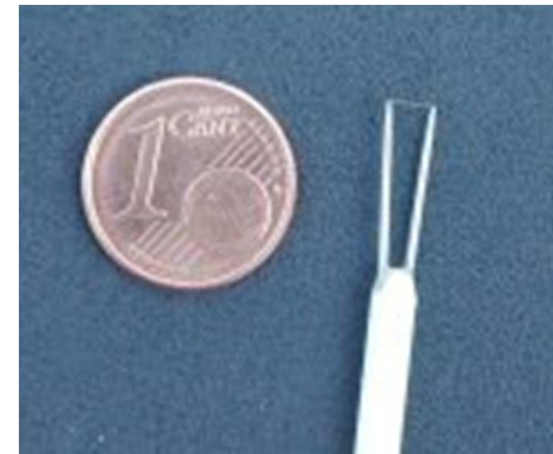


# Lab 3: Airfoil Wake Measurements and Hotwire Anemometer Calibration



$$mc \frac{dT_w}{dt} = i^2 R_w - \dot{q}(V, T_w)$$

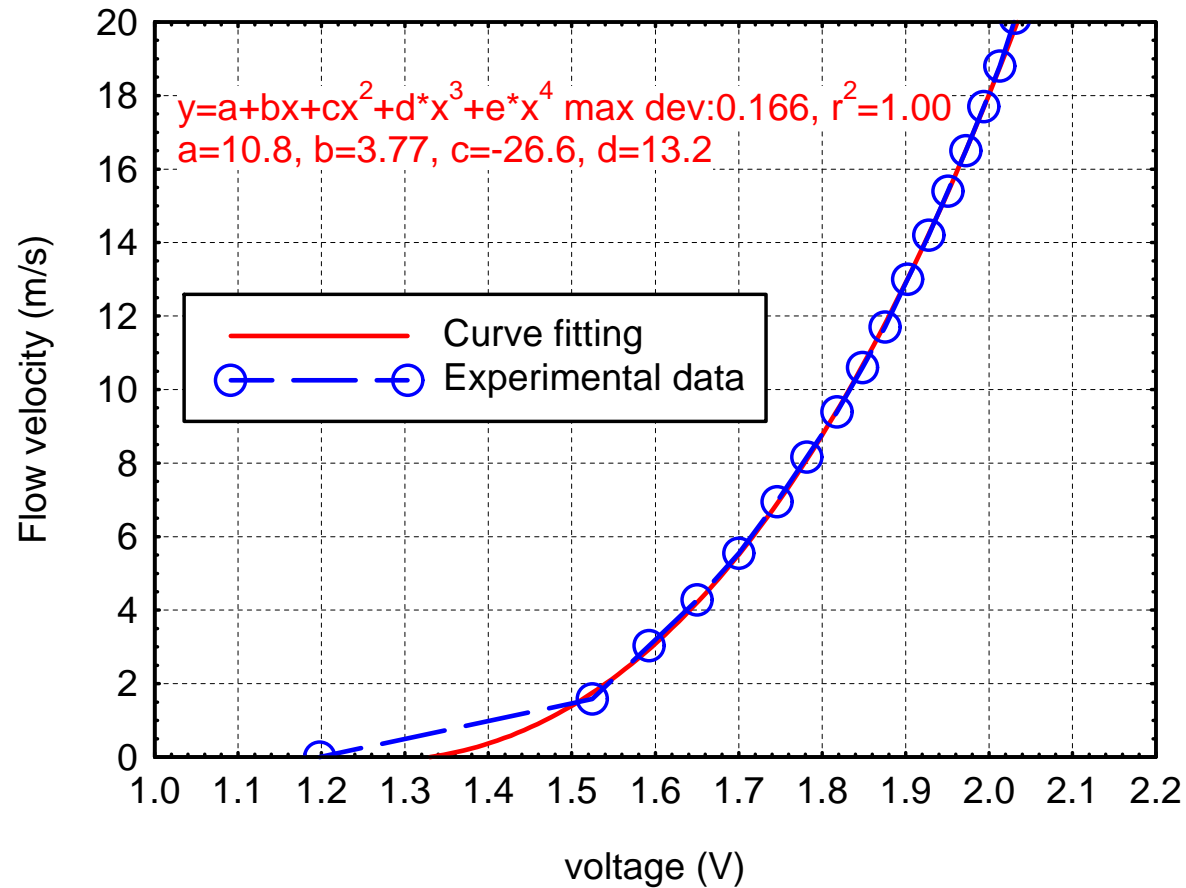
- *Constant-temperature anemometry*



*CTA hotwire probe*

# Hotwire Anemometer Calibration

- To quantify the relationship between the flow velocity and voltage output from the CTA probe



# Required Measurement Results

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## *Required Plots:*

- *$C_p$  distribution in the wake (for each angle of attack) for the airfoil wake measurements*
- *$C_d$  vs angle of attack (do your values look reasonable?) based on the airfoil wake measurements*
- *Your hot wire anemometer calibration curve: Velocity versus voltage output of hotwire anemometer (including a 4<sup>th</sup> order polynomial fit)*

## *Please briefly describe the following details:*

- *How you calculated your drag—you should show your drag calculations*
- *How these drag calculations compared with the drag calculations you made in the previous experiment.*
- *Reynolds number of tests and the incoming flow velocity*